

MEBS6006 Environmental Services 1
Exercise on 'Loading Estimation'

Consider a classroom having the following configuration and details. By using RTS Method, determine the total sensible and latent load of the classroom at 4pm (solar time) of a design day in July (July 21).

- Size: 6m × 8m × 3m(H)
 Population: 48 people (9am – 5pm) – no people other times
 Window wall: 1 no. 8m × 3m(H) (others are internal walls)
 Window area: 5 nos. 1.5m × 1m(H) – south facing, no shading, U = 1.8W/m²K, clear glass
 Roof: not required
 Assume all walls are brick walls using Wall No. 11 in Table 16 (Wall Conduction Time Series)

Solar Intensity and Sol-air temperature are presented.
 Design room temperature = 25°C, 50%rh

Step 1)
 Conduction Heat Gain through external walls and roof

$$q_{\theta} = \sum_{j=0}^{23} c_j UA(t_{e,\theta-j\delta} - t_{rc})$$

$$q_{\theta} = c_0 UA(t_{e,\theta} - t_{rc}) + c_1 UA(t_{e,\theta-\delta} - t_{rc}) + c_2 UA(t_{e,\theta-2\delta} - t_{rc}) + \dots + c_{23} UA(t_{e,\theta-23\delta} - t_{rc})$$

where

- q_{θ} = hourly conductive heat gain, Btu/h (W), for the surface
 U = overall heat transfer coefficient for the surface, Btu/h·ft²·°F (W/m²·K)
 A = surface area, ft² (m²)
 c_j = j^{th} conduction time series factor
 $t_{e,\theta-j\delta}$ = sol-air temperature, °F (°C), j hours ago
 t_{rc} = presumed constant room air temperature, °F (°C)
 θ = the current hour
 δ = the time step (one hour)

U value = 0.571 W/m²K
 Area = 8m × 3m – 5 × 1.5m × 1m = 16.5m²

Table 16 Wall Conduction Time Series (CTS)

Wall Number =	CURTAIN WALLS			STUD WALLS				EIFS			BRICK WALLS									
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
U-Factor, W/(m ² ·K)	0.428	0.429	0.428	0.419	0.417	0.406	0.413	0.668	0.305	0.52	0.571	0.577	0.283	0.581	0.348	0.628	0.702	0.514	0.581	0.389
Total R	2.3	2.3	2.3	2.4	2.4	2.5	2.4	1.5	3.3	1.9	1.7	2.7	3.5	1.7	2.9	1.6	1.4	1.9	1.7	2.6
Mass, kg/m ²	31.0	20.9	80.0	25.5	84.6	25.6	66.7	36.6	38.3	130.9	214.1	214.7	215.8	290.6	304.0	371.7	391.5	469.3	892.2	665.1
Thermal Capacity, kJ/(m ² ·K)	30.7	20.4	67.5	24.5	73.6	32.7	61.3	36.7	38.8	120.5	177.8	177.8	177.8	239.1	253.5	320.9	312.7	388.4	784.9	580.5
Hour	Conduction Time Factors, %																			
0	18	25	8	19	6	7	5	11	2	2	0	0	0	1	2	2	1	3	4	3
1	58	57	45	59	42	44	41	50	25	2	5	4	1	1	2	2	1	3	4	3
2	20	15	32	18	33	32	34	26	31	5	14	13	7	2	2	2	3	3	4	3
3	4	3	11	3	13	12	13	9	20	9	17	17	12	5	3	4	6	3	4	4
4	0	0	3	1	4	4	4	3	11	9	15	15	13	8	5	5	7	3	4	4
5	0	0	1	0	1	1	2	1	5	9	12	12	13	9	6	6	8	4	4	4
6	0	0	0	0	1	0	1	0	3	8	9	9	11	9	7	6	8	4	4	5
7	0	0	0	0	0	0	0	0	2	7	7	7	9	9	7	7	8	5	4	5
8	0	0	0	0	0	0	0	0	1	5	5	5	7	8	7	7	8	5	4	5
9	0	0	0	0	0	0	0	0	0	5	4	4	6	7	7	6	7	5	4	5
10	0	0	0	0	0	0	0	0	0	5	3	3	5	7	6	6	6	5	4	5
11	0	0	0	0	0	0	0	0	0	5	2	2	4	6	6	6	6	5	5	5
12	0	0	0	0	0	0	0	0	0	4	2	2	3	5	5	5	5	5	5	5
13	0	0	0	0	0	0	0	0	0	4	1	2	2	4	5	5	4	5	5	5
14	0	0	0	0	0	0	0	0	0	3	1	2	2	4	5	5	4	5	5	5
15	0	0	0	0	0	0	0	0	0	3	1	1	1	3	4	4	3	5	4	4
16	0	0	0	0	0	0	0	0	0	3	1	1	1	3	4	4	3	5	4	4
17	0	0	0	0	0	0	0	0	0	2	1	1	1	2	3	4	3	4	4	4
18	0	0	0	0	0	0	0	0	0	2	0	0	1	2	3	3	2	4	4	4
19	0	0	0	0	0	0	0	0	0	2	0	0	1	2	3	3	2	4	4	4
20	0	0	0	0	0	0	0	0	0	2	0	0	0	1	3	3	2	4	4	4
21	0	0	0	0	0	0	0	0	0	0	0	0	0	1	2	2	1	4	4	4
22	0	0	0	0	0	0	0	0	0	0	0	0	0	1	2	2	1	4	4	3
23	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	3	4	3
Total Percentage	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100
Layer ID from outside to inside (see Table 19)	F01 F09 F04 I02 F04 G01 F02 0	F01 F08 F04 I02 F04 G01 F02 0	F01 F10 F04 I02 F04 G01 F02 0	F01 F10 G03 I04 G01 F02 0	F01 F10 G03 I04 G01 F02 0	F01 F11 G02 I04 G04 F02 0	F01 F07 G03 I04 G01 F02 0	F01 F06 I01 G03 I04 G01 F02 0	F01 F06 I01 G03 I04 G01 F02 0	F01 F05 I01 G03 M03 F04 G01 F02 0	F01 M01 F04 I01 G03 I04 G01 F02 0	F01 M01 F04 I01 G03 I04 G01 F02 0	F01 M01 F04 I01 M03 I01 I01 I01 I01 M15	F01 M01 F04 I01 M03 I04 M05 M01 M13 M16 I04	F01 M01 F04 I01 M03 I04 M05 M01 M13 M16 I04	F01 M01 F04 I01 M03 I04 M05 M01 M13 M16 I04	F01 M01 F04 I01 M03 I04 M05 M01 M13 M16 I04	F01 M01 F04 I01 M03 I04 M05 M01 M13 M16 I04	F01 M01 F04 I01 M03 I04 M05 M01 M13 M16 I04	F01 M01 F04 I01 M03 I04 M05 M01 M13 M16 I04
Wall Number Description	<ol style="list-style-type: none"> 1. Spandrel glass, insulation board, gyp board 2. Metal wall panel, insulation board, gyp board 3. 25 mm stone, insulation board, gyp board 4. Metal wall panel, sheathing, batt insulation, gyp board 5. 25 mm stone, sheathing, batt insulation, gyp board 6. Wood siding, sheathing, batt insulation, 13 mm wood 7. 25 mm stucco, sheathing, batt insulation, gyp board 8. EIFS finish, insulation board, sheathing, gyp board 9. EIFS finish, insulation board, sheathing, batt insulation, gyp board 10. EIFS finish, insulation board, sheathing, 200 mm LW CMU, gyp board 11. Brick, insulation board, sheathing, gyp board 12. Brick, sheathing, batt insulation, gyp board 13. Brick, insulation board, sheathing, batt insulation, gyp board 14. Brick, insulation board, 200 mm LW CMU 15. Brick, 200 mm LW CMU, batt insulation, gyp board 16. Brick, insulation board, 200 mm HW CMU, gyp board 17. Brick, insulation board, brick 18. Brick, insulation board, 200 mm LW concrete, gyp board 19. Brick, insulation board, 300 mm HW concrete, gyp board 20. Brick, 200 mm HW concrete, batt insulation, gyp board 																			

The calculation is best computed using an excel spreadsheet

time	Hour ago	c	U	A	t_e	t_{rc}	q
16:00	0	0	0.571	16.5	38.6	25	0.00
15:00	1	5	0.571	16.5	39.9	25	7.02
14:00	2	14	0.571	16.5	40.6	25	20.58
13:00	3	17	0.571	16.5	41.9	25	27.07
12:00	4	15	0.571	16.5	41.4	25	23.18
11:00	5	12	0.571	16.5	39.3	25	16.17
10:00	6	9	0.571	16.5	37.7	25	10.77
9:00	7	7	0.571	16.5	36.0	25	7.25
8:00	8	5	0.571	16.5	34.0	25	4.24
7:00	9	4	0.571	16.5	31.6	25	2.49
6:00	10	3	0.571	16.5	28.7	25	1.05
5:00	11	2	0.571	16.5	28.7	25	0.70
4:00	12	2	0.571	16.5	28.8	25	0.72
3:00	13	1	0.571	16.5	28.9	25	0.37
2:00	14	1	0.571	16.5	29.1	25	0.39
1:00	15	1	0.571	16.5	29.2	25	0.40
0:00	16	1	0.571	16.5	29.4	25	0.41
23:00	17	1	0.571	16.5	29.7	25	0.44
22:00	18	0	0.571	16.5	30.0	25	0.00
21:00	19	0	0.571	16.5	30.4	25	0.00
20:00	20	0	0.571	16.5	30.8	25	0.00
19:00	21	0	0.571	16.5	31.2	25	0.00
18:00	22	0	0.571	16.5	34.4	25	0.00
17:00	23	0	0.571	16.5	36.8	25	0.00

total **123.22W**

Step 2)

Fenestration Heat Gain is separated into parts: conductive heat gain and solar radiation

Conductive heat gain

$$q_{\theta} = UA(t_{o,\theta} - t_{rc}),$$

where

- q_{θ} = hourly conductive heat gain, Btu/h (W), for the window;
- U = overall heat transfer coefficient for the window, Btu/h·ft²·°F (W/m²·K) as specified by the window manufacturer;
- A = window area—including frame, ft² (m²);
- $t_{o,\theta}$ = outdoor air temperature, °F (°C);
- t_{rc} = presumed constant room air temperature, °F (°C); and
- θ = the current hour.

$$q = 1.8 \text{ W/m}^2\text{K} \times 7.5\text{m}^2 \times (32.2 - 25)^{\circ}\text{C} = \mathbf{97.2\text{W}}$$

Solar Radiation

$$q_{SHG,D} = E_D A_{sunlit} SHGC(\theta) \quad (7.4a)$$

$$q_{SHG,d} = (E_d + E_r) A \cdot SHGC_{diffuse} \quad (7.4b)$$

$$q_{SHG} = q_{SHG,D} + q_{SHG,d} \quad (7.4c)$$

where

- $q_{SHG,D}$ = direct (beam) solar heat gain, Btu/h·ft² (W/m²)
- $q_{SHG,d}$ = diffuse solar heat gain, Btu/h·ft² (W/m²)
- q_{SHG} = total solar heat gain, Btu/h·ft² (W/m²)
- E_D = incident direct (beam) irradiation, Btu/h·ft² (W/m²)
- E_d = incident diffuse irradiation from sky, Btu/h·ft² (W/m²)
- E_r = incident diffuse reflected irradiation, Btu/h·ft² (W/m²)
- $SHGC(\theta)$ = angle-dependent SHGC determined from manufacturer's normal $SHGC$ corrected by correction factors in Table 7.9 or 3.8
- $SHGC_{diffuse}$ = the SHGC for diffuse irradiation, determined by multiplying the manufacturer's normal SHGC by the diffuse correction factor in Table 7.9 or 3.8
- A_{sunlit} = the unshaded area of the window, ft² (m²)
- A = the total area of the window, including the frame, ft² (m²)

$$q_{SHG,D} = 122.2 \text{ W/m}^2 \times 7.5\text{m}^2 \times (0.86 \times 0.488) = 384.6\text{W}$$

where $E_D = 122.2 \text{ W/m}^2$, $SHGC = \text{Normal } SHGC \times \text{Correction Factor}$

$$q_{SHG,d} = (45.4 + 39.7) \times 7.5 \text{ m}^2 \times (0.86 \times 0.907) = 497.8\text{W}$$

where $E_d = 45.4$, $E_r = 39.7$, $SHGC = \text{Normal } SHGC \times \text{Correction Factor}$

$$q_{SHG} = 384.6\text{W} + 497.8\text{W} = \mathbf{882.4\text{W}}$$

Using the same approach, assume that the solar heat gains for the 24 hours are calculated. Using RTS to convert to cooling load, the Table 7.12 should be used.

time	qSHG	RTF	
16:00	882.40	52	458.85
15:00	1051.92	16	168.31
14:00	1181.52	8	94.52
13:00	1401.12	5	70.06
12:00	1403.28	3	42.10
11:00	1189.44	2	23.79
10:00	1055.52	2	21.11
9:00	884.88	1	8.85
8:00	664.56	1	6.65
7:00	373.68	1	3.74
6:00	0.00	1	0.00
5:00	0.00	1	0.00
4:00	0.00	1	0.00
3:00	0.00	1	0.00
2:00	0.00	1	0.00
1:00	0.00	1	0.00
0:00	0.00	1	0.00
23:00	0.00	1	0.00
22:00	0.00	1	0.00
21:00	0.00	0	0.00
20:00	0.00	0	0.00
19:00	0.00	0	0.00
18:00	365.76	0	0.00
17:00	658.08	0	0.00

897.96W

Table 7.12 Representative Solar RTS Values for Light to Heavy Construction

% Glass	Light						Medium						Heavy					
	With Carpet			No Carpet			With Carpet			No Carpet			With Carpet			No Carpet		
	10	50	90	10	50	90	10	50	90	10	50	90	10	50	90	10	50	90
Hour	Radiant Time Factor, %																	
0	53	54	55	44	45	46	52	53	55	28	29	29	46	48	50	27	27	28
1	17	17	17	19	19	19	16	16	15	15	15	15	11	12	12	12	12	12
2	9	9	9	11	11	11	8	8	8	10	10	10	6	6	6	7	7	7
3	6	5	5	7	7	7	5	4	4	7	7	7	4	4	4	5	5	5
4	4	4	3	5	5	5	3	3	3	6	6	6	3	3	3	4	4	4
5	3	2	2	4	3	3	2	2	2	5	5	5	3	2	2	4	4	4
6	2	2	2	3	3	2	2	1	1	4	4	4	2	2	2	3	3	3
7	1	1	1	2	2	2	1	1	1	3	3	3	2	2	2	3	3	3
8	1	1	1	1	1	1	1	1	1	3	3	3	2	2	2	3	3	3
9	1	1	1	1	1	1	1	1	1	3	3	3	2	2	2	3	3	3
10	1	1	1	1	1	1	1	1	1	2	2	2	2	2	2	3	3	3
11	1	1	1	1	1	1	1	1	1	2	2	2	2	2	1	3	3	3
12	1	1	1	1	1	1	1	1	1	2	2	2	2	2	1	2	2	2
13	0	1	1	0	0	0	1	1	1	2	2	2	2	1	1	2	2	2
14	0	0	0	0	0	0	1	1	1	1	1	1	2	1	1	2	2	2
15	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	2	2	2
16	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	2	2	2
17	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	2	2	2
18	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	2	2	2
19	0	0	0	0	0	0	0	1	0	1	1	1	1	1	1	2	2	2
20	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	2	2	2
21	0	0	0	0	0	0	0	0	0	1	0		1	1	1	2	2	2
22	0	0	0	0	0	0	0	0	0		0	0	1	1	1	2	2	1
23	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1
	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100

Step 3)

Let Occupant heat gain = 65W (sensible), 30W(latent)

Occupant sensible (radiant) = 65W × 0.6 = 39W/person → 48 × 39W = 1872W

Occupant sensible (convective) = 65W × 0.4 = 26W/person → 48 × 26W = 1248W

Occupant latent = 48 × 30W = 1440W

Let lighting load = 15W/m² → 48m² × 15W/m² = 720W

Assume radiant fraction = 0.6, space fraction = 0.4

Lighting load (radiant) = 720W × 0.6 = 432W

Lighting load (convective) = 720W × 0.4 = 288W

Using RTS to convert to cooling load, the Table 7.11 should be used.

Total internal radiant load = 1872W + 432W = 2304W

time	Q _{sen}	RTF	
16:00	2304	46	1059.84
15:00	2304	17	391.68
14:00	2304	9	207.36
13:00	2304	5	115.2
12:00	2304	3	69.12
11:00	2304	2	46.08
10:00	2304	2	46.08
9:00	2304	1	23.04
8:00	0	1	0
7:00	0	1	0
6:00	0	1	0
5:00	0	1	0
4:00	0	1	0
3:00	0	1	0
2:00	0	1	0
1:00	0	1	0
0:00	0	1	0
23:00	0	1	0
22:00	0	1	0
21:00	0	1	0
20:00	0	1	0
19:00	0	1	0
18:00	0	1	0
17:00	2304	0	0

1958.4W

Step 4)

Ventilation load

Consider each person demands 8L/s of fresh air

Total fresh air = $48 \times 8\text{L/s} = 384 \text{ L/s} = 0.384\text{m}^3/\text{s}$

Consider

outdoor air condition = 32.2°C DB, 26.7°C WB → $w = 20.02 \text{ g/kg}$

indoor air condition = 25°C DB, 50%rh → $w = 9.92 \text{ g/kg}$

sensible load = $1.23 \times 0.384 \times (32.2 - 25) = 3.4\text{kW}$

latent load = $3010 \times 0.384 \times (20.02 - 9.92)/1000 = 11.7\text{kW}$

Table 7.11 Representative Nonsolar RTS Values for Light to Heavy Construction

% Glass	Light						Medium						Heavy						Interior Zones					
	With Carpet			No Carpet			With Carpet			No Carpet			With Carpet			No Carpet			Light		Medium		Heavy	
	10	50	90	10	50	90	10	50	90	10	50	90	10	50	90	10	50	90	10	50	10	50	10	50
Hour	Radiant Time Factor, %																							
0	47	50	53	41	44	44	46	49	52	31	33	36	34	38	42	22	25	29	46	41	45	30	33	22
1	19	18	17	20	19	19	17	17	16	16	16	15	9	9	9	9	9	9	19	20	18	17	9	9
2	11	10	9	12	11	11	9	9	8	11	10	10	6	6	5	6	6	6	11	12	10	11	6	6
3	6	6	6	7	7	7	5	5	4	7	7	7	5	4	4	5	5	5	7	8	6	8	5	5
4	4	4	4	5	5	5	3	3	3	6	5	5	4	4	4	5	5	4	4	5	4	6	4	5
5	3	3	2	4	3	3	2	2	2	4	4	4	4	3	3	4	4	4	3	4	2	4	4	4
6	2	2	2	3	3	3	2	2	2	4	4	3	3	3	3	4	4	4	2	3	2	4	3	4
7	2	1	1	2	2	2	1	1	1	3	3	3	3	3	3	4	4	4	2	2	1	3	3	4
8	1	1	1	2	1	1	1	1	1	3	3	2	3	3	3	4	3	3	1	2	1	3	3	4
9	1	1	1	1	1	1	1	1	1	2	2	2	3	3	2	3	3	3	1	1	1	2	3	3
10	1	1	1	1	1	1	1	1	1	2	2	2	3	2	2	3	3	3	1	1	1	2	3	3
11	1	1	1	1	1	1	1	1	1	2	2	2	2	2	2	3	3	3	1	1	1	2	3	3
12	1	1	1	1	1	1	1	1	1	1	1	2	2	2	2	3	3	3	1	0	1	1	2	3
13	1	1	1	0	1	1	1	1	1	1	1	1	2	2	2	3	3	2	1	0	1	1	2	3
14	1	0	0	0	0	0	1	1	1	1	1	1	2	2	2	3	2	2	0	0	1	1	2	3
15	0	0	0	0	0	0	1	1	1	1	1	1	2	2	2	3	2	2	0	0	1	1	2	3
16	0	0	0	0	0	0	1	1	1	1	1	1	2	2	2	2	2	2	0	0	1	1	2	2
17	0	0	0	0	0	0	1	1	1	1	1	1	2	2	2	2	2	2	0	0	1	1	2	2
18	0	0	0	0	0	0	1	1	1	1	1	1	2	2	1	2	2	2	0	0	1	1	2	2
19	0	0	0	0	0	0	1	1	1	1	1	1	2	2	1	2	2	2	0	0	1	1	2	2
20	0	0	0	0	0	0	1	0	0	1	1	0	2	1	1	2	2	2	0	0	0	0	2	2
21	0	0	0	0	0	0	1	0	0	0	0	0	1	1	1	2	2	2	0	0	0	0	1	2
22	0	0	0	0	0	0	1	0	0	0	0	0	1	1	1	2	2	1	0	0	0	0	1	2
23	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	2	2	1	0	0	0	0	1	2
	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100	100

Step 5)
Consolidation of Sensible and Latent Load

	Sensible (W)		Latent (W)
	Radiant	Convective	
Wall (CTS)		123	
Fenestration	898	97	
Occupant	1958	1248	1440
Lighting		288	
Ventilation		3400	11700
Total	8012		13140