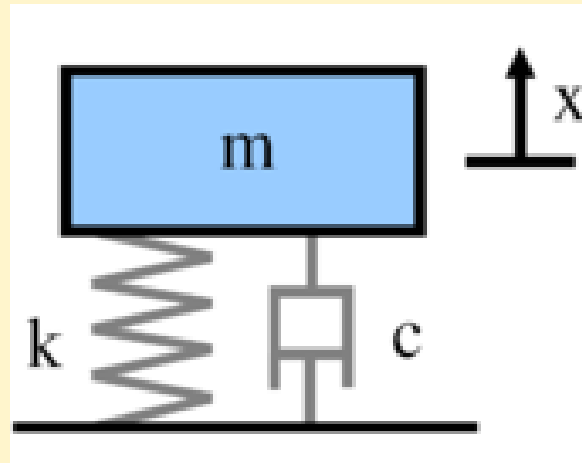


# MEBS6008 Environmental Services II

<http://www.hku.hk/mech/msc-courses/MEBS6008/index.html>



## Acoustic Treatment – Vibration Control



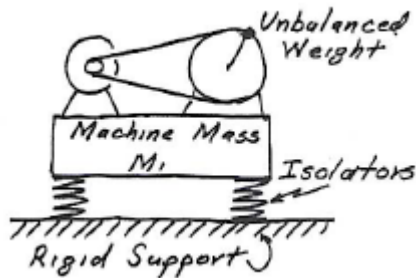
Department of Mechanical Engineering  
The University of Hong Kong

# Content



- **Fundamental of Vibration**
- **Vibration isolation**
- **Single Degree of Freedom Model**
- **Modes of Vibration**
- **Transmissibility and Isolation Efficiency**
- **Two Degree of Freedom Model**
- **Selection Guide for Vibration Isolator**
- **Vibration Control in Practice**

# Fundamental of Vibration



A **rigidly mounted** machine transmits its internal vibratory forces directly to the supporting structure.

**Vibration isolators** is resilient mountings

By inserting **isolators between the machine and supporting structure**, the magnitude of transmitted vibration can be reduced (%).

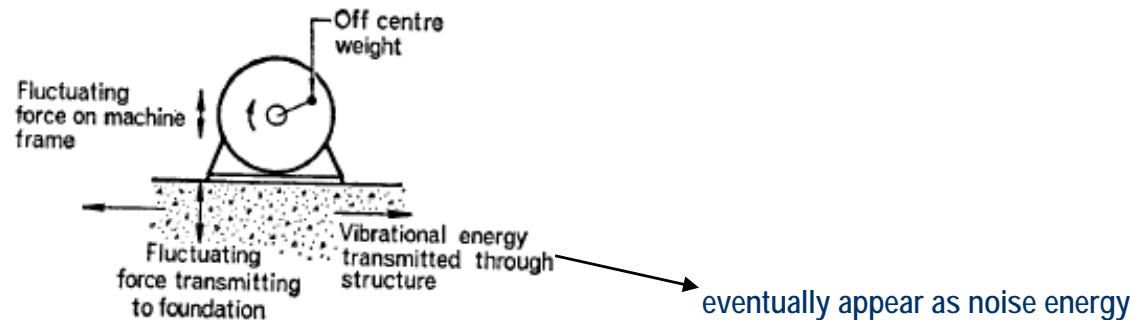
Vibration isolators can also be used to protect **sensitive equipment** from disturbing vibrations.

Vibration energy from mechanical equipment → transmitted to the building structure → radiated as **structure-borne noise**.

# Vibration isolation



Any residual, **out-of-balance force** in the rotating parts as a weight located eccentrically.

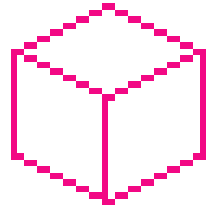


The weight rotates  $\rightarrow$  each part of the machine structure subjected to a **cyclic force** from inertia of the rotating off-centre height

**Vertical component** of the force is concerned  $\rightarrow$  acting alternately upwards and downwards, at a **frequency** equal to the shaft rotational frequency.

Other case of cyclic force example: Combustion loads in reciprocating engines

# Single Degree of Freedom Model



Only motion along the vertical axis is considered , damping is disregarded

Valid only **when the stiffness of the supporting structure  $\gg$  the stiffness of the vibration isolator.**

(mechanical equipment on G/F or basement locations)

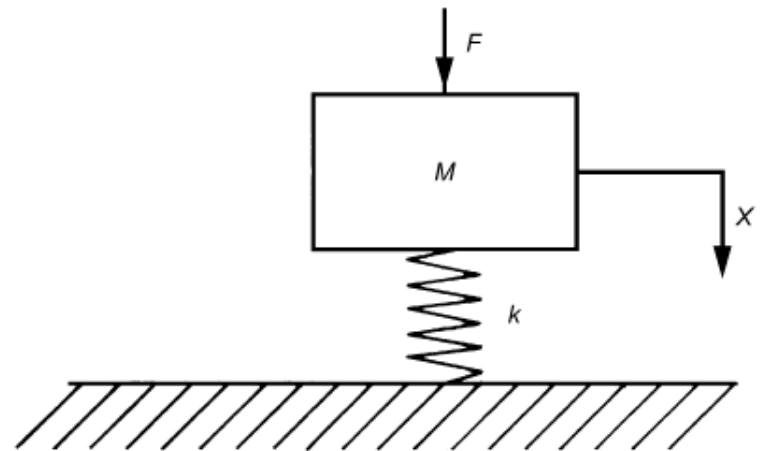
**Natural frequency** of the isolator : deflect the spring a little more + suddenly release it  $\rightarrow$  the machine oscillate vertically about its rest position at natural frequency.

The **natural frequency**  $f_n$  of the system is

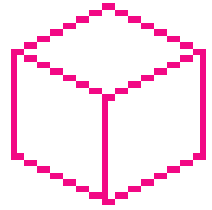
$$f_n = \frac{1}{2\pi} \sqrt{\frac{k}{M}}$$

where  **$k$  is the stiffness** of vibration isolator (force per unit deflection)

**$M$  is mass** of the equipment supported by isolator.



Single-Degree-of-Freedom System

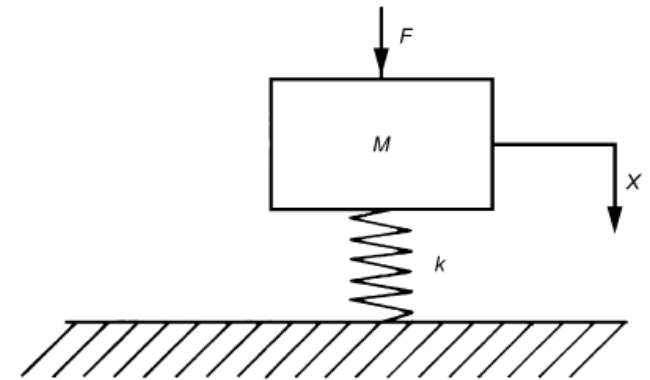


# Single Degree of Freedom Model

This model is the one upon which most manufacturers of vibration isolation hardware base their **catalog** information.

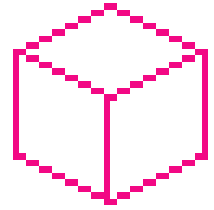
It is valid only when the **stiffness** of the supporting structure is **large** with respect to the stiffness of the vibration isolator.

This condition is usually satisfied for mechanical equipment in **on-grade** or **basement** locations.

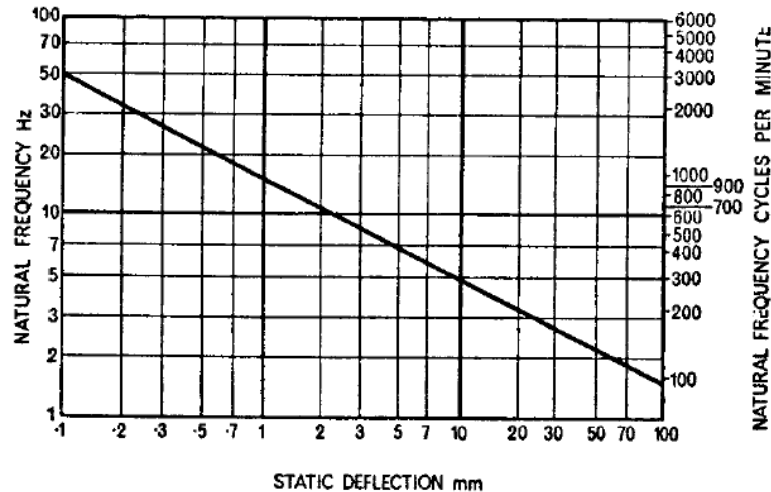


Single-Degree-of-Freedom System

# Single Degree of Freedom Model



$$f_n = \frac{1}{2\pi} \sqrt{\frac{k}{M}} \quad \xrightarrow{\text{This equation simplifies to (try yourself, noting the unit of g)}} \quad f_n = \frac{15.8}{\sqrt{\delta_{st}}}$$



where  $\delta_{st}$  is the isolator static deflection in mm,  $k/M = g/\delta_{st}$ .

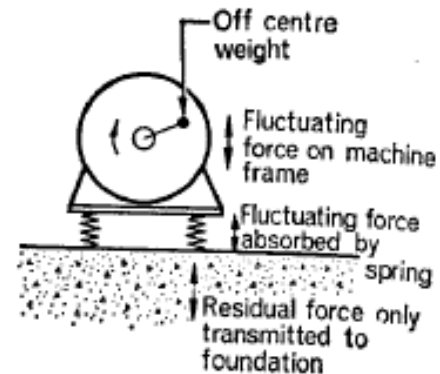
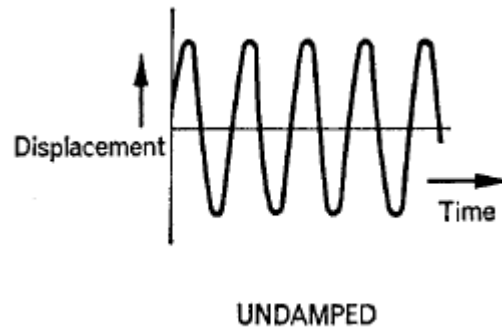
Static deflection = incremental distance the isolator spring compressed under equipment weight.

Isolator static deflection & supporting load  $\rightarrow$  achieve the **appropriate system natural frequency**

# Modes of Vibration - Undamped



Use the steel spring as vibration isolator.



The machine settles under its own weight

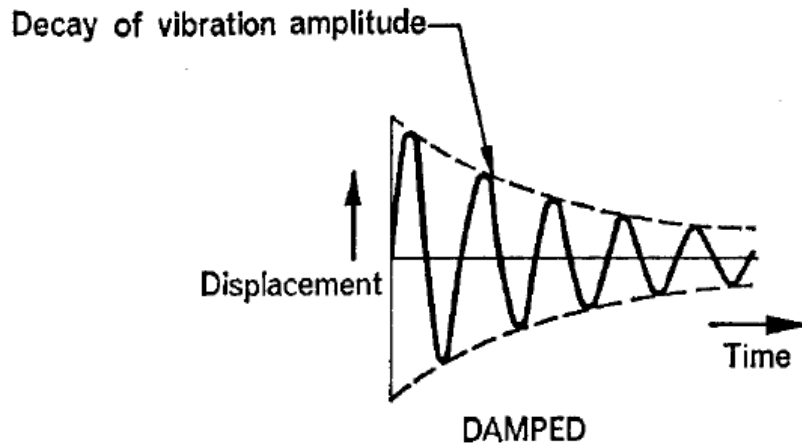
The machine deflects the spring by a certain amount → **static deflection** of the isolator

Static deflection determines the **eventual performance** of the spring as an isolator when the machine is running.

Static deflection depends **only** upon **static stiffness of the spring** , **weight of the machine**.



# Modes of Vibration - Damped Vibration



## Damped Vibration

Real isolators have a certain degree of **internal damping**

Energy is progressively removed from the system

**Amplitude** of vibration steadily **reduces**  
Large amount of damping → movement of the mass back to its rest position after initial deflection will be very sluggish

**Neither overshoot nor oscillate**

## Critical damping

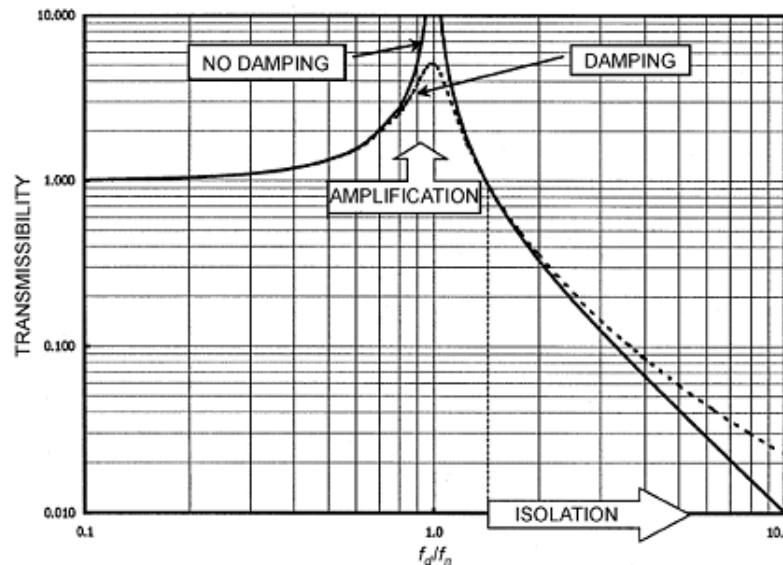
Amount of damping just **sufficient for mass to return to its mean position in min. time without overshoot**

# Transmissibility and Isolation Efficiency



$$\text{Transmissibility} = \frac{\text{Force transmitted to the foundation}}{\text{Force applied by the machine}}$$

Transmissibility  $T$  is **inversely proportional to** the square of the ratio of the disturbing frequency  $f_d$  to the system natural frequency  $f_n$ , or



$$T = \left| \frac{1}{1 - (f_d/f_n)^2} \right|$$

Vibration Transmissibility  $T$  as a Function of  $f_d/f_n$

# Transmissibility and Isolation Efficiency

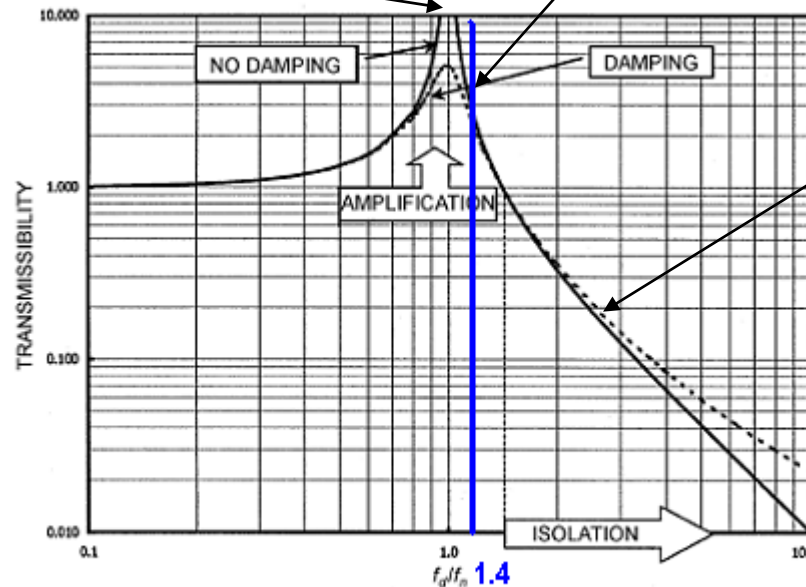


Vibration isolation begin after  $f_d/f_n > 1.4$ .

At  $f_d = f_n$ , resonance occurs (the denominator of Equation equals zero)

At resonance  
→ theoretically infinite transmission of vibration.

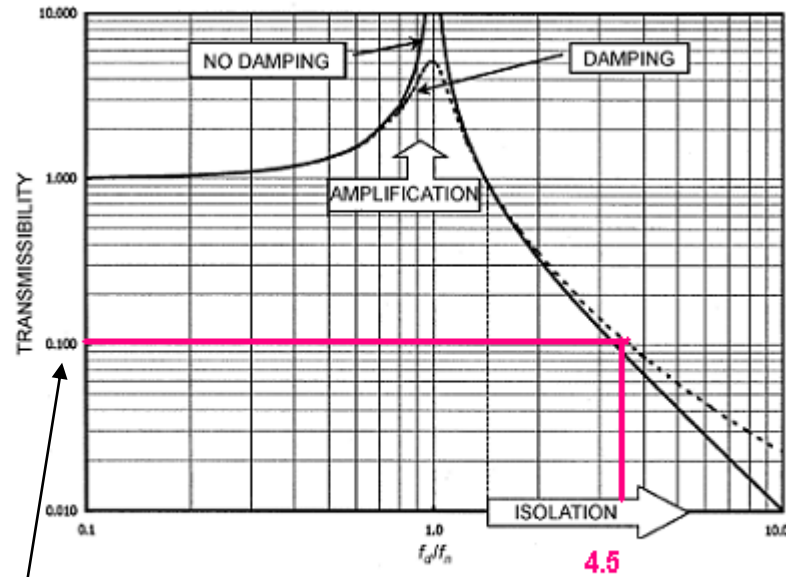
In practice, some limit on the transmission at resonance exists due to some inherent damping.



Vibration transmissibility rapidly decreases.

Vibration Transmissibility  $T$  as a Function of  $f_d/f_n$

# Transmissibility and Isolation Efficiency



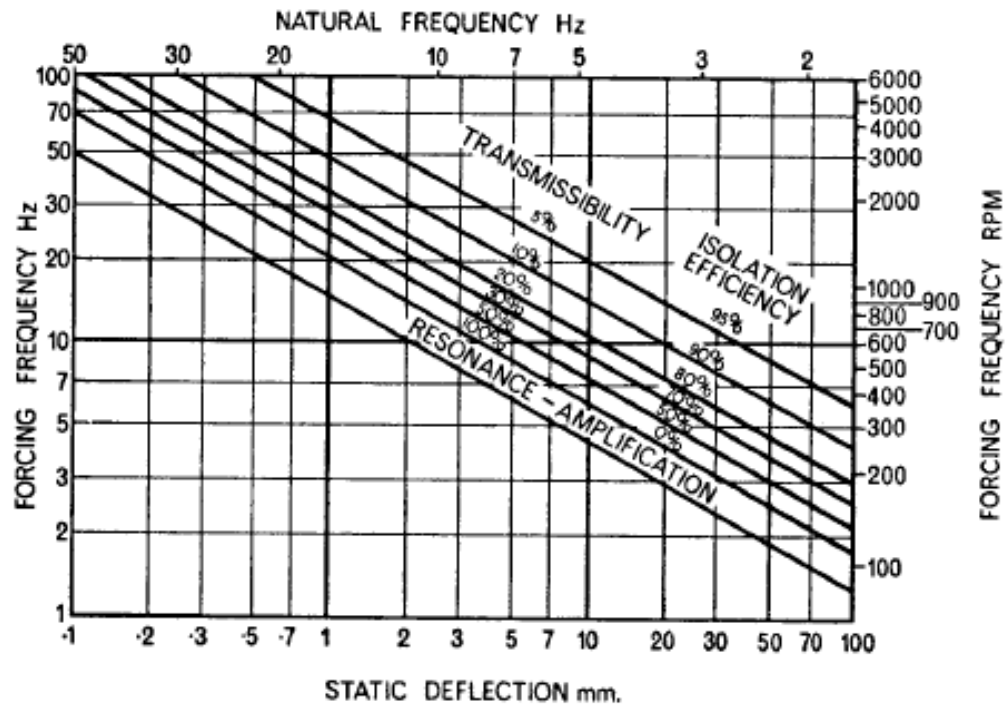
Vibration Transmissibility  $T$  as a Function of  $f_d/f_n$

A frequency ratio of at least 4.5 is often specified, which corresponds to an isolation efficiency of about 90%, or 10% transmissibility.

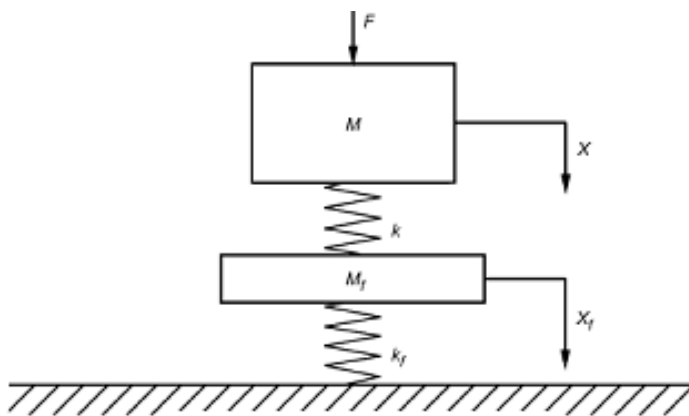
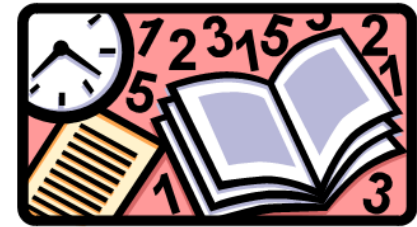
Higher ratios may be specified, but in practice this is difficult to achieve.

Nonlinear characteristics cause typical isolators to depart from the theoretical curve.

# Transmissibility and Isolation Efficiency



# Two Degree of Freedom Model



Two-Degree-of-Freedom System

$M$  and  $M_f$  represent effective masses of vibrating equipment and supporting floor, respectively;  $k$  and  $k_f$  are corresponding stiffness of isolator and floor system.

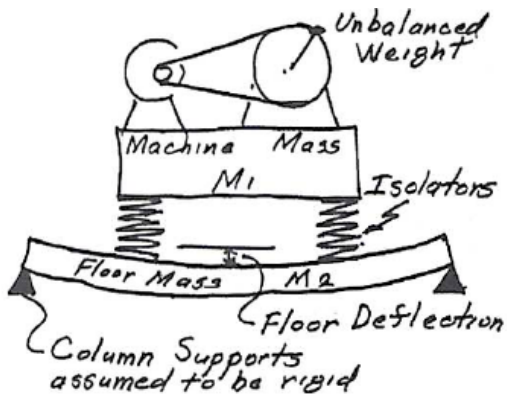
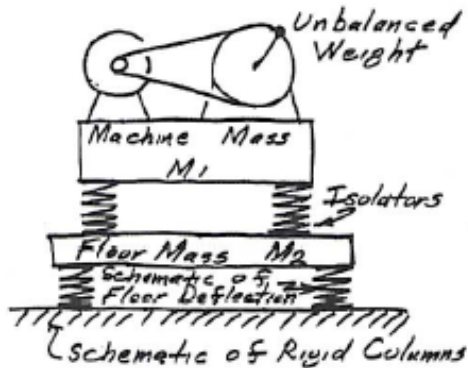
When heavy mechanical equipment is installed on a structural floor( especially roof), **the stiffness of the supporting structure may NOT be  $\gg$  the stiffness of the vibration isolator.**

Significantly "softer" vibration isolators are usually required in this case.

Two-degree-of-freedom model for the design of **vibration isolation in upper-floor locations.**



# Two Degree of Freedom Model



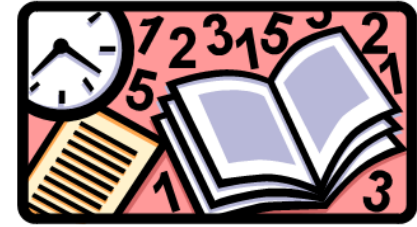
The **precise behavior** of this system with respect to vibration isolation is difficult to determine.

The objective is to **minimize the motion** of the supporting floor  $M_f$  in response to the exciting force  $F$ .

Evaluating the **interaction between two system natural frequencies** and the frequency of the exciting force  $\rightarrow$  complicated

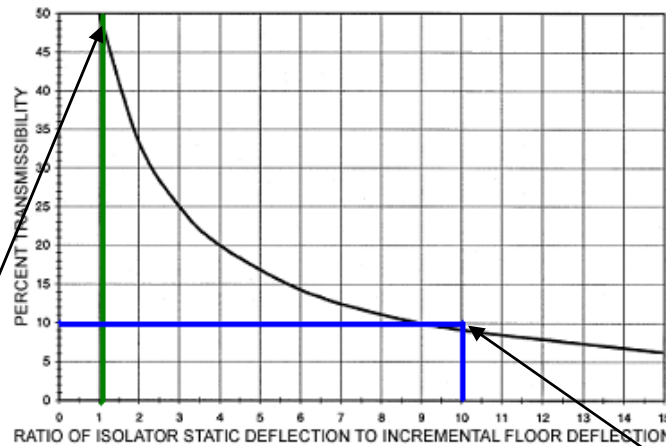
Fraction of vibratory force transmitted across an isolator to the building structure (transmissibility) depends in part the **isolator stiffness comparing with that of supporting floor**.

# Two Degree of Freedom Model



Ratio = isolator static deflection / incremental floor deflection

To optimize isolation efficiency → static deflection of the loaded isolator >> incremental static deflection of the floor under added equipment weight.

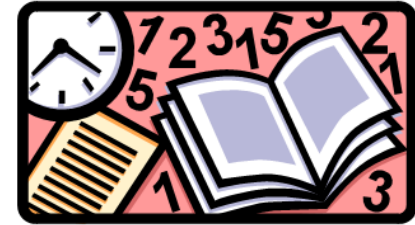


Floor deflection → excessive vibration is attributable to upper floor or rooftop mechanical installations.

Static deflection of the vibration isolator is = incremental deflection of the supporting floor under the added weight of the equipment → 50% of the vibratory force

Ideally, this ratio should be on the order of 10:1 to approach an isolation efficiency of about 90%.





# Two Degree of Freedom Model

Selection of vibration isolators on the basis of the single-degree-of-freedom model → neglected floor stiffness → inadequate

## Steps to choose vibration isolators with consideration of floor stiffness

Asking **structural** engineer to estimate the incremental static deflection of the floor due to the added weight of the equipment at the point of loading

Choose an isolator that will provide a static deflection of **8 to 10 times** that of the estimated incremental floor deflection.

Consider **also building spans, equipment operating speeds, equipment power, damping and other factors**

## Remarks

The type of equipment, proximity to noise-sensitive areas, and the type of building construction may alter these choices.



# Selection Guide for Vibration Isolator

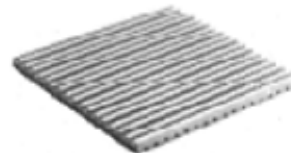
Equipment Type	Shaft Power, kW and Other	Rpm	Equipment Location											
			Slab on Grade			Up to 6 m Floor Span			6- to 9 m Floor Span			9- to 12 m Floor Span		
			Base Type	Iso- lator Type	Min. Defl., in.	Base Type	Iso- lator Type	Min. Defl., in.	Base Type	Iso- lator Type	Min. Defl., in.	Base Type	Iso- lator Type	Min. Defl., in.
<b>Refrigeration Machines and Chillers</b>														
Bare compressors	All	All	A	2	0.25	C	3	0.75	C	3	1.75	C	4	2.50
Reciprocating	All	All	A	2	0.25	A	4	0.75	A	3	1.75	A	4	2.50
Centrifugal	All	All	A	1	0.25	A	4	0.75	A	3	1.75	A	3	1.75
Open centrifugal	All	All	C	1	0.25	C	4	0.75	C	3	1.75	C	3	1.75
Absorption	All	All	A	1	0.25	A	4	0.75	A	3	1.75	A	3	1.75

## Base Types:

- A. No base, isolators attached directly to equipment
- B. Structural steel rails or base
- C. Concrete inertia base
- D. Curb-mounted base

## Isolator Types:

- 1. Pad, rubber, or glass fiber
- 2. Rubber floor isolator or hanger
- 3. Spring floor isolator or hanger
- 4. Restrained spring isolator
- 5. Thrust restraint



Type 1 Rubber Pad



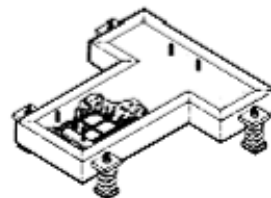
Type 2 Rubber Mount



Type 3 Spring Isolator



Type 4 Restrained  
Spring Isolator



CONCRETE BASES (Type C)

# Selection Guide for Vibration Isolator



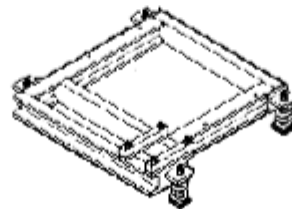
Equipment Type	Shaft Power, kW and Other	Rpm	Equipment Location											
			Slab on Grade			Up to 6 m Floor Span			6- to 9 m Floor Span			9- to 12 m Floor Span		
			Base Type	Iso- lator Type	Min. Defl., in.	Base Type	Iso- lator Type	Min. Defl., in.	Base Type	Iso- lator Type	Min. Defl., in.	Base Type	Iso- lator Type	Min. Defl., in.
Cooling Towers	All	Up to 300	A	1	0.25	A	4	3.50	A	4	3.50	A	4	3.50
		301 to 500	A	1	0.25	A	4	2.50	A	4	2.50	A	4	2.50
		500 and over	A	1	0.25	A	4	0.75	A	4	0.75	A	4	1.75
Boilers—Fire-tube	All	All	A	1	0.25	B	4	0.75	B	4	1.75	B	4	2.50

## Base Types:

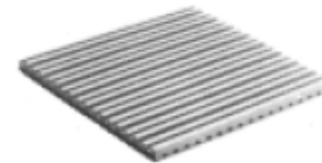
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- D. Curb-mounted base

## Isolator Types:

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- 4. Restrained spring isolator
- 5. Thrust restraint



STRUCTURAL BASES (Type B)



Type 1 Rubber Pad



Type 4 Restrained  
Spring Isolator



# Selection Guide for Vibration Isolator

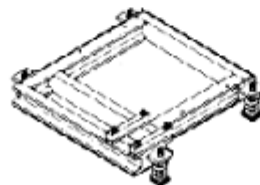
Equipment Type	Shaft Power, kW and Other	Rpm	Equipment Location																	
			Slab on Grade			Up to 6 m Floor Span			6- to 9 m Floor Span			9- to 12 m Floor Span								
			Base Type	Iso-lator Type	Min. Defl., in.	Base Type	Iso-lator Type	Min. Defl., in.	Base Type	Iso-lator Type	Min. Defl., in.	Base Type	Iso-lator Type	Min. Defl., in.						
<b>Pumps</b>																				
Closed coupled	Up to 5.6	All	B	2	0.25	C	3	0.75	C	3	0.75	C	3	0.75	C	3	1.75	C	3	1.75
	7.5 and over	All	C	3	0.75	C	3	0.75	C	3	0.75	C	3	1.75	C	3	1.75	C	3	1.75
Large inline	3.7 to 19	All	A	3	0.75	A	3	1.75	A	3	1.75	A	3	1.75	A	3	1.75	A	3	1.75
	22 and over	All	A	3	1.75	A	3	1.75	A	3	1.75	A	3	1.75	A	3	2.50	A	3	2.50
End suction and split case	Up to 30	All	C	3	0.75	C	3	0.75	C	3	0.75	C	3	1.75	C	3	1.75	C	3	1.75
	37 to 93	All	C	3	0.75	C	3	0.75	C	3	0.75	C	3	1.75	C	3	1.75	C	3	2.50
	110 and over	All	C	3	0.75	C	3	1.75	C	3	1.75	C	3	1.75	C	3	1.75	C	3	2.50

## Base Types:

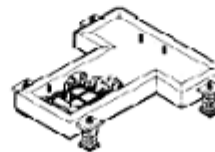
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## Isolator Types:

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- 4. Restrained spring isolator
- 5. Thrust restraint



STRUCTURAL BASES (Type B)



CONCRETE BASES (Type C)



Type 2 Rubber Mount



Type 3 Spring Isolator



# Selection Guide for Vibration Isolator

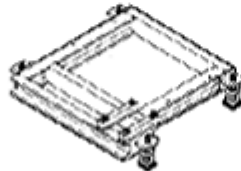
Equipment Type	Shaft Power, kW and Other	Rpm	Equipment Location											
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			Base Type	Iso-lator Type	Min. Defl., in.	Base Type	Iso-lator Type	Min. Defl., in.	Base Type	Iso-lator Type	Min. Defl., in.	Base Type	Iso-lator Type	Min. Defl., in.
<b>Axial Fans, Fan Heads, Cabinet Fans, and Fan Sections</b>														
Up to 560 mm dia.	All	All	A	2	0.25	A	3	0.75	A	3	0.75	C	3	0.75
610 mm dia. and over	Up to 500 Pa s.p.	Up to 300	B	3	2.50	C	3	3.50	C	3	3.50	C	3	3.50
		300 to 500	B	3	0.75	B	3	1.75	C	3	2.50	C	3	2.50
		501 and over	B	3	0.75	B	3	1.75	B	3	1.75	B	3	1.75
<b>Centrifugal Fans</b>														
Up to 560 mm dia.	All	All	B	2	0.25	B	3	0.75	B	3	0.75	C	3	1.75
610 mm dia. and over	Up to 30	Up to 300	B	3	2.50	B	3	3.50	B	3	3.50	B	3	3.50
		300 to 500	B	3	1.75	B	3	1.75	B	3	2.50	B	3	2.50
		501 and over	B	3	0.75	B	3	0.75	B	3	0.75	B	3	1.75

## Base Types:

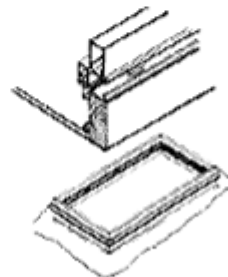
- A. No base, isolators attached directly to equipment
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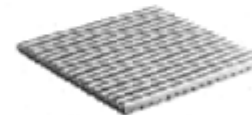
STRUCTURAL BASES (Type B)



CURB ISOLATION (Type D)



CONCRETE BASES (Type C)



Type 1 Rubber Pad



Type 3 Spring Isolator

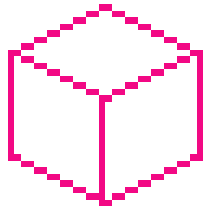


Type 2 Rubber Mount

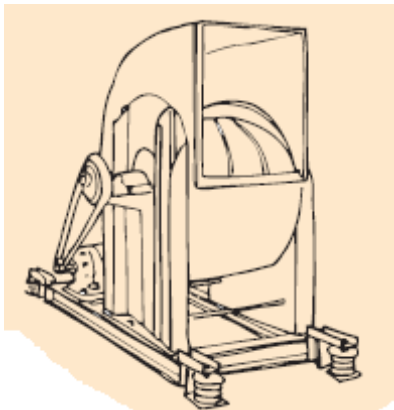


Type 4 Restrained Spring Isolator

# Vibration Control in Practice



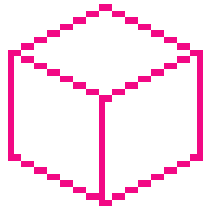
## Fans and Air-Handling Equipment



Fan with wheel diameter  $\leq 560$  mm and operate at speeds  $\leq 300$  rpm NOT generate large vibratory forces.

For fans operating under 300 rpm, select isolator deflection so that the isolator natural frequency is 40% or less of the fan speed ( for example, fan speed at 275 rpm, an isolator natural frequency of 110 rpm (1.8 Hz) or lower is required ( $0.4 \times 275 = 110$  rpm)).

# Vibration Control in Practice



## Pumps

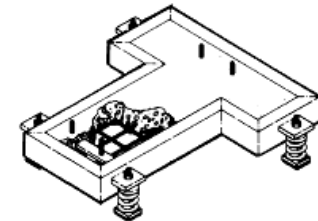
Concrete bases (Type C) should be designed for a thickness of one tenth the longest dimension with minimum thickness as follows:

For up to 20 kW, 150 mm;

For 30 to 55 kW, 200 mm;

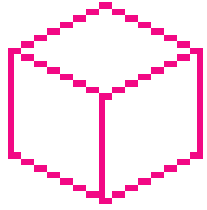
For 75 kW and higher, 300 mm.

Pumps **over 55 kW** and multistage pumps may exhibit excessive motion at start-up  
→ supplemental **restraining devices** can be installed if necessary.



CONCRETE BASES (Type C)

# Vibration Control in Practice



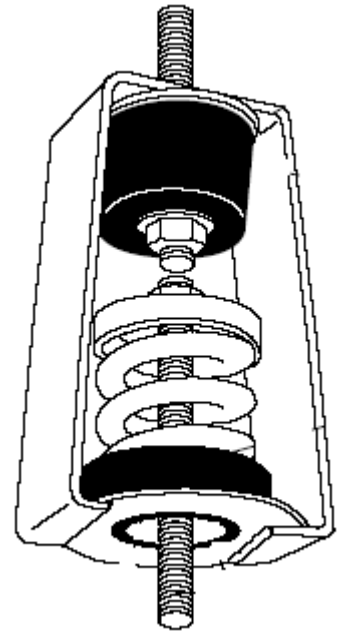
## Resilient Pipe Hangers and Supports

Resilient pipe hangers and supports are necessary to prevent vibration and noise transmission from the piping to the building structure and to provide flexibility in the piping.

Isolation hangers should be used for all piping in equipment rooms.

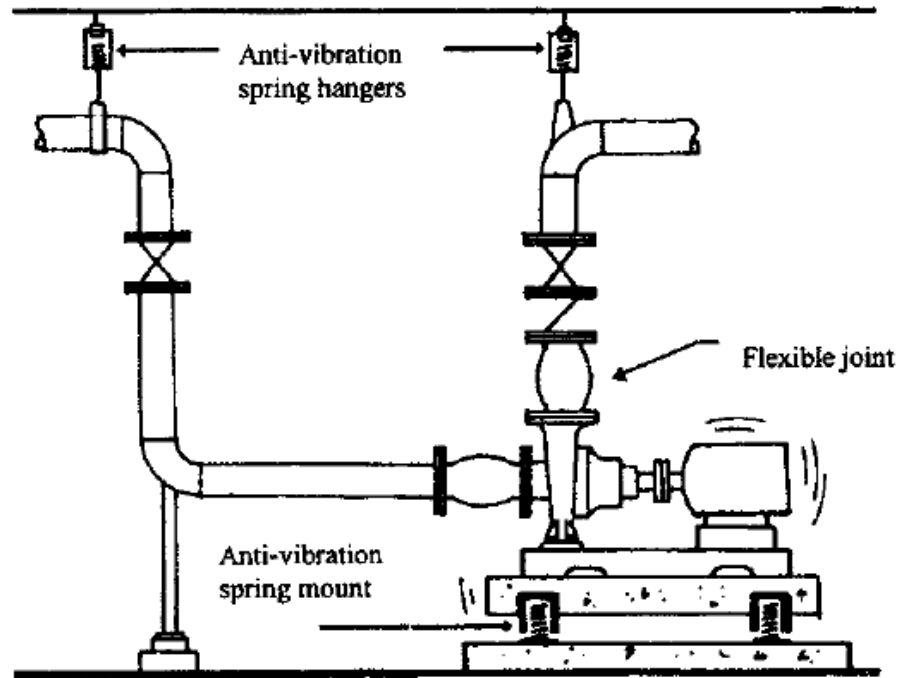
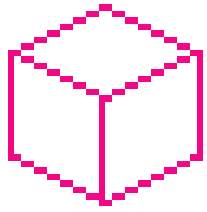
The first three hangers **from the equipment** : the same deflection as the equipment isolators (a max. limitation of 50 mm deflection)

**Remaining hangers** : spring or combination spring and rubber with 20 mm deflection.





# Vibration Control in Practice



**Vibration isolation for pumping system**



# Question and Answer