

## Advanced Psychrometry



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# Contents



- Introduction to Psychrometry
- Psychrometric Processes
- Psychrometric Software
- Psychrometric Analysis

# Introduction to Psychrometry



- Chapter 1 – Introduction to Psychrometry

<http://ibse.hk/MEBS7012/DencoCH1.pdf>

- Atmosphere and water vapour
- Psychrometric chart (theory)
- The psychrometric equation
- Psychrometric chart (CIBSE)
- Quick revision study guide (5 questions) & chapter notes
- Appendix - Thermodynamic Basics
  - Perfect gas laws
  - 1st law of thermodynamics
  - Conservation of energy

Study notes



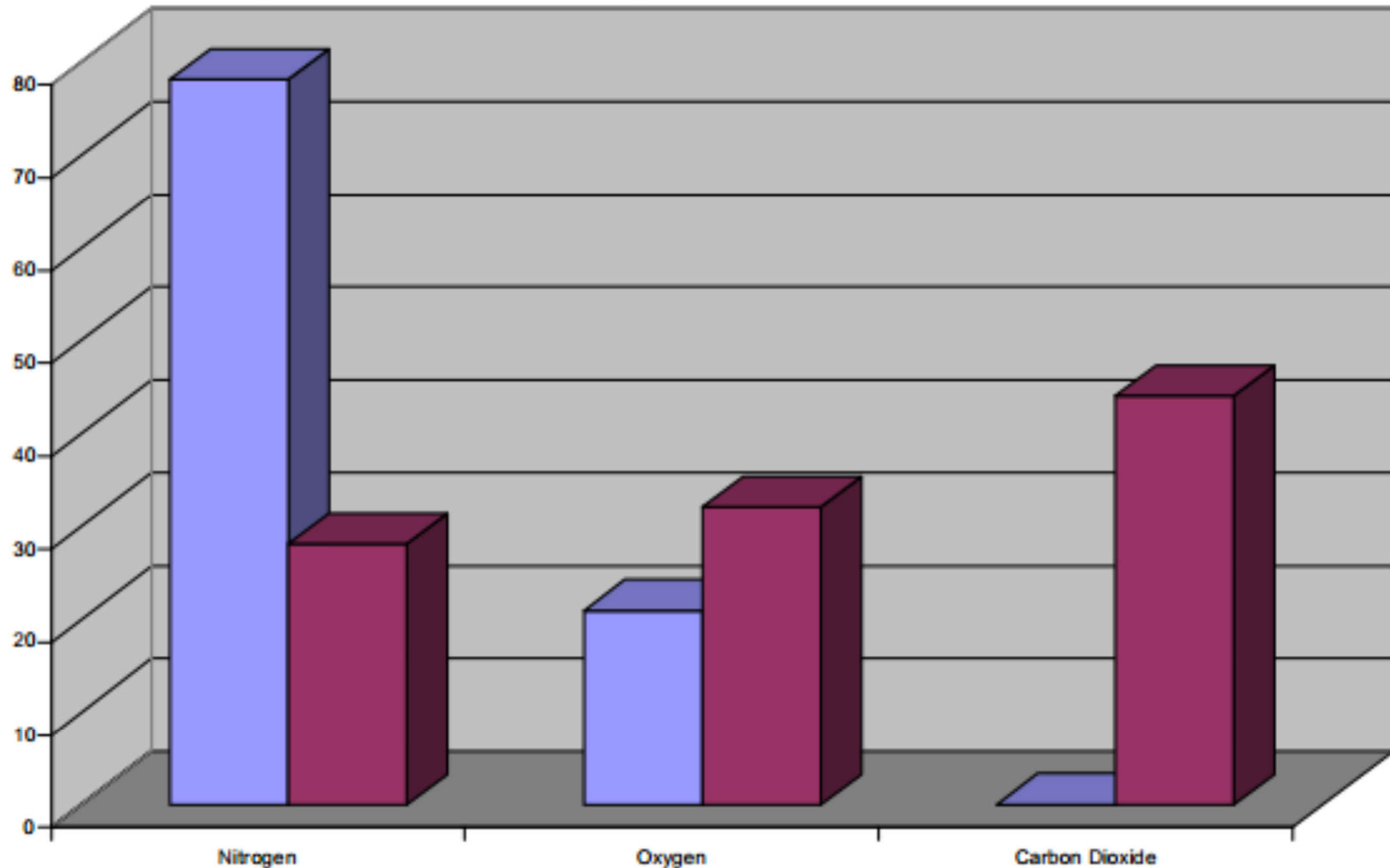
# Introduction to Psychrometry



- Psychrometry (測濕學)
  - The measurement or study of the thermodynamic properties of **moist air** (dry air + water vapour)
    - The Greek term psuchron (ψυχρόν) meaning "cold" and metron (μέτρον) meaning "means of measurement"
  - Moist air properties:
    - Ideal gas laws: Dalton's law of partial pressures
    - Standard atmospheric pressure = 101.325 kPa
    - Saturated vapour pressure: Max. pressure of water vapour that can occur at any given temperature

**Moist Air = Dry Air + Water Vapour (the gas phase of H<sub>2</sub>O)**

## Principle Dry Atmospheric Gases



**■ Molecular Weight**    **■ % Atmosphere**

# Introduction to Psychrometry



- Psychrometric chart (空氣濕度線圖)
  - A tool for understanding the relationships between the various parameters of supply air and the relative humidity
    - Can be used to assess the physical and thermodynamic properties of gas-vapour mixtures at a constant pressure
  - Learning to use psychrometric chart
    - Identify parts of the chart
    - Determine moist air properties
    - Use chart to analyse processes involving moist air

BAROMETRIC PRESSURE:

101.325 kPa

0 - 914 mt (0 - 3000 ft)

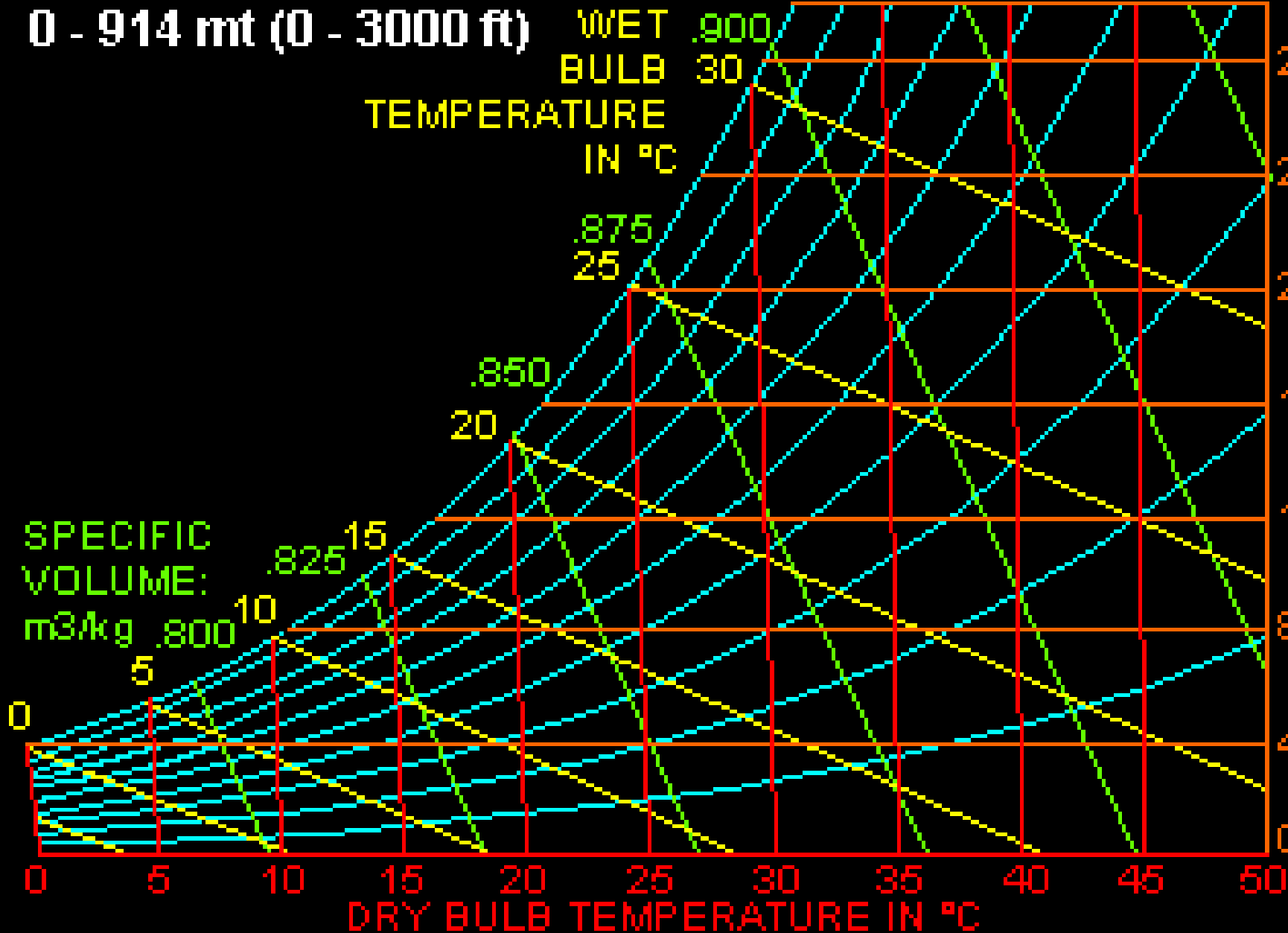
.925  
RELATIVE HUMIDITY

100% 80% 60% .950  
90% 70% 50% 40%

WET BULB TEMPERATURE IN °C  
.900  
30  
.875  
25  
.850  
20  
.825  
15  
.800  
10  
5  
0

SPECIFIC VOLUME:  
m³/kg  
.800  
0

ABSOLUTE HUMIDITY: g/kg  
28  
24  
20  
16  
12  
8  
4  
0  
30%  
20%  
10%



DRY BULB TEMPERATURE IN °C

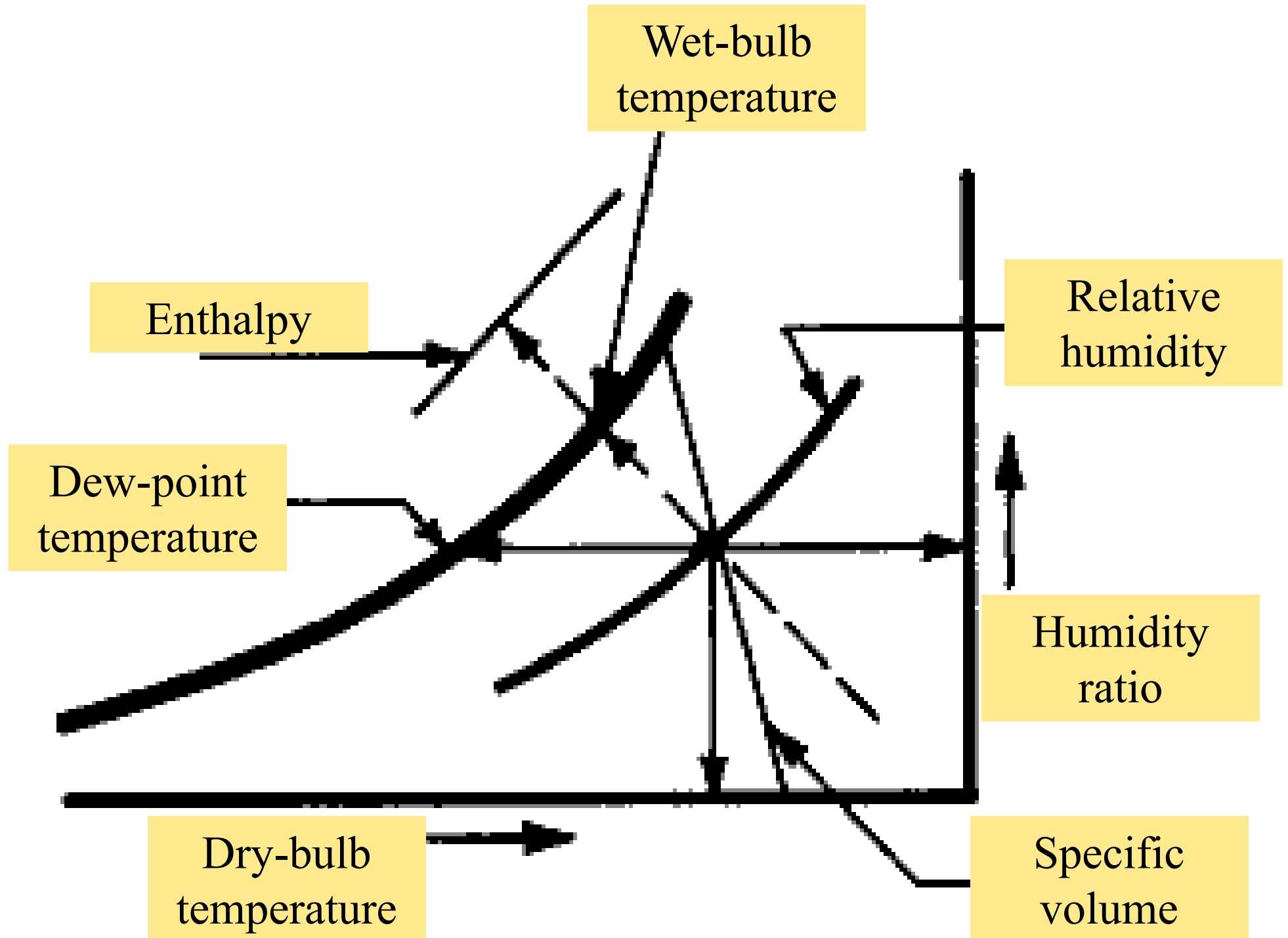
# Introduction to Psychrometry



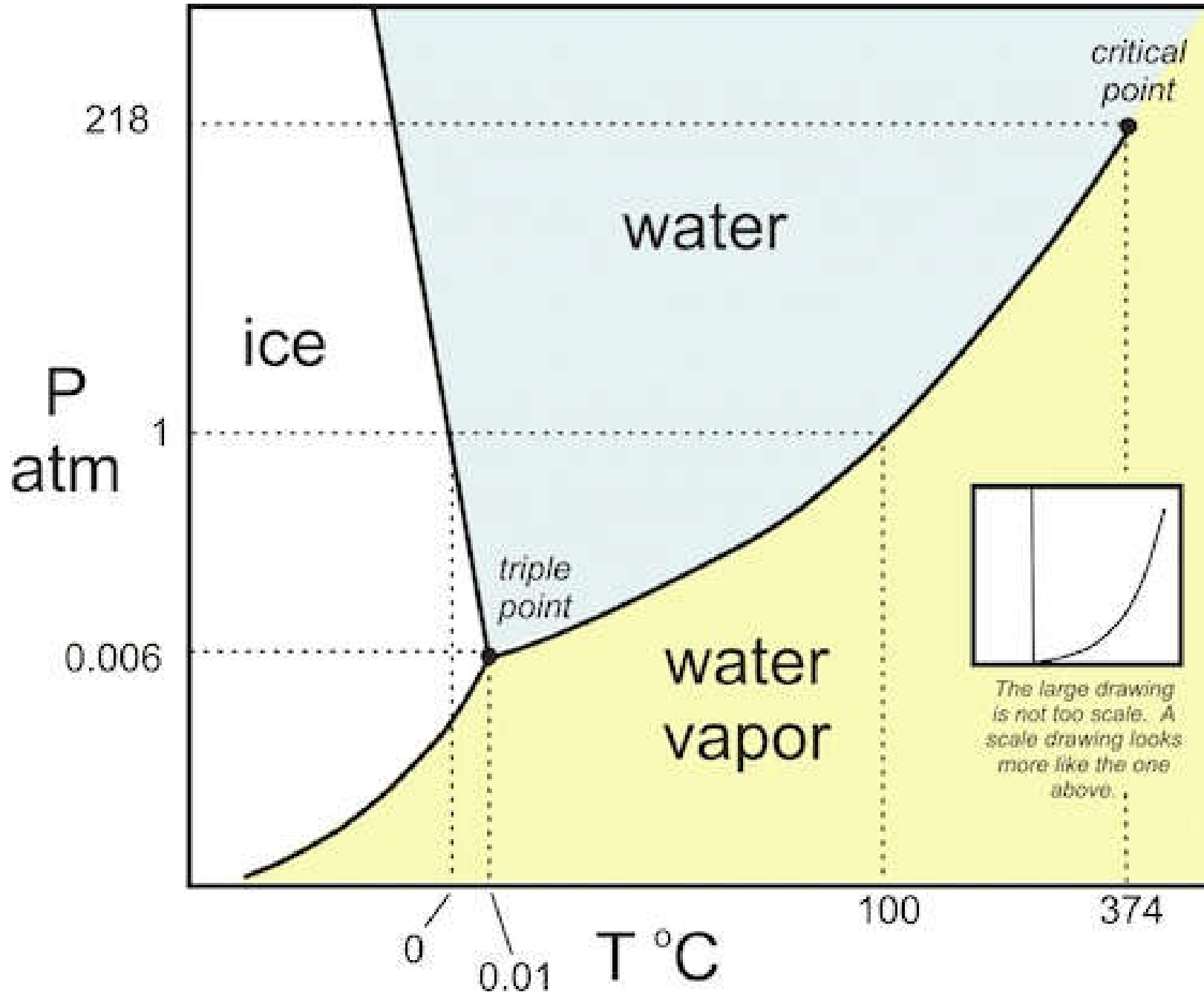
- Major parameters: (see handouts for details)
  - Moisture content ( $g$ ), or absolute humidity ( $w$ )
  - Relative humidity ( $rh$  or RH)
  - Percentage saturation ( $\mu$ )
  - Wet-bulb temperature ( $t_{wb}$ )
  - Dew-point temperature ( $t_{dp}$ )
  - Specific enthalpy ( $h$ )
  - Specific volume ( $v$ )
  - Density ( $\rho$ )



# Major parameters on a psychrometric chart

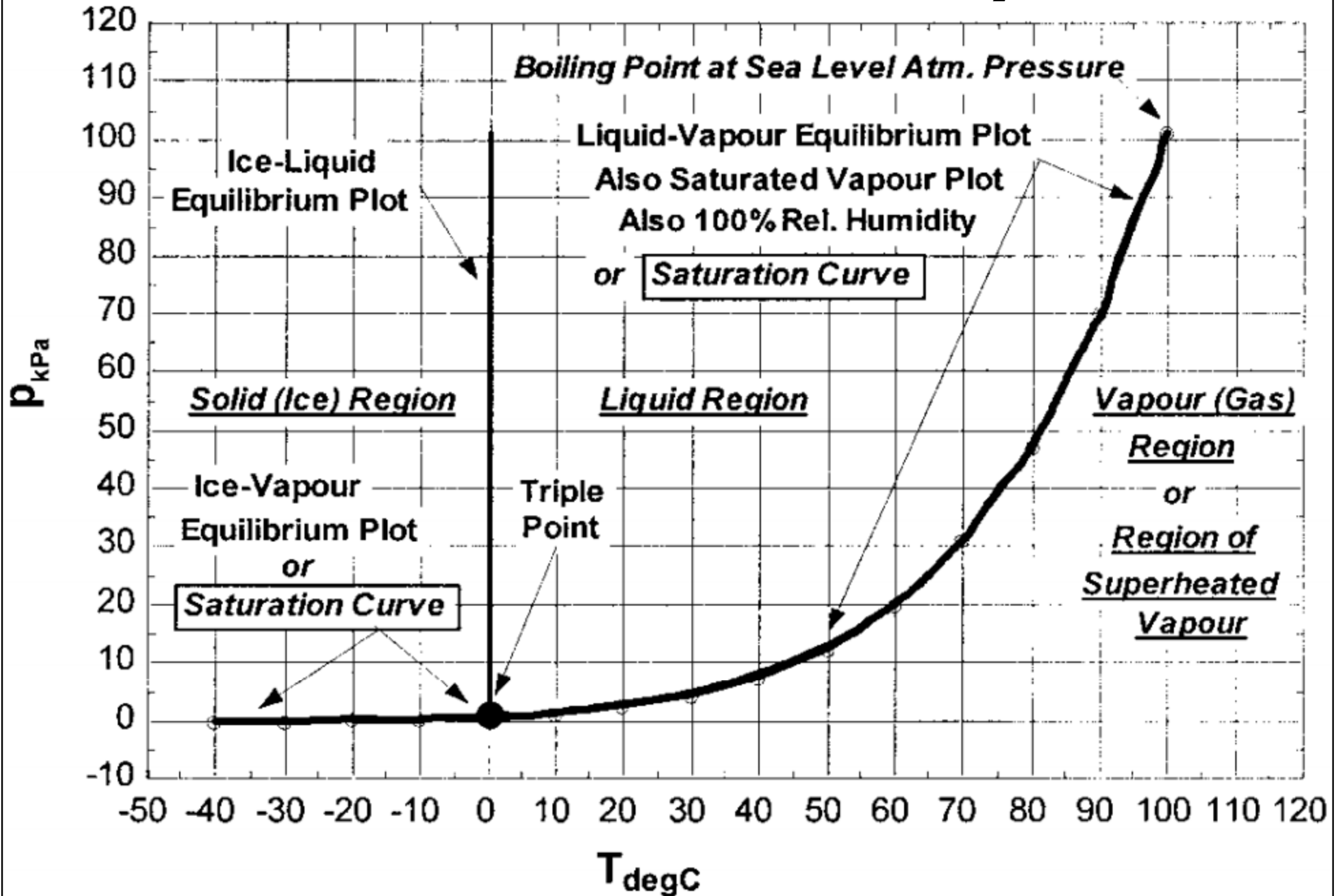


# From chemistry to psychrometrics (pressure-temperature diagram for water)

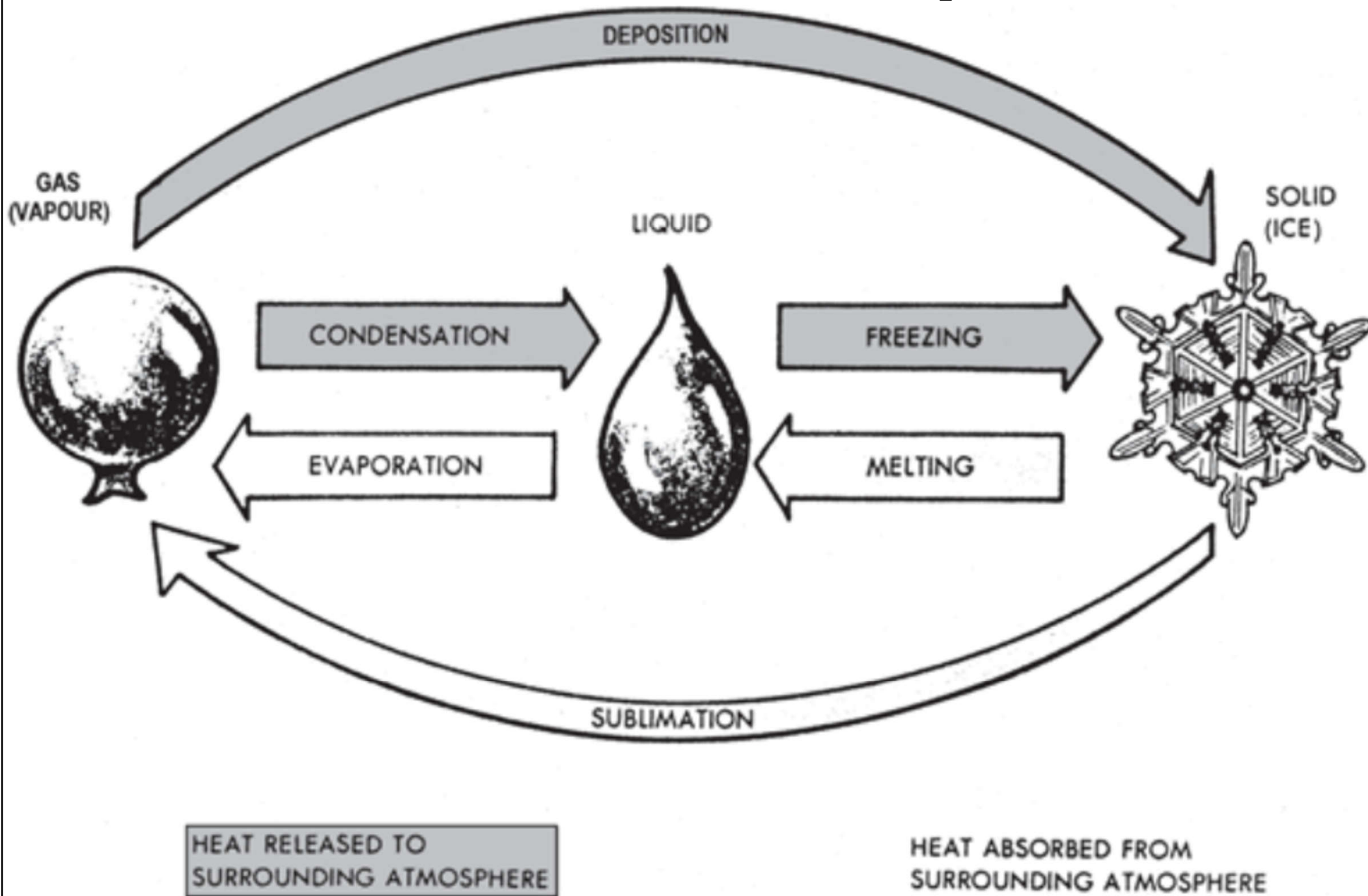


In psychrometrics, we care mainly about the yellow region (the boundary between the vapor phase and the liquid or solid phases)

# Pressure vs. temperature diagram for H<sub>2</sub>O



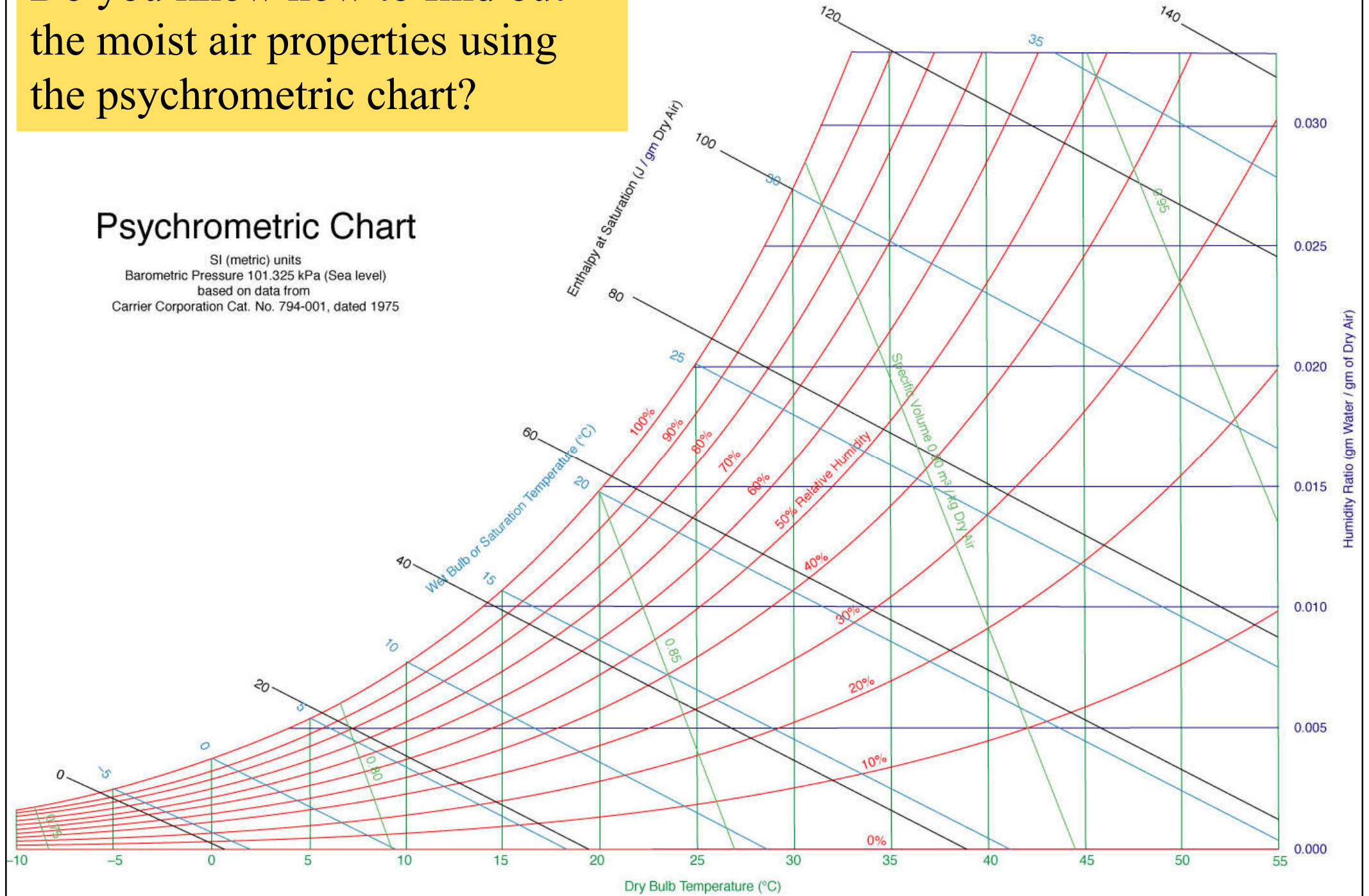
# Phase change processes for H<sub>2</sub>O



Do you know how to find out the moist air properties using the psychrometric chart?

## Psychrometric Chart

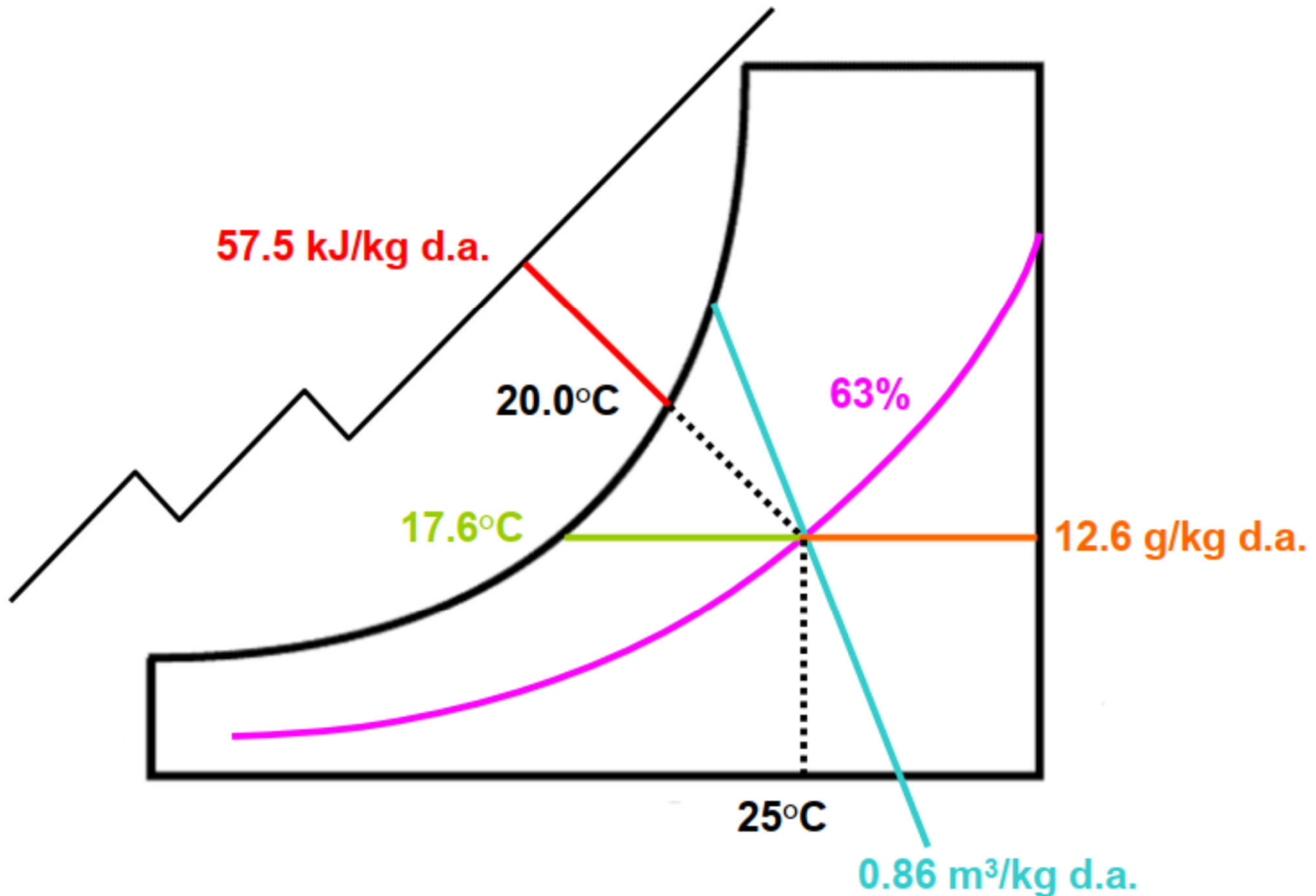
SI (metric) units  
Barometric Pressure 101.325 kPa (Sea level)  
based on data from  
Carrier Corporation Cat. No. 794-001, dated 1975



# Psychrometric chart: Example 1

Given: DBT = 25°C, WBT = 20°C

Find: (a) RH, (b) dew point temp., (c) humidity ratio, (d) specific volume, (e) enthalpy



# Measurement of moist air by sling psychrometer

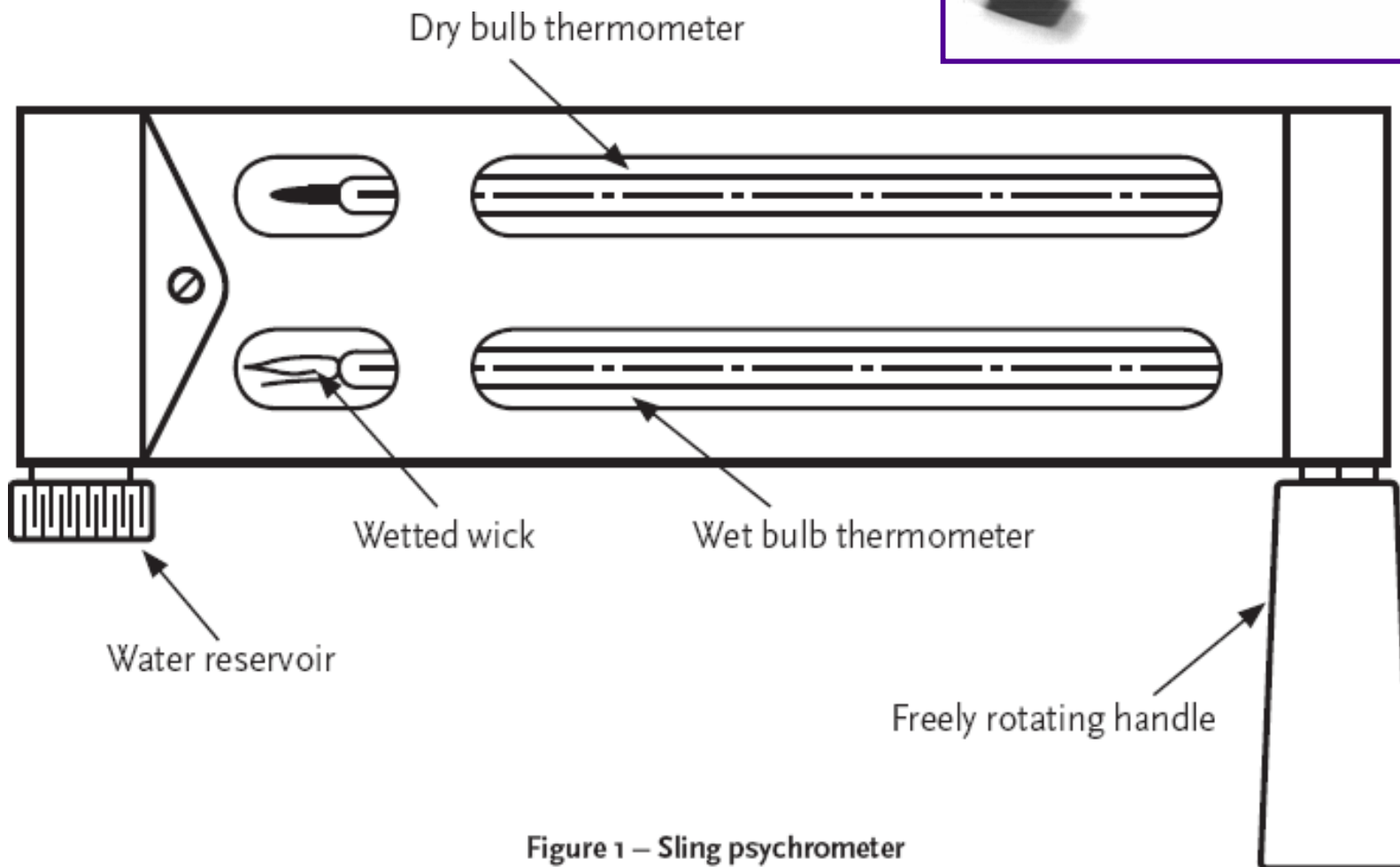


Figure 1 – Sling psychrometer

# Introduction to Psychrometry



- Commonly used psychrometric charts
  - ASHRAE psychrometric chart
  - CIBSE psychrometric chart
  - Carrier psychrometric chart
  - Trane psychrometric chart
  - Mr. S K Wang (similar to Trane)
  - Mollier chart in Mainland China (濕空氣焓濕圖)
- You should learn how to read and use the psychrometric charts for HVAC design





# ASHRAE PSYCHROMETRIC CHART NO.1

NORMAL TEMPERATURE

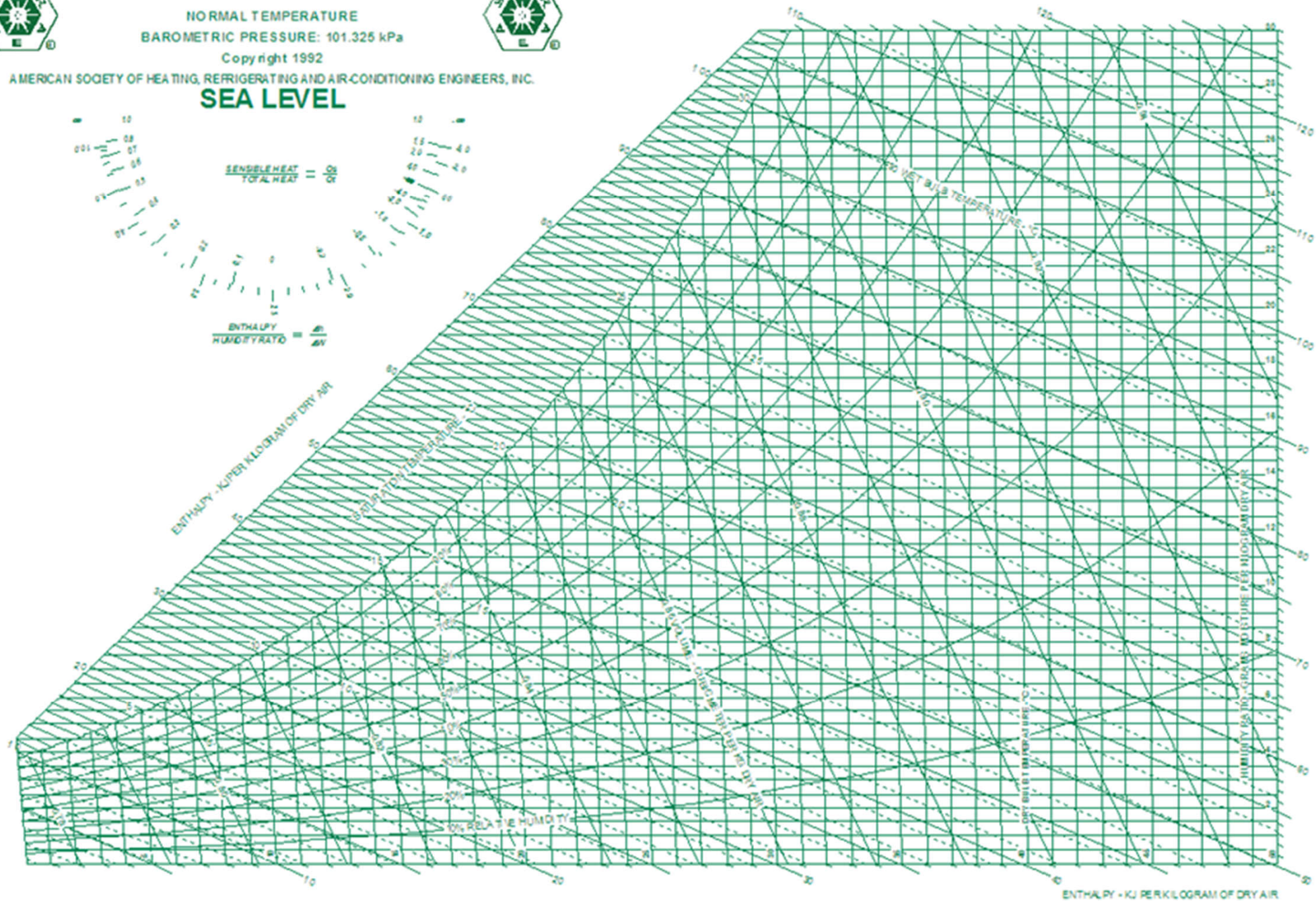
BAROMETRIC PRESSURE: 101.325 kPa

Copyright 1992

AMERICAN SOCIETY OF HEATING, REFRIGERATING AND AIR-CONDITIONING ENGINEERS, INC.



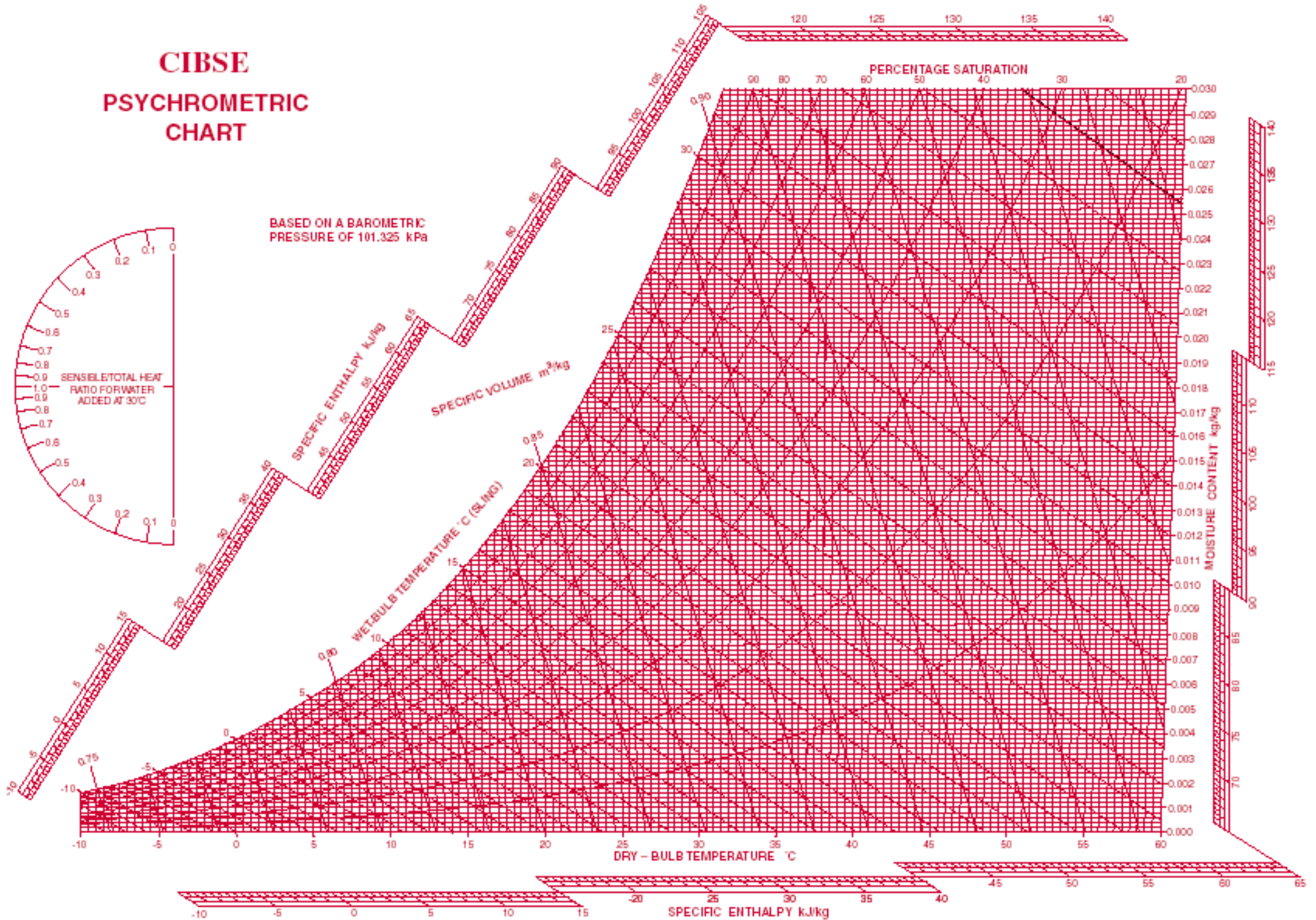
## SEA LEVEL



ENTHALPY - KJ PER KILOGRAM OF DRY AIR

# CIBSE PSYCHROMETRIC CHART

BASED ON A BAROMETRIC  
PRESSURE OF 101.325 kPa

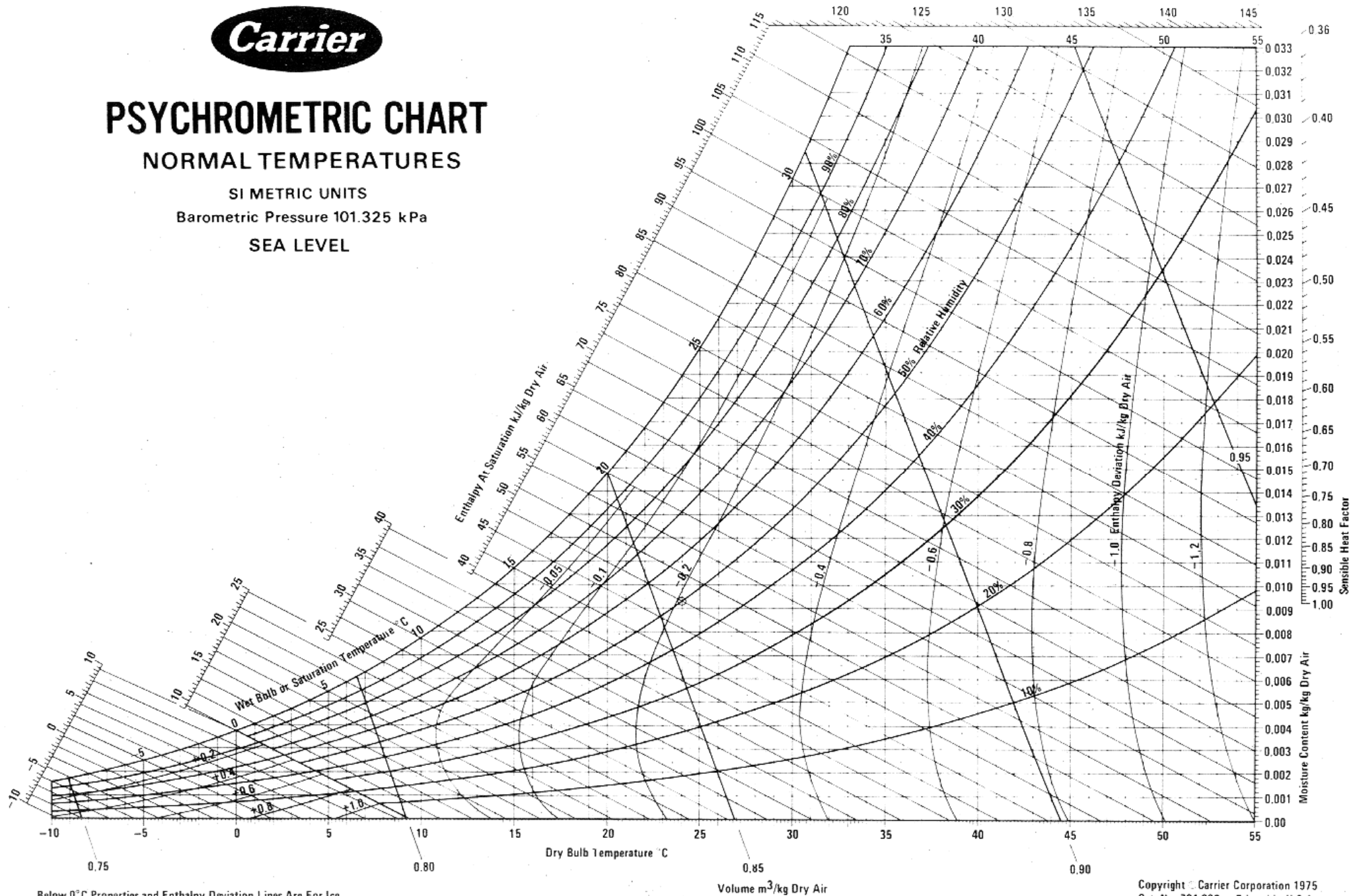




# PSYCHROMETRIC CHART

NORMAL TEMPERATURES

SI METRIC UNITS  
Barometric Pressure 101.325 kPa  
SEA LEVEL



Below 0°C Properties and Enthalpy Deviation Lines Are For Ice

Copyright © Carrier Corporation 1975  
Cat. No. 794-002 Printed in U.S.A.

Reproduced courtesy of Carrier Corporation

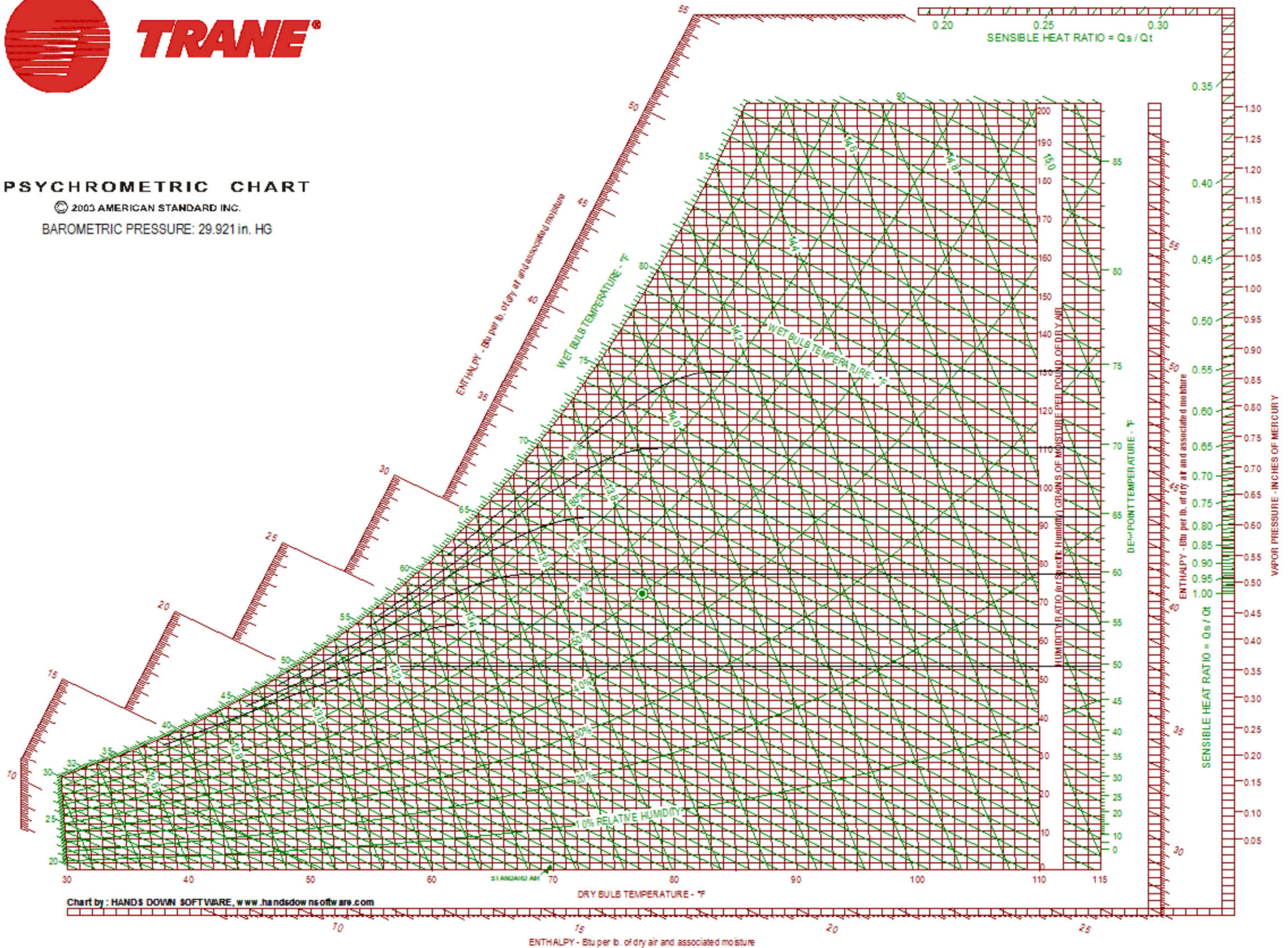


# TRANE®

## PSYCHROMETRIC CHART

© 2005 AMERICAN STANDARD INC.

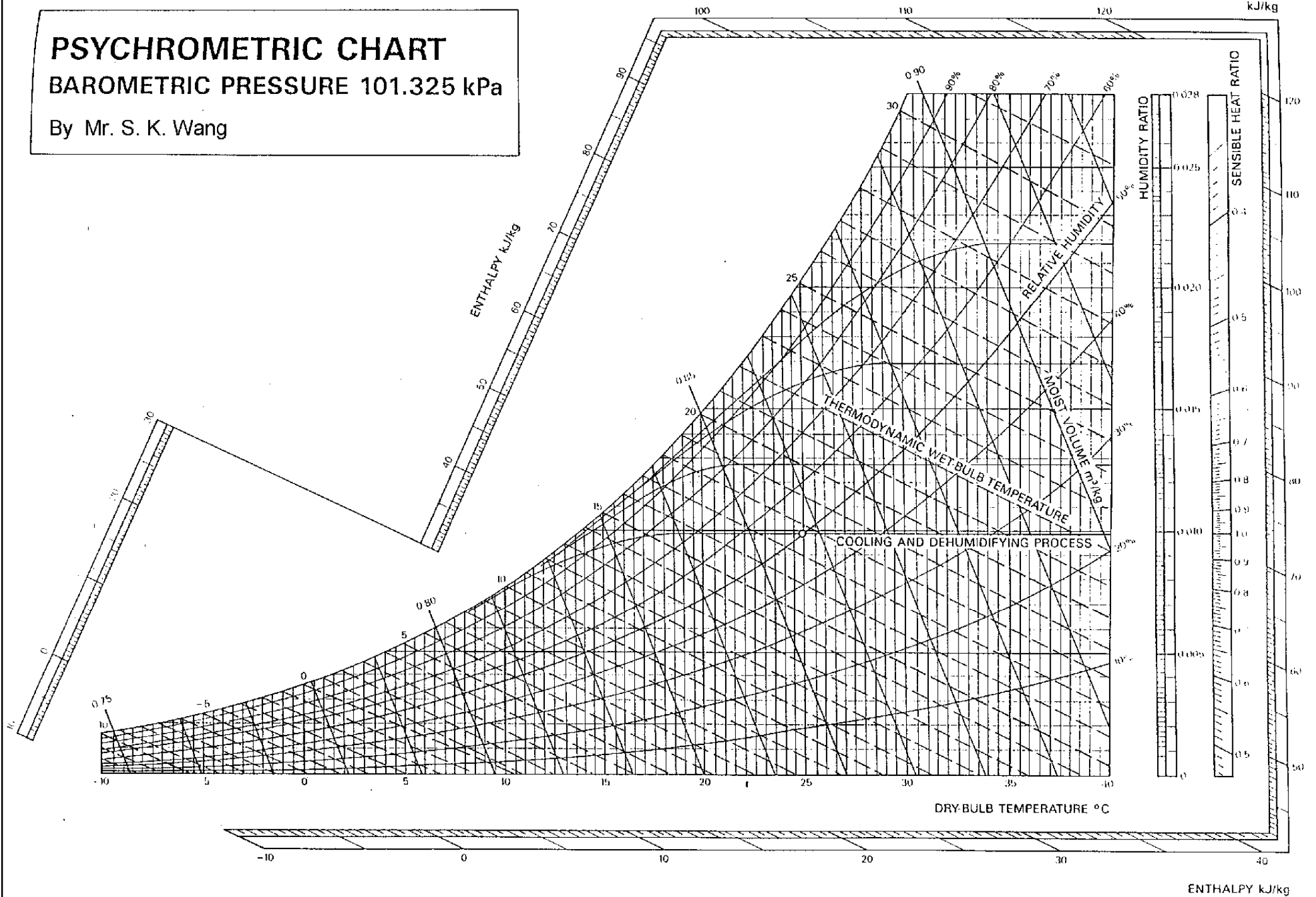
BAROMETRIC PRESSURE: 29.921 in. HG

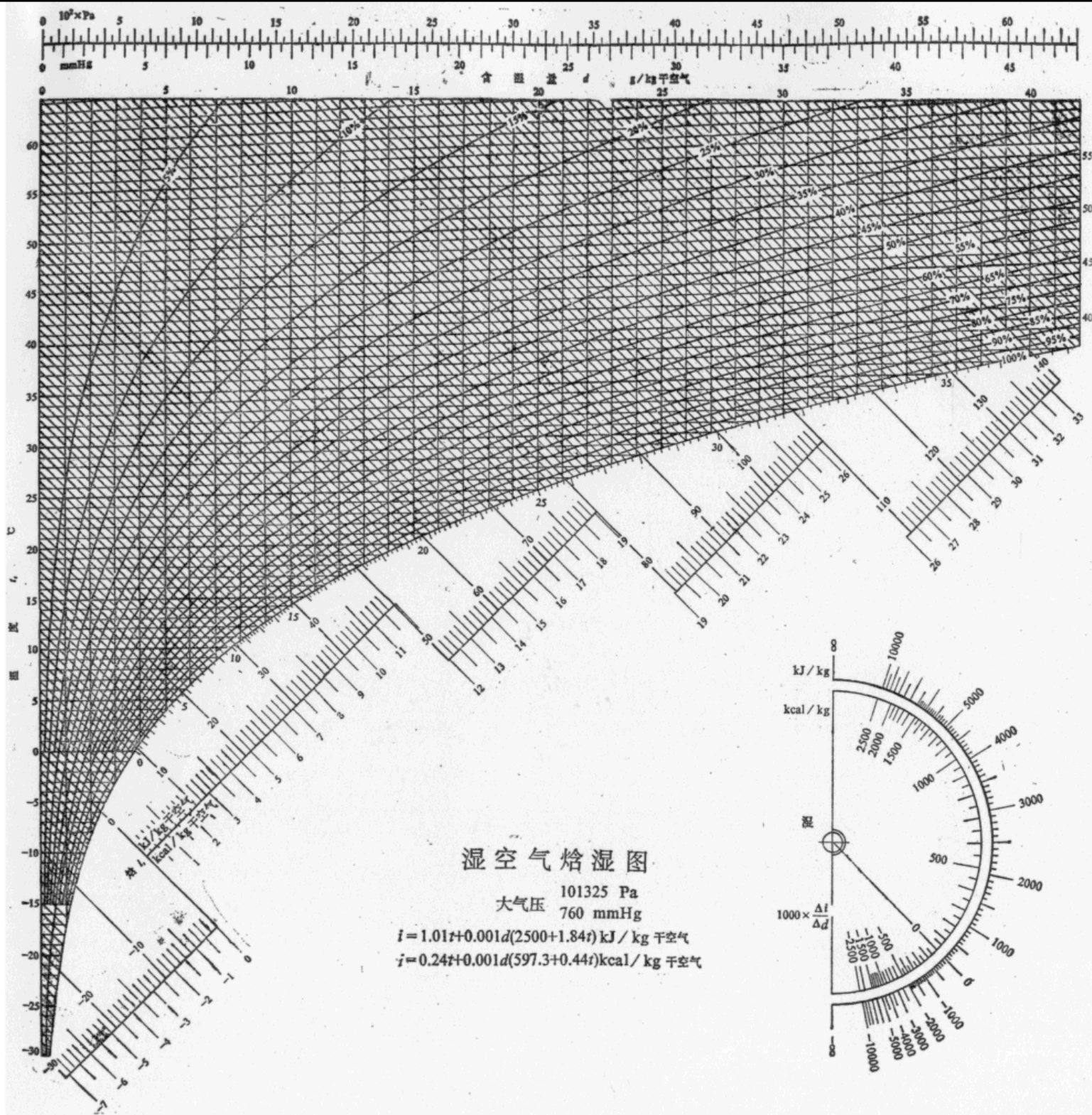


# PSYCHROMETRIC CHART

BAROMETRIC PRESSURE 101.325 kPa

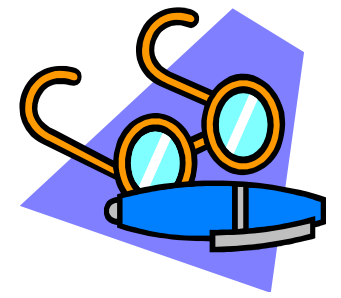
By Mr. S. K. Wang





Mollier  
chart style

# Psychrometric Processes

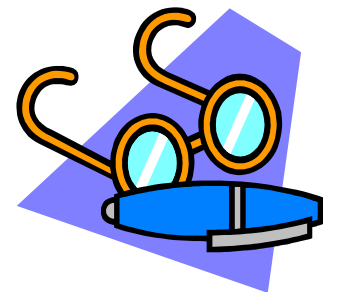


- Chapter 2 – Psychrometric Processes  
<http://ibse.hk/MEBS7012/DencoCH2.pdf>
  - Sensible heating coils
  - Cooling coils
  - Humidifiers
  - Water spray types
  - Steam humidifier
  - Humidifier – psychrometric process
  - Room psychrometric process
  - Mixing air streams
  - Quick revision study guide & chapter notes

Study notes



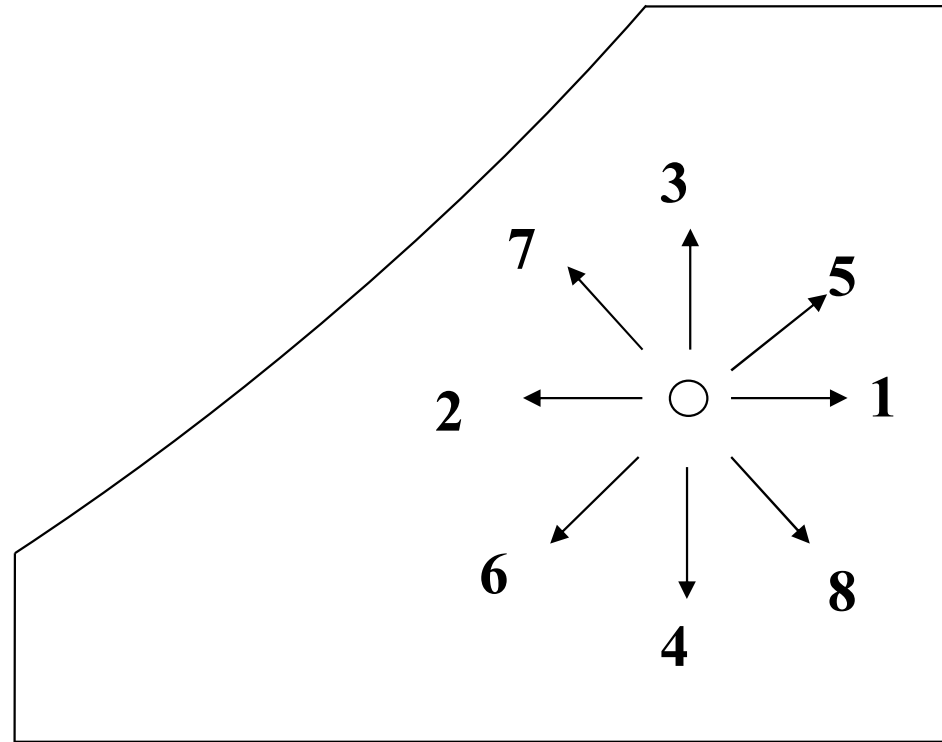
# Psychrometric Processes



- Common processes:
  - Sensible cooling / sensible heating
  - Cooling and dehumidification / heating and humidification
  - Humidification / dehumidification
  - Evaporative cooling / chemical dehydration
- Typical devices:
  - Cooling/heating coils
  - Humidifiers / dehumidifiers



# Basic psychrometric processes



Process 0-1: Sensible heating

Process 0-2: Sensible cooling

Process 0-3: Humidifying

Process 0-4: Dehumidifying

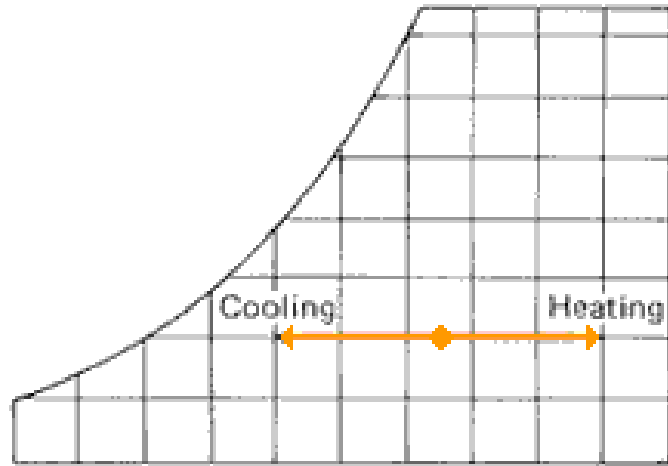
Process 0-5: Heating and humidifying

Process 0-6: Cooling and dehumidifying

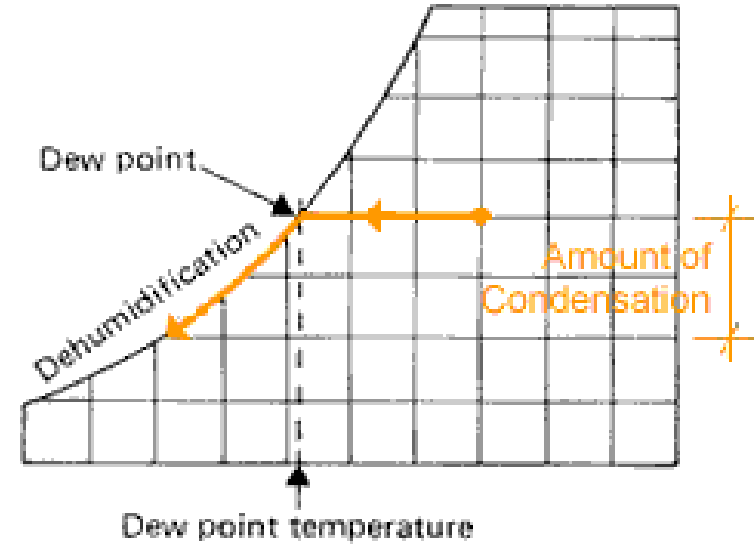
Process 0-7: Cooling and humidifying

Process 0-8: Heating and dehumidifying

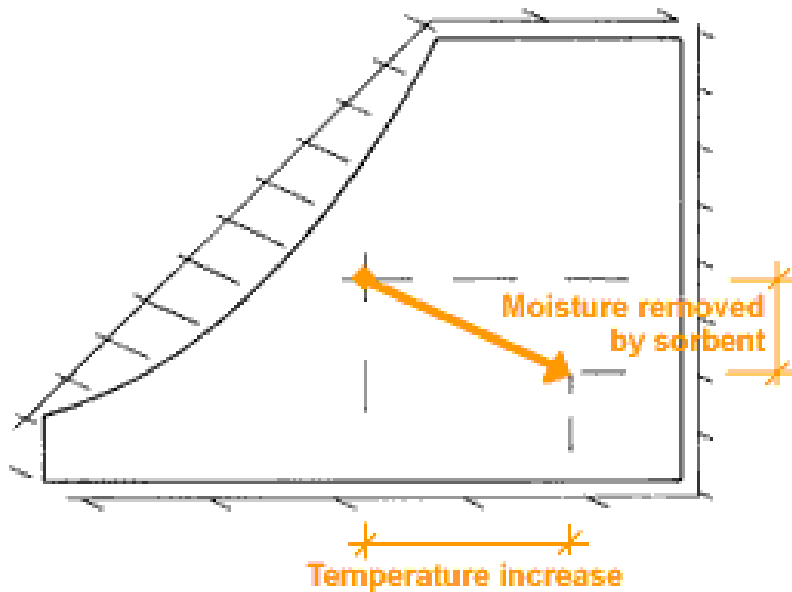
# Psychrometric processes



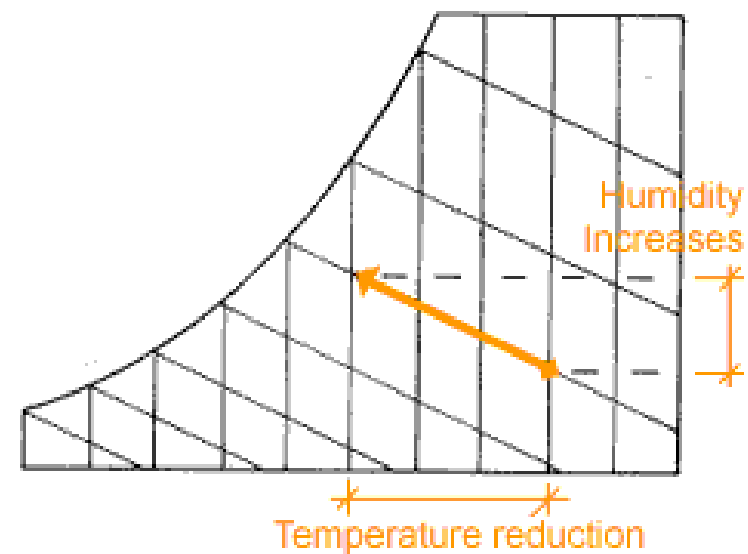
Sensible cooling/heating



Cooling and dehumidification

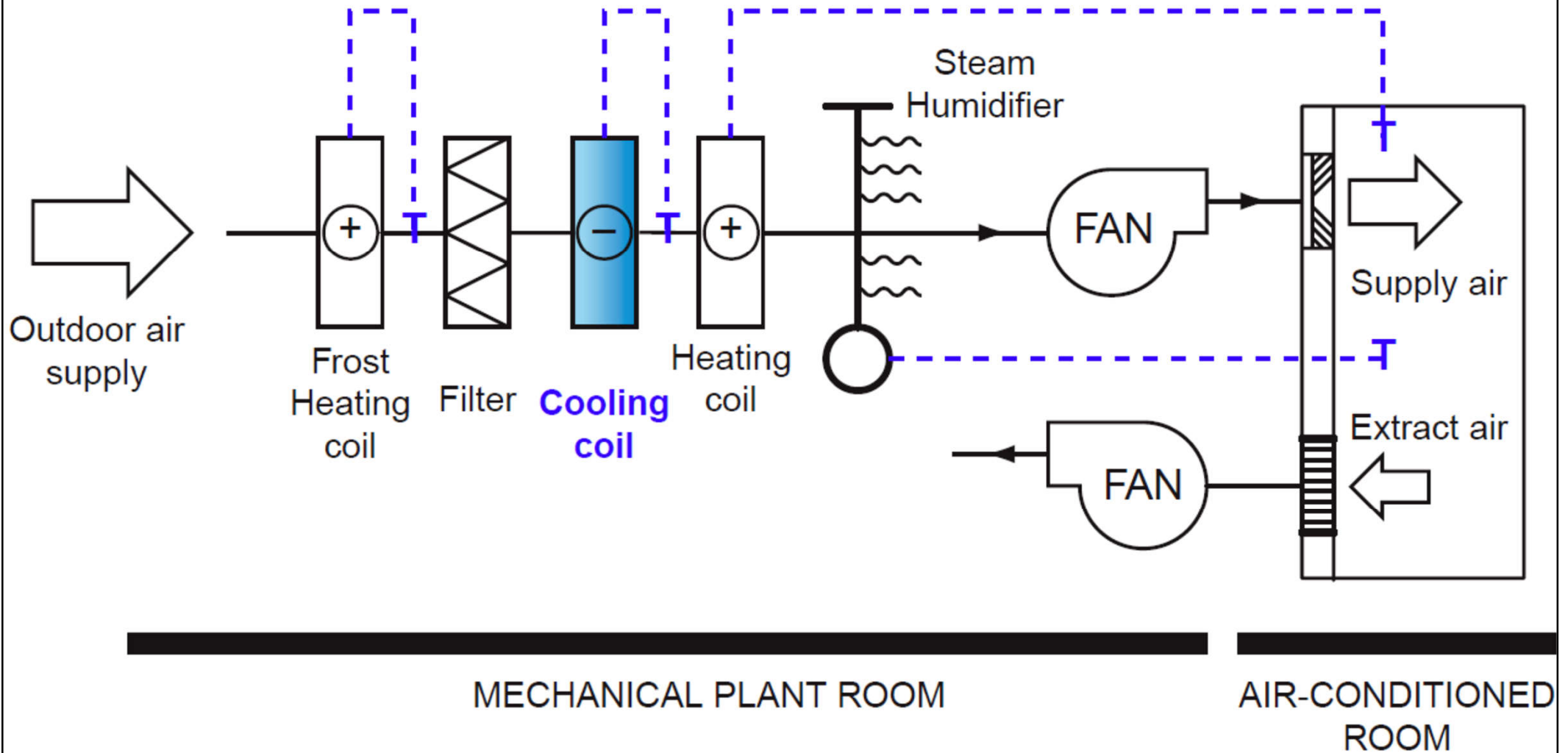


Adiabatic dehumidification



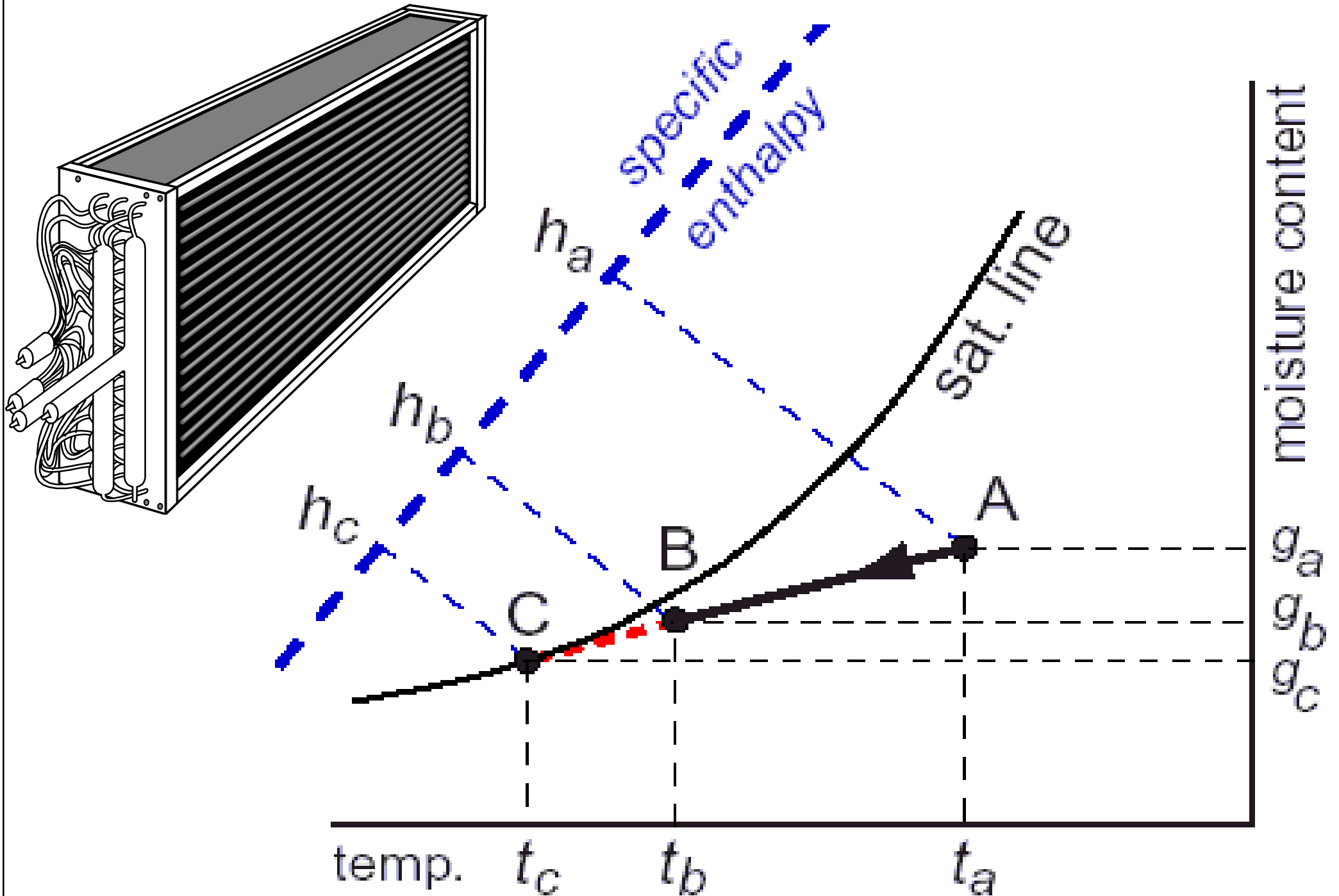
Evaporative cooling

# Schematic representation of all fresh-air, constant volume air conditioning system

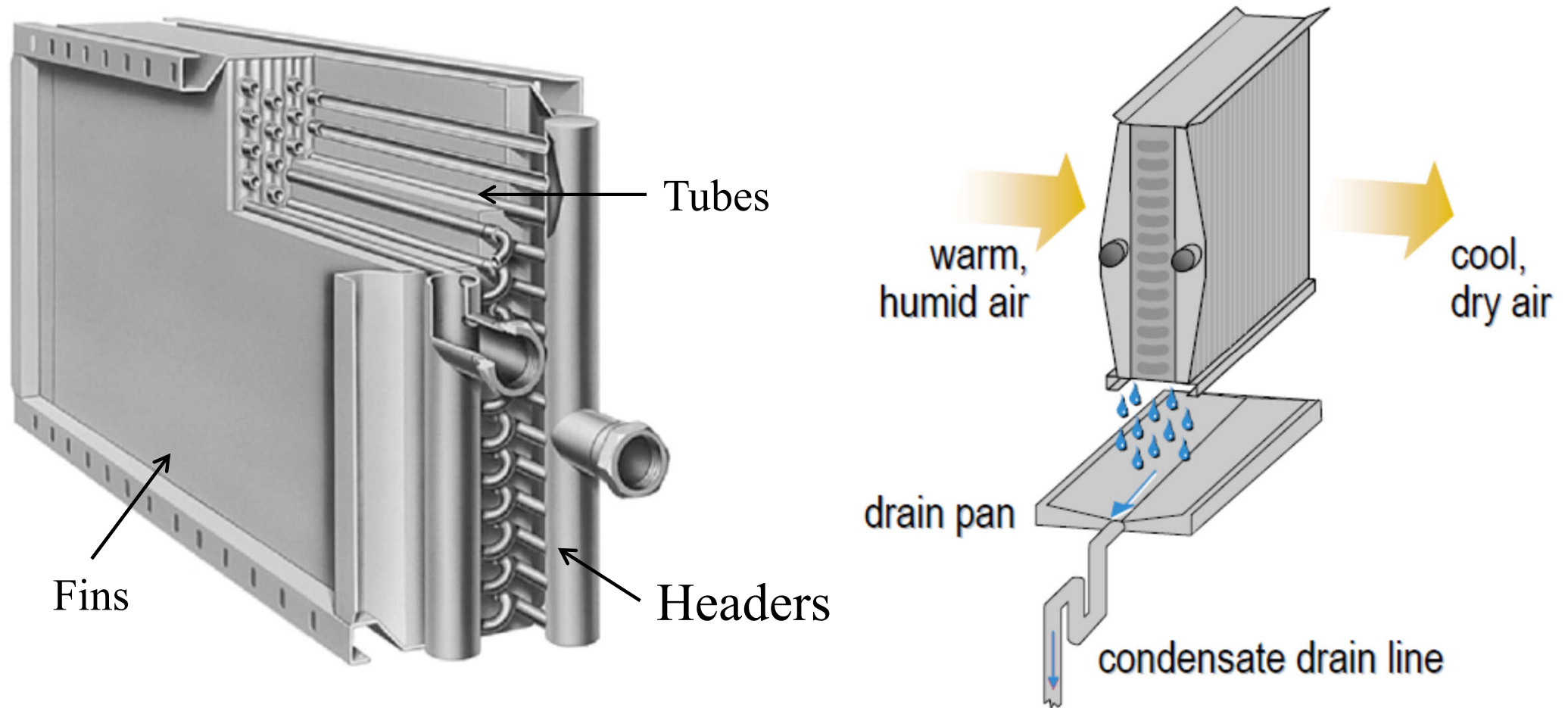


Can you explain the functions of each components?

# Cooling and dehumidification process at the cooling coil

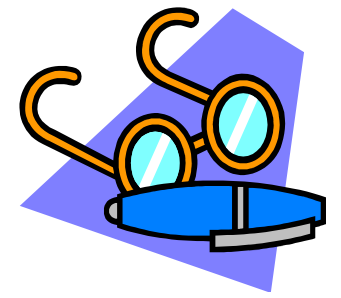


# Chilled water cooling coil (a heat exchanger)



Sensible heat exchange:  $q_S = m_a \times c_p \times (t_b - t_a)$

Latent heat exchange:  $q_L = m_a \times h_{fg}$



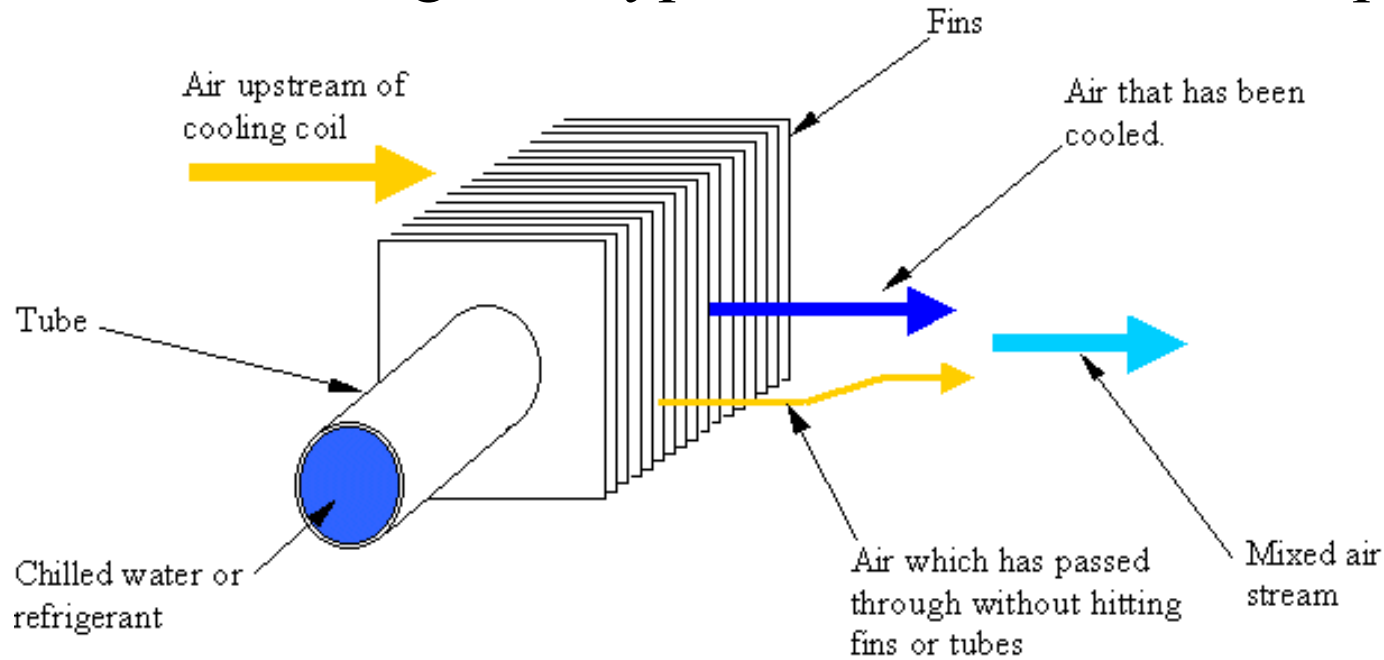
# Psychrometric Processes

- Specific enthalpy difference:  $q = m \times (h_a - h_b)$
- Sensible heat:  $q_S = m_a \times c_p \times (t_b - t_a)$
- Latent heat:  $q_L = m_a \times h_{fg}$
- Contact factor (cooling coil):

$$\beta = \frac{g_a - g_b}{g_a - g_c} = \frac{h_a - h_b}{h_a - h_c} = \frac{t_a - t_b}{t_a - t_c}$$

- Bypass factor = 1 – Contact factor

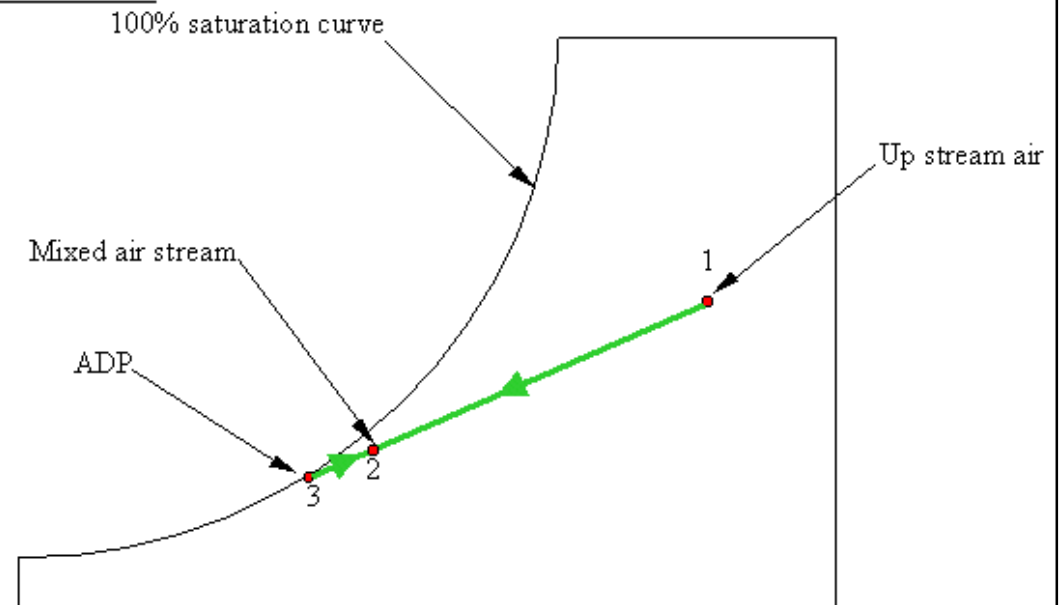
# Cooling coil bypass/contact factor and apparatus dew point



The percentage of air that passes through the coil unchanged is called the bypass factor.

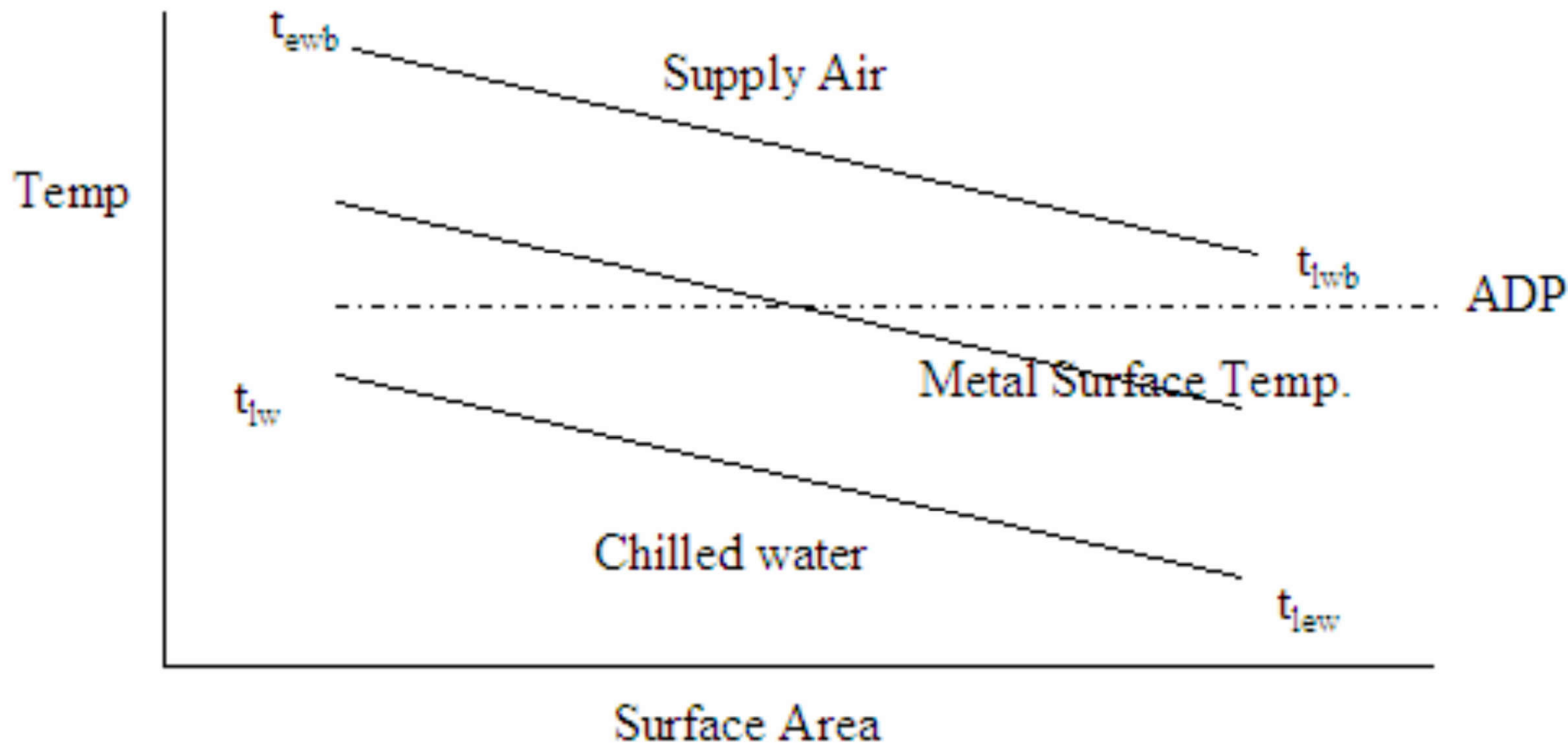
A SECTION OF COOLING COIL SHOWING AIR STREAMS

ADP = apparatus dew point  
It is the coil surface dew point temperature required to accomplish a cooling/dehumidifying process.



PSYCHROMETRIC CHART SHOWING COOLING COIL CONTACT FACTOR

# Relationship of apparatus dew point (ADP) to supply air and chilled water temperatures

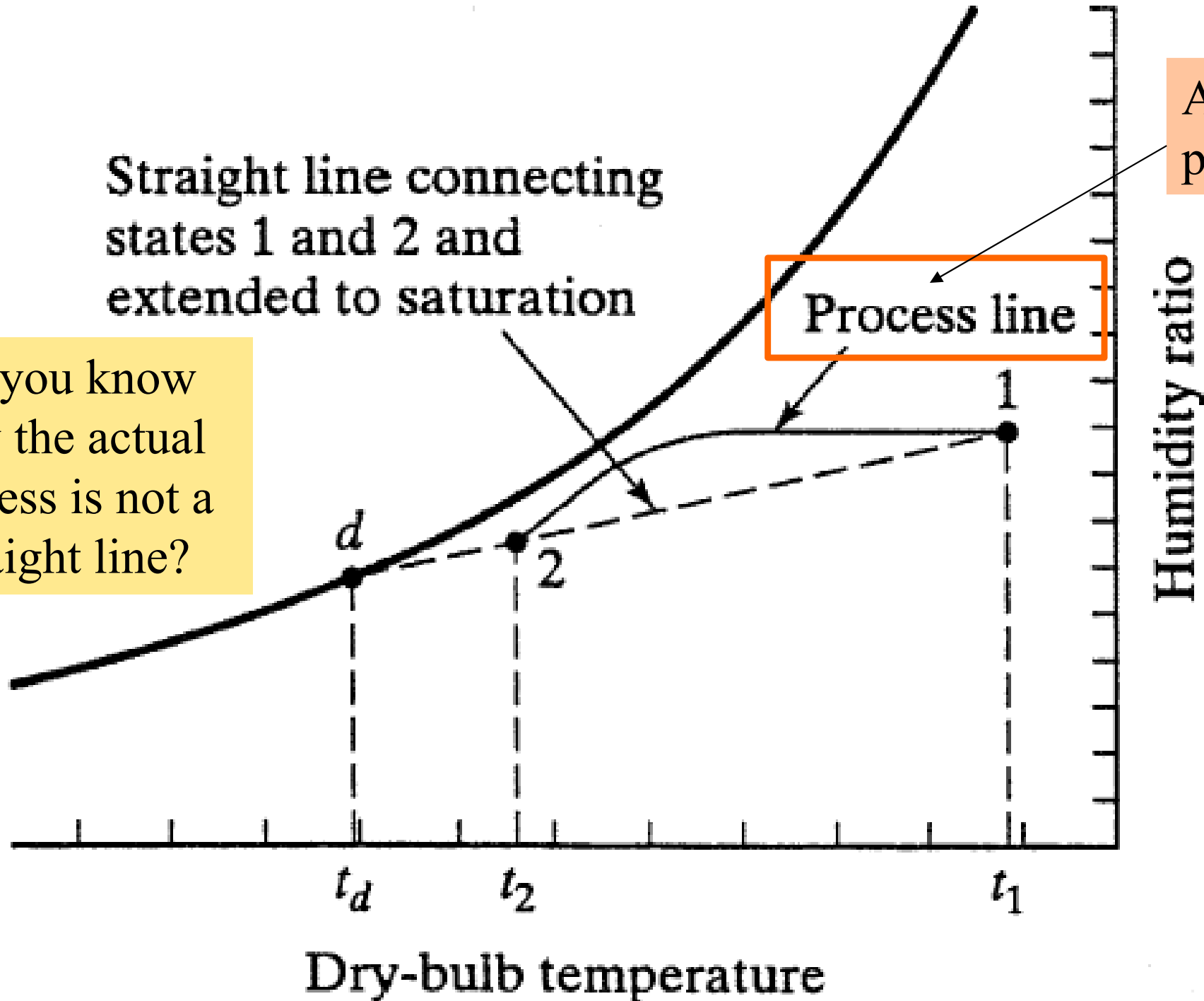




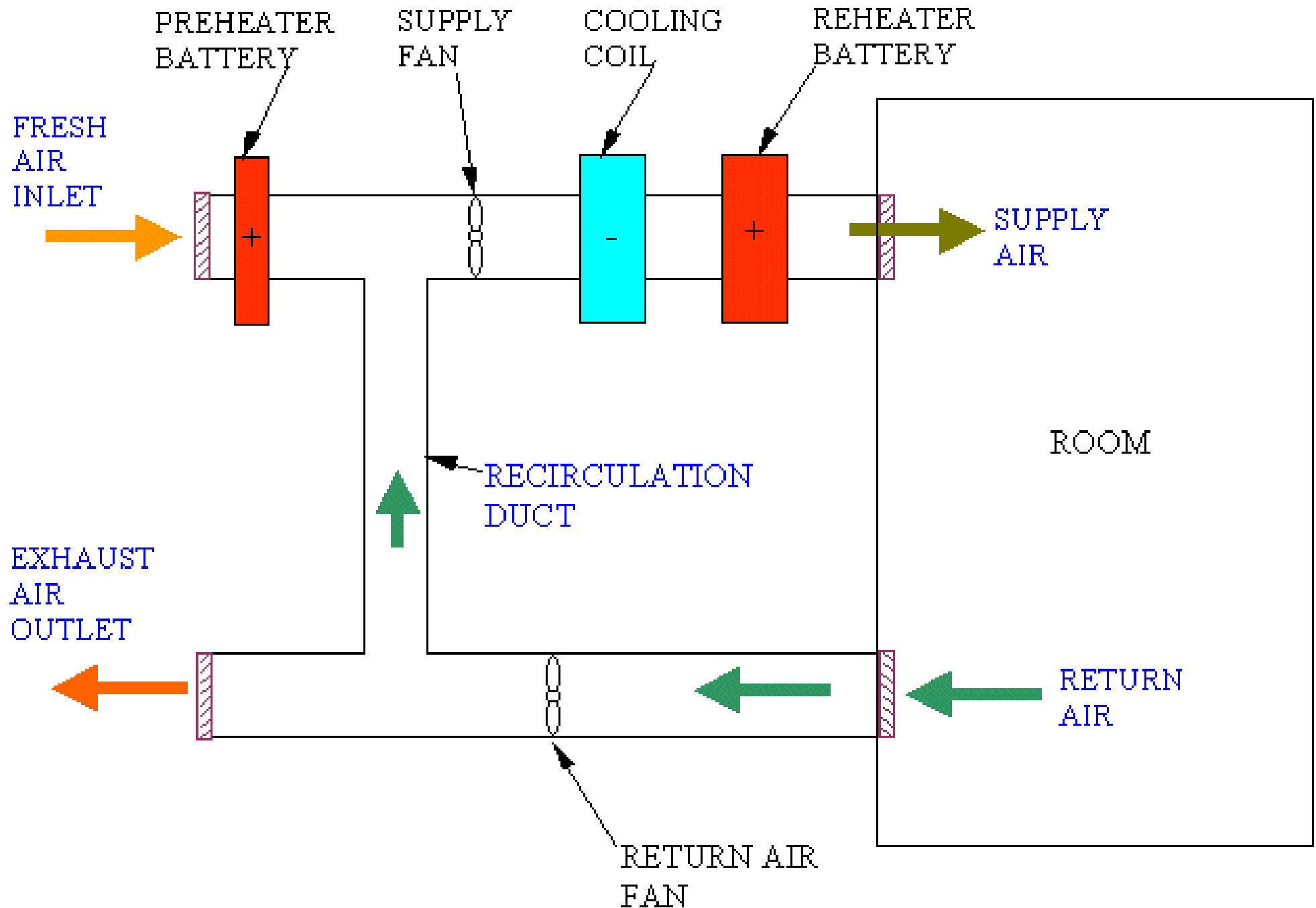
# Cooling and dehumidification process line

Straight line connecting states 1 and 2 and extended to saturation

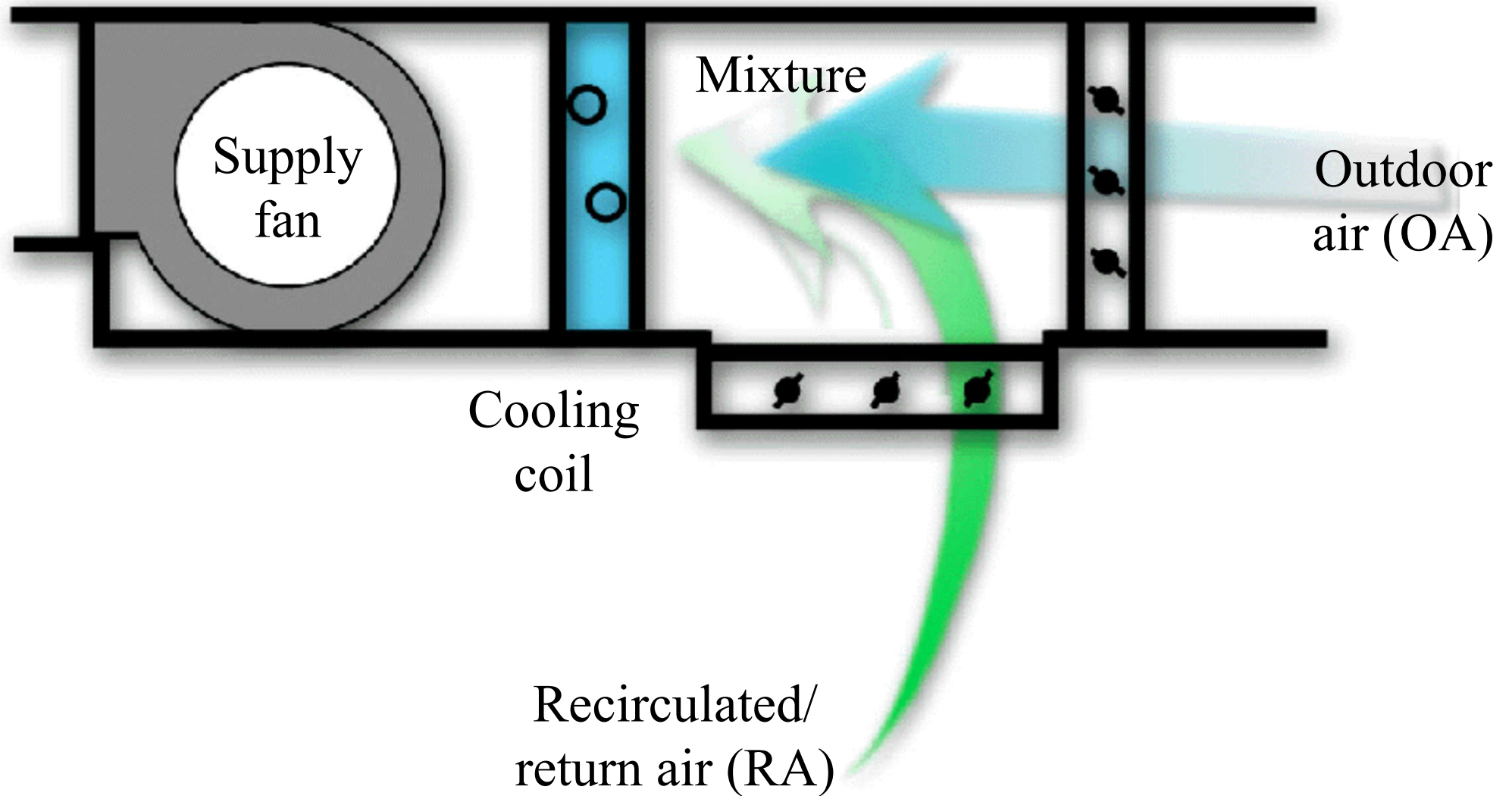
Do you know why the actual process is not a straight line?



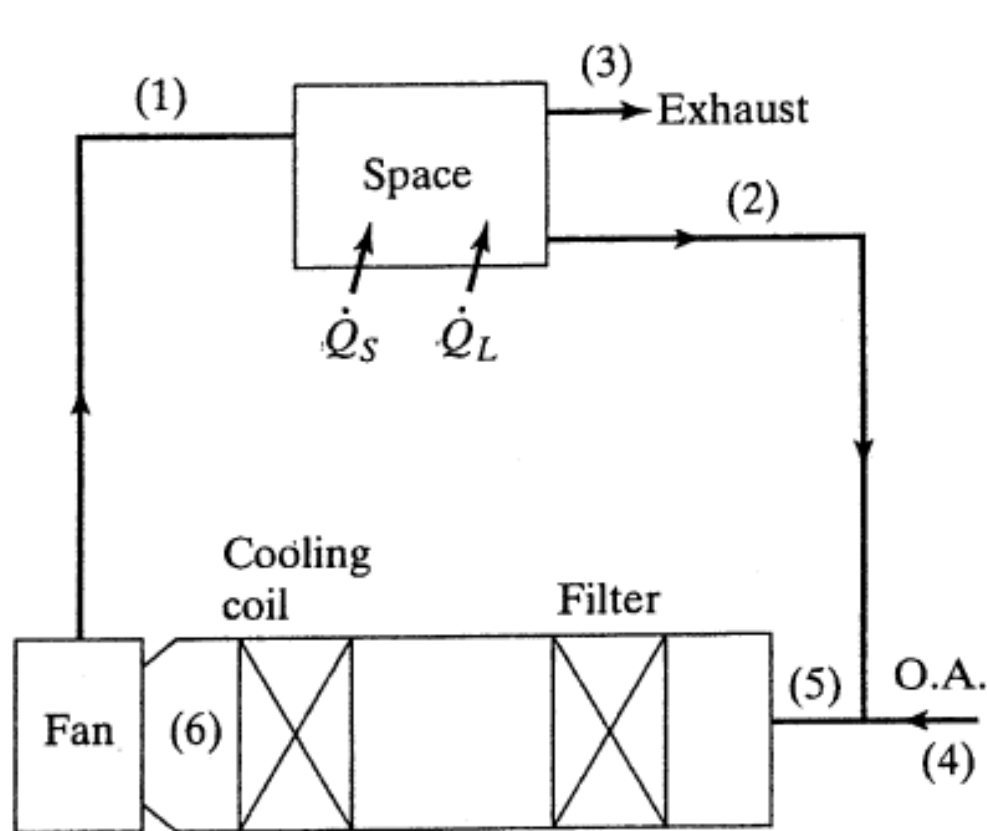
# Major components of the HVAC air-side system



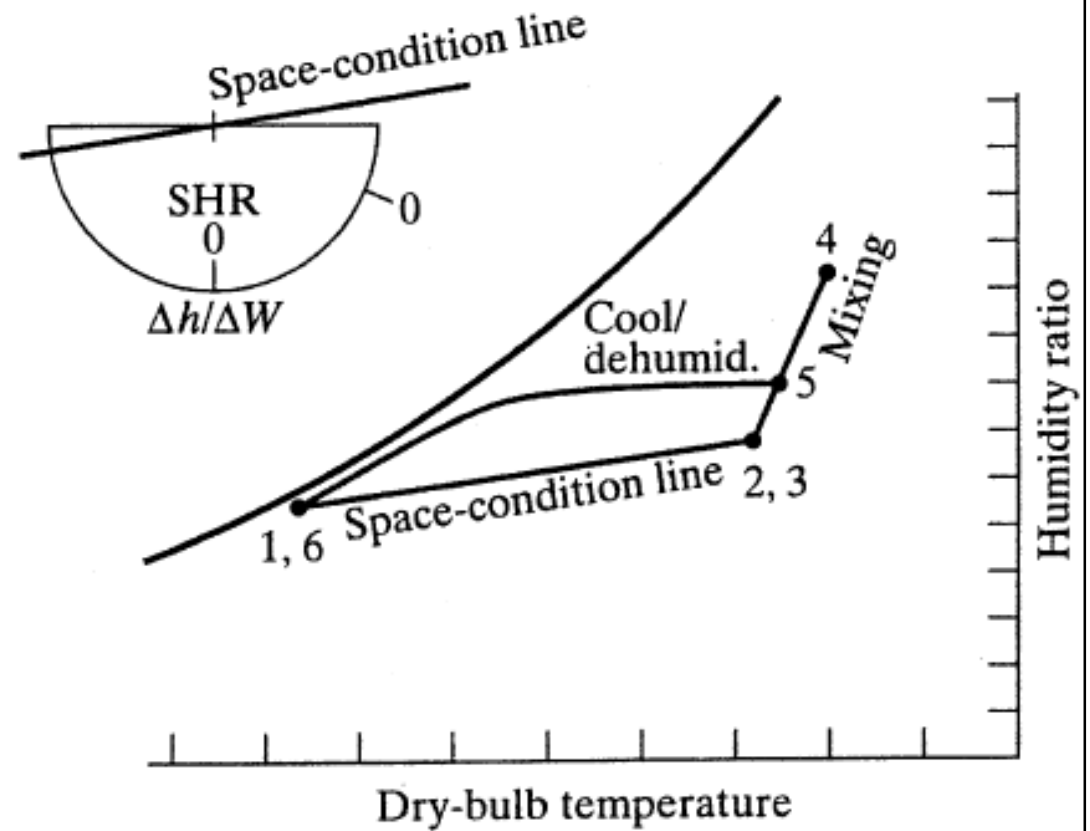
# Determining entering air conditions



# Simple air conditioning cycle



(a)

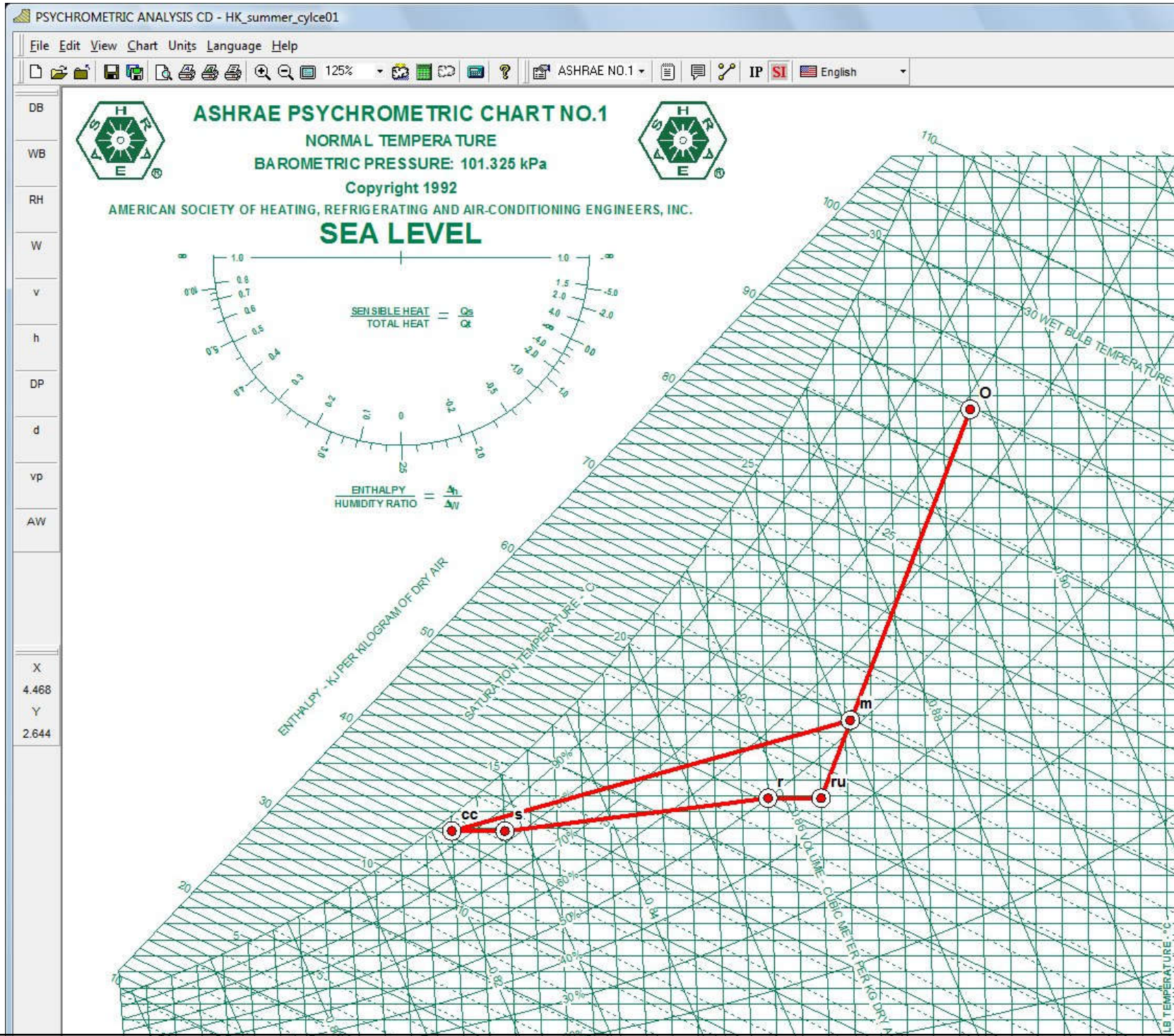


(b)

Can you draw such a cycle for Hong Kong summer conditions?

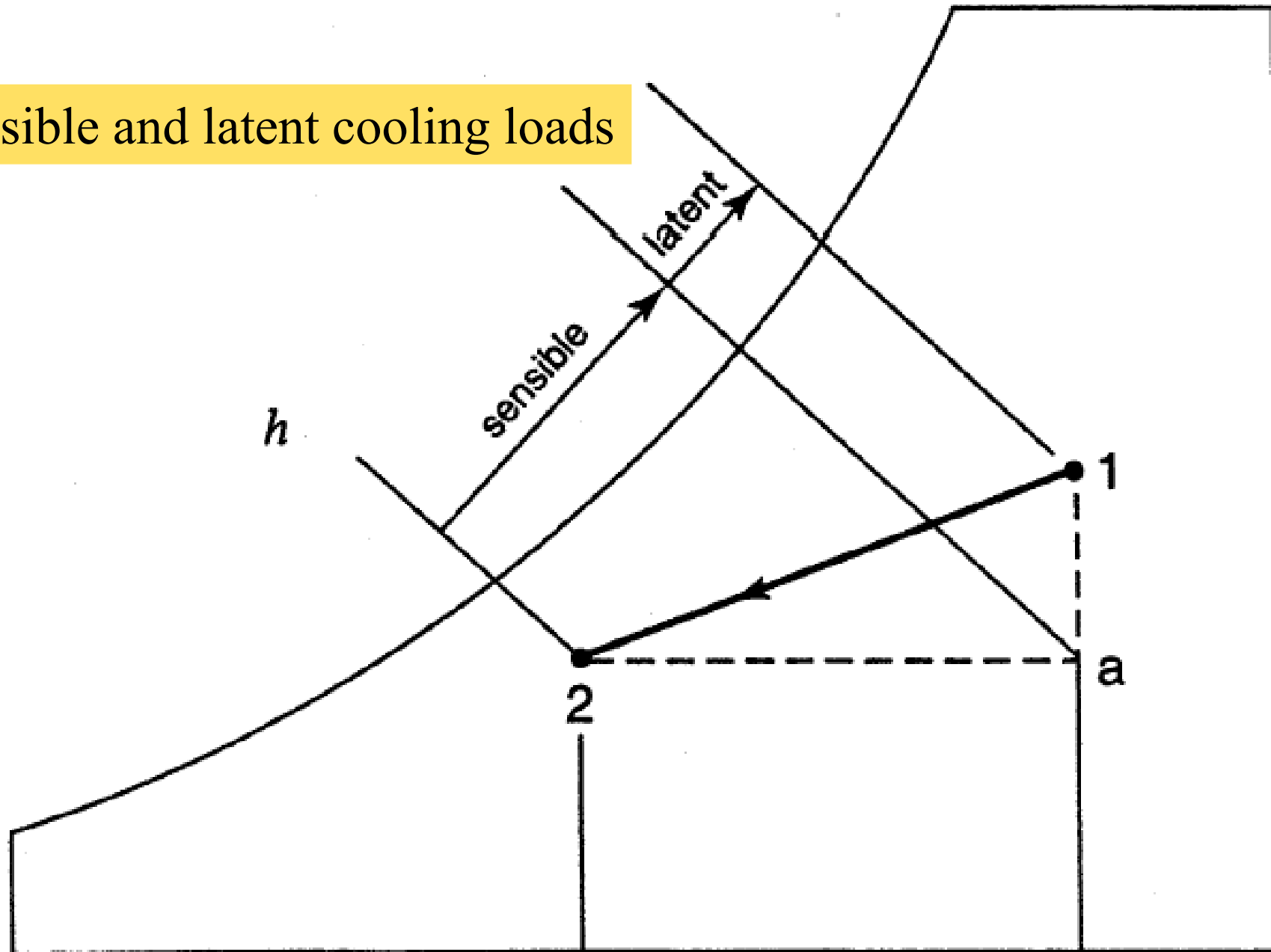
- Outdoor: DBT = 33 °C; WBT = 28 °C; flow = 20% of supply air
- Indoor: DBT = 25 °C; %RH = 50%
- Air leaving cooling coil: DBT = 13 °C; %RH = 95%

# An example of Hong Kong summer air-conditioning cycle

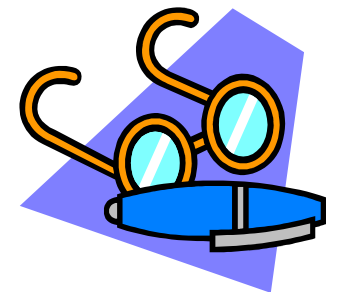


Using psychrometric chart to represent different HVAC systems  
(provide a visualization of the processes of air-conditioning cycles)

Sensible and latent cooling loads



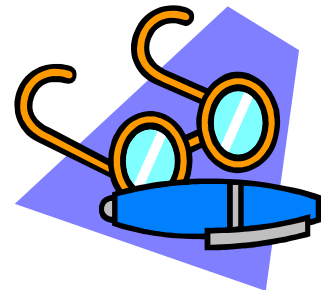
# Psychrometric Processes



- Video demonstration examples of calculations using the psychrometric chart
- An Example Using the Psychrometric Chart (6:25)  
<http://youtu.be/xzT9y0QZz20>
- Use Psychrometric chart for cooling moist air (9:45) <http://youtu.be/A6PVsARawvs>
- Exercises on Advanced Psychrometry (worked examples)
  - [http://ibse.hk/MEBS7012/advanced\\_psychrometry\\_exercise.pdf](http://ibse.hk/MEBS7012/advanced_psychrometry_exercise.pdf)



# Psychrometric Processes

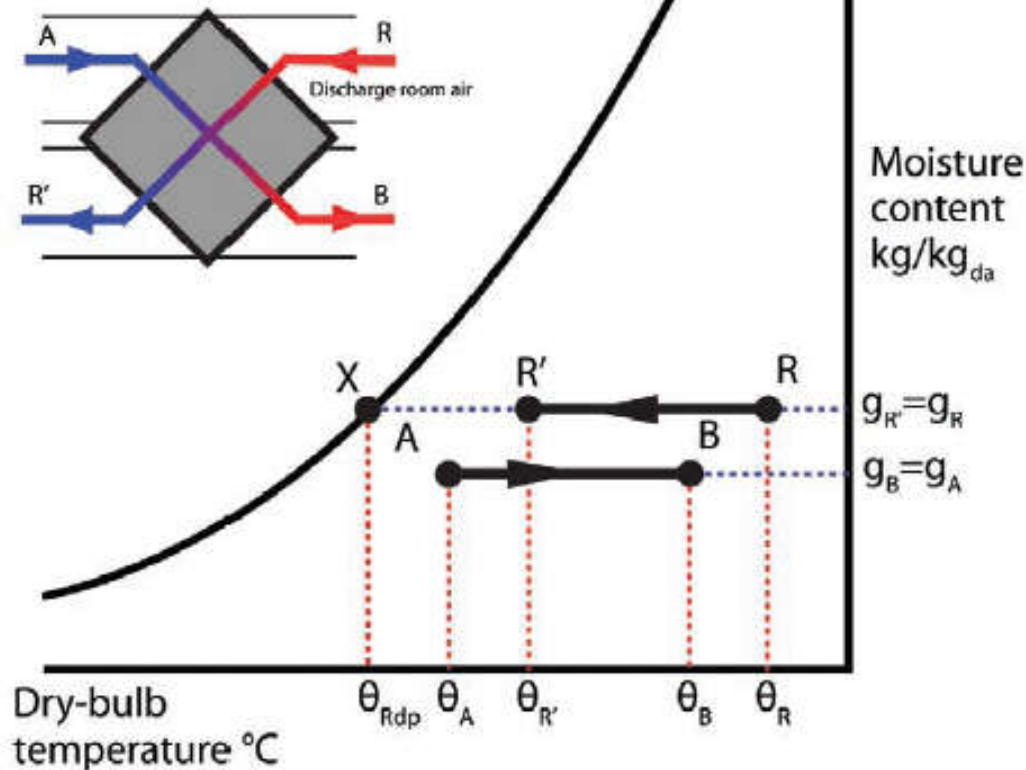


- Typical calculations:
  - 1. Sensible heat ratio (SHR)
    - SHR is the ratio of sensible heat load to total heat load
  - 2. Space cooling load
  - 3. Cooling coil's load/capacity
  - 4. Humidification capacity
  - 5. Mixing processes
    - Using principles of heat balance & conservation of mass

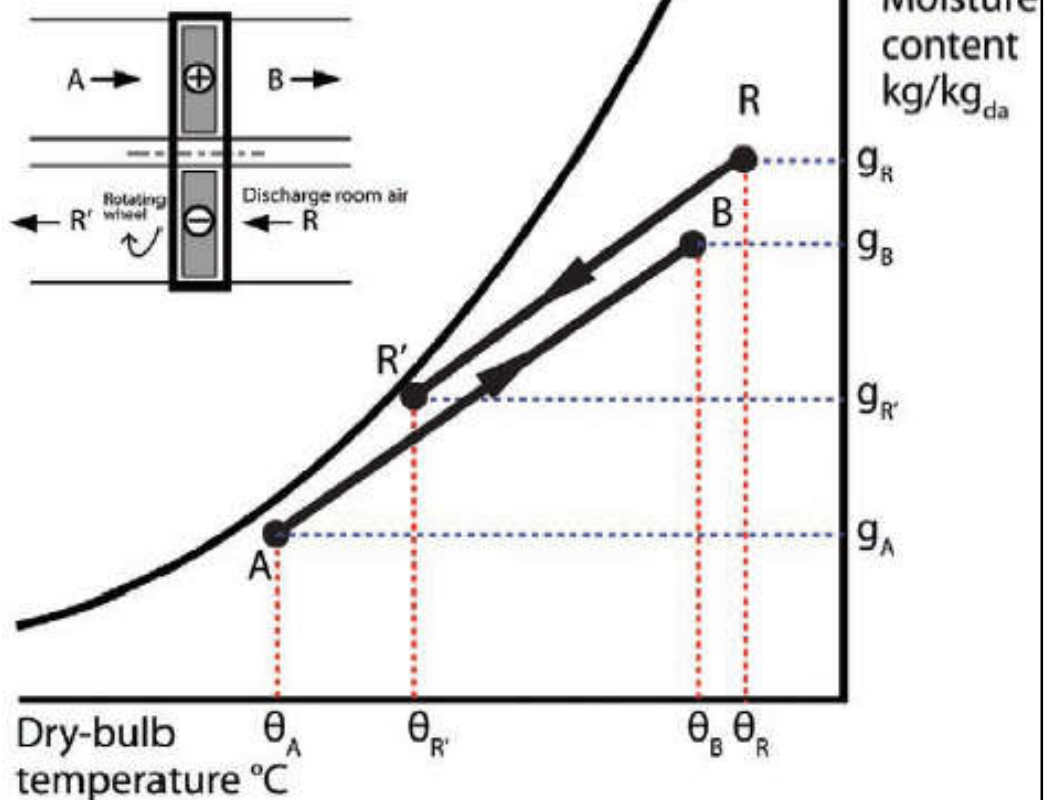


# The psychrometrics of HVAC sub-systems

## Plate Heat Exchanger (sensible heat recovery)



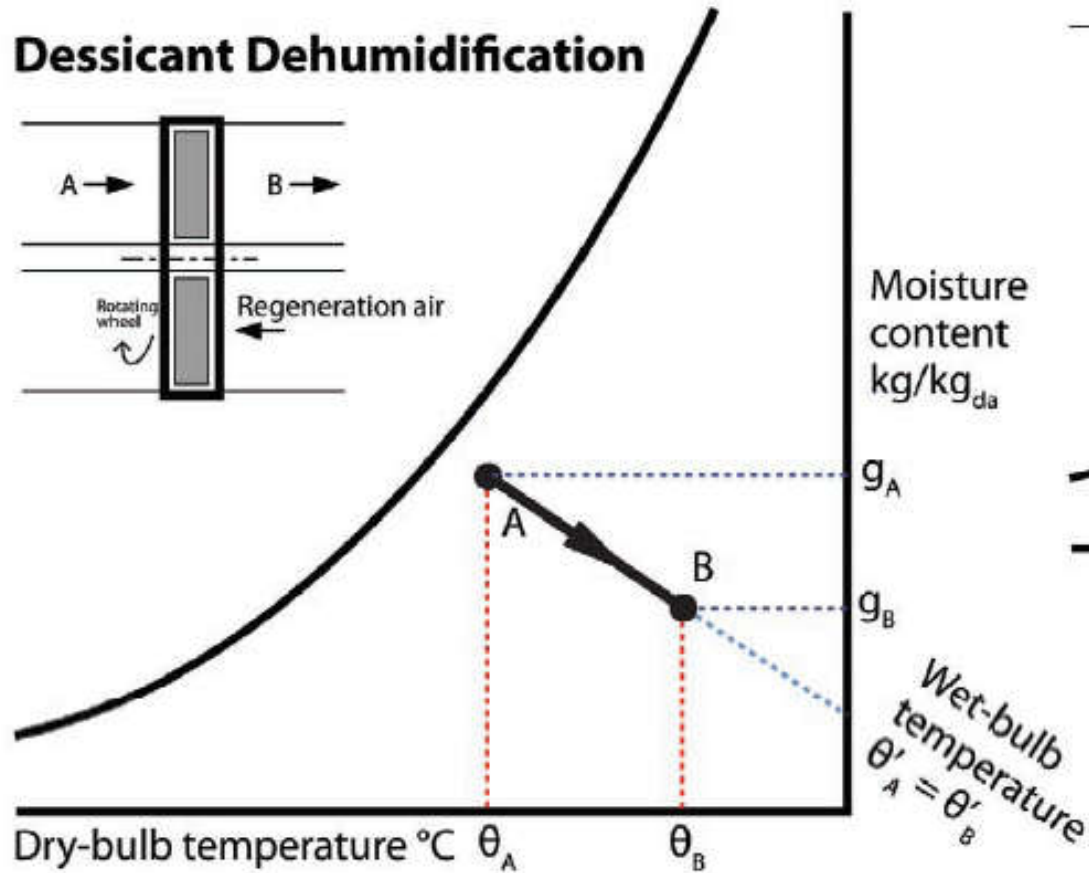
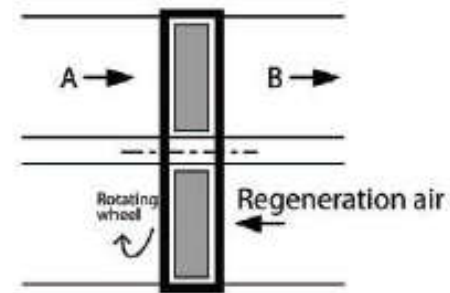
## Regenerative Thermal Wheel (sensible + latent heat recovery)



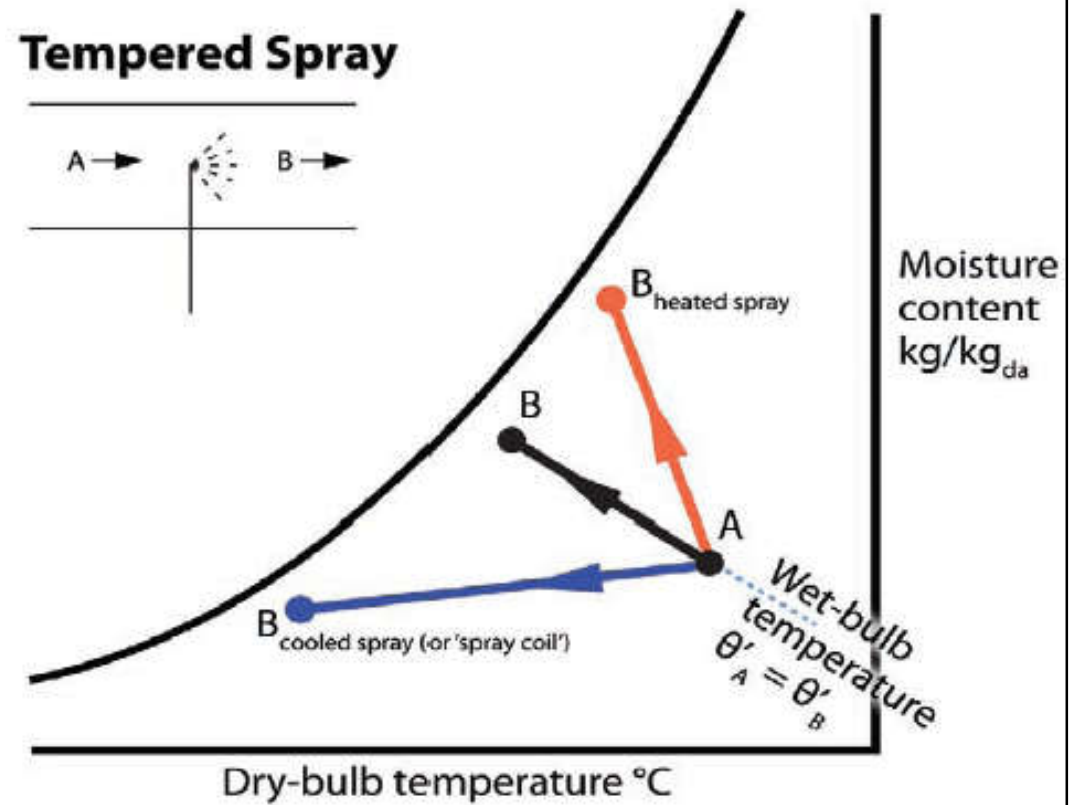
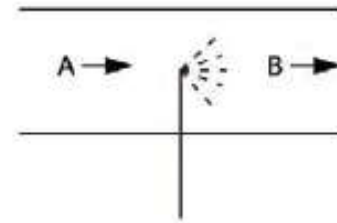
Do you know how to represent the processes of different HVAC sub-systems on the psychrometric chart?

# The psychrometrics of HVAC sub-systems (cont'd)

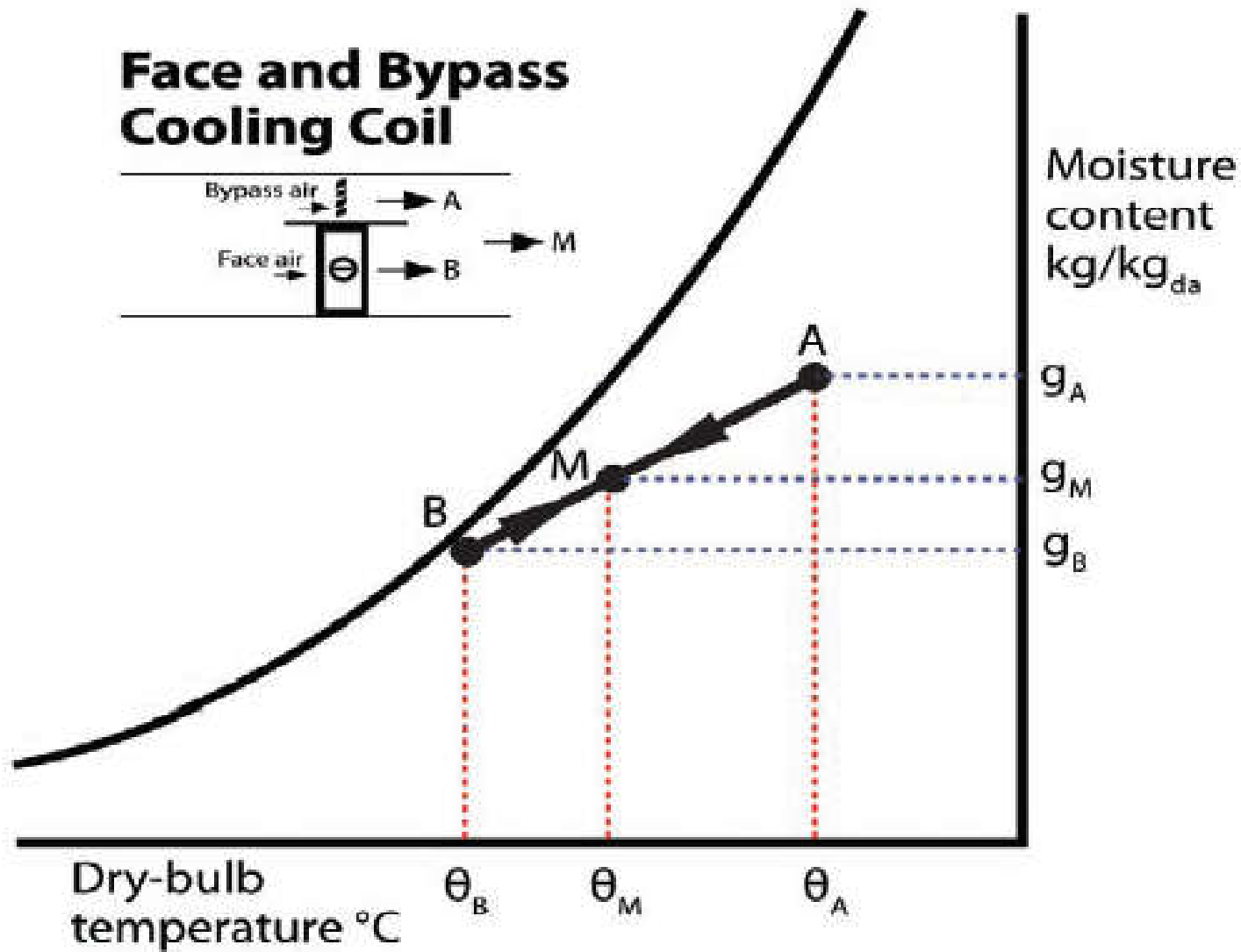
## Dessicant Dehumidification



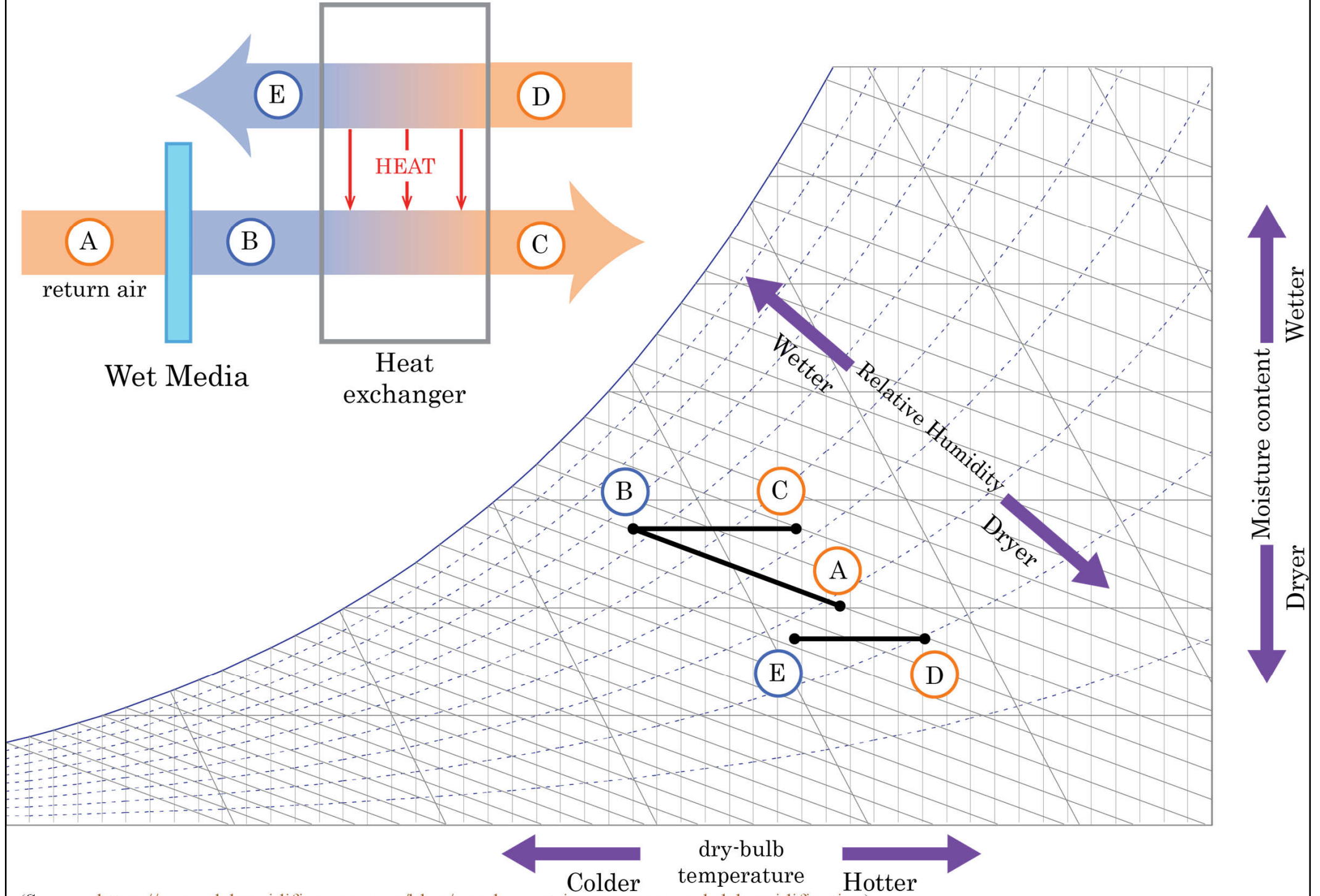
## Tempered Spray



# The psychrometrics of HVAC sub-systems (cont'd)



# Psychrometric processes and dehumidification



(Source: <https://www.dehumidifiercorp.com/blog/psychrometric-processes-and-dehumidification>)

# Psychrometric Software

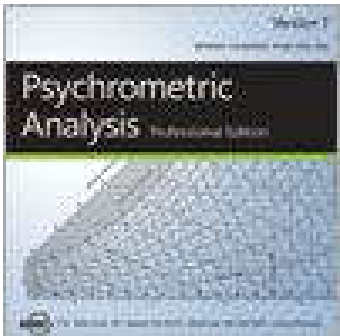


- Latest trends:
  - Apply computer software & mobile apps for psychrometric chart and calculations
  - Online psychrometric charts and calculators
  - Use of psychrometric chart analysis for climatic data, thermal comfort, system design & operation of HVAC or drying systems (e.g. for food, medicine & agriculture)

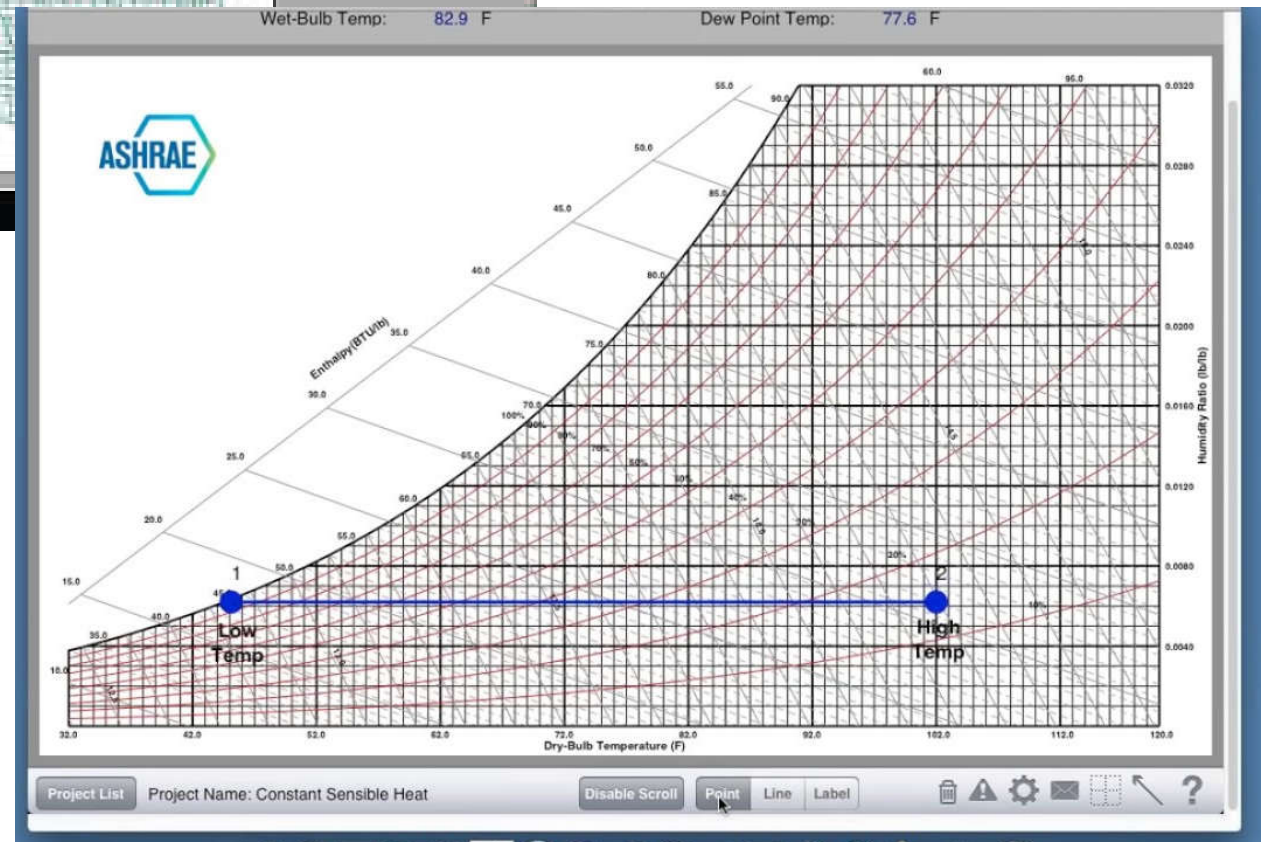
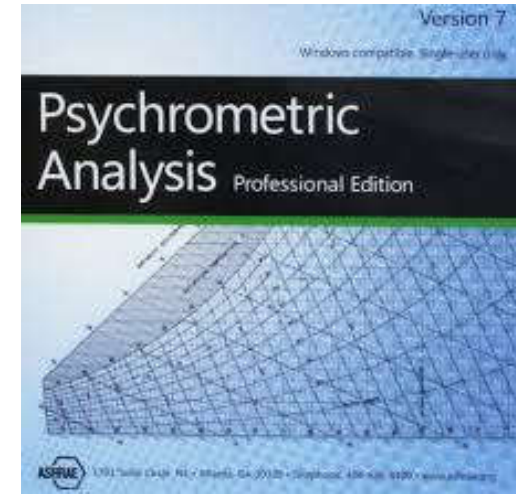
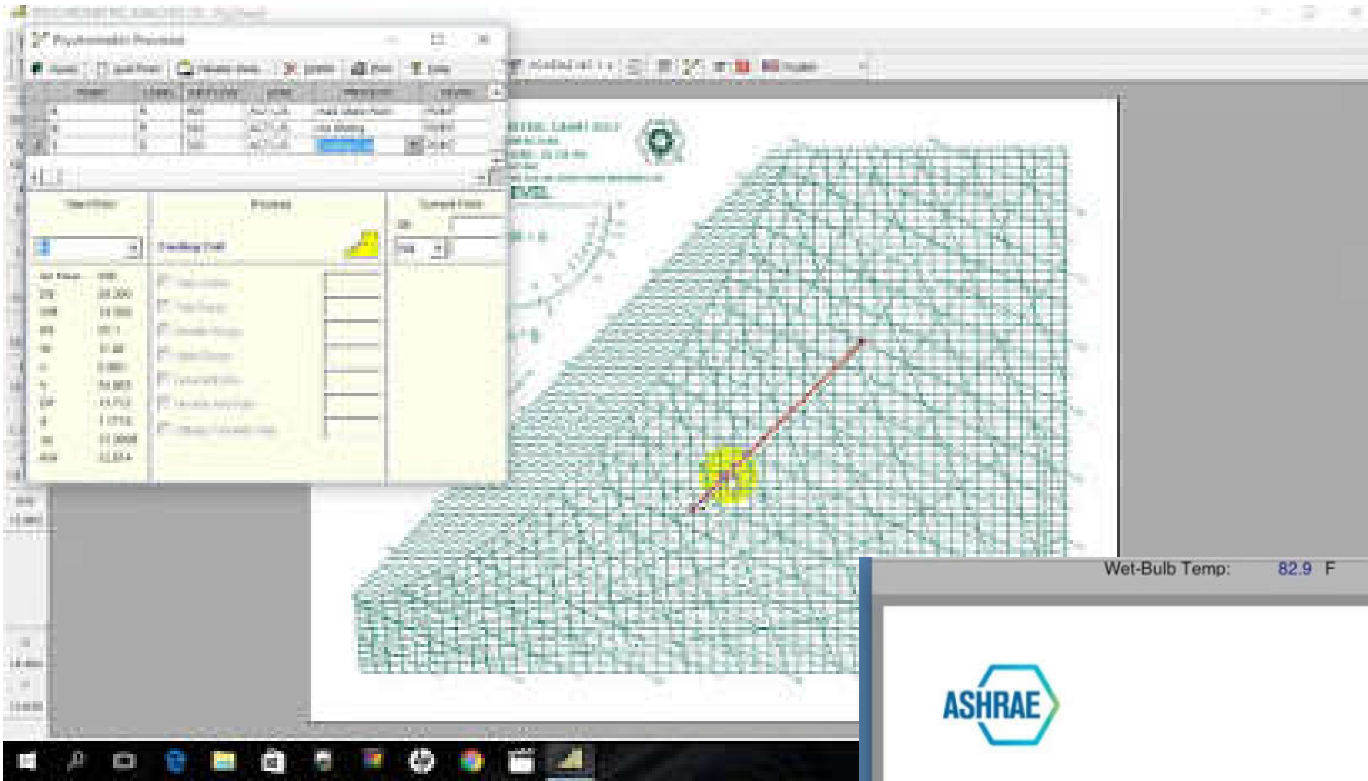
# Psychrometric Software



- ASHRAE Psychrometric Analysis CD-ROM (2012, 2007, 2002) [AV 697 P97]
  - The program allows the user to plot typical psychrometric processes and perform the corresponding energy calculations
    - The program produces near-exact replications of the charts and can output a listing of points and processes in a tabular report with calculated properties and energy values for each. It includes a presentation of the ASHRAE climate data presented in the 2009 ASHRAE Handbook - Fundamentals



# ASHRAE Psychrometric Analysis Software and Mobile App



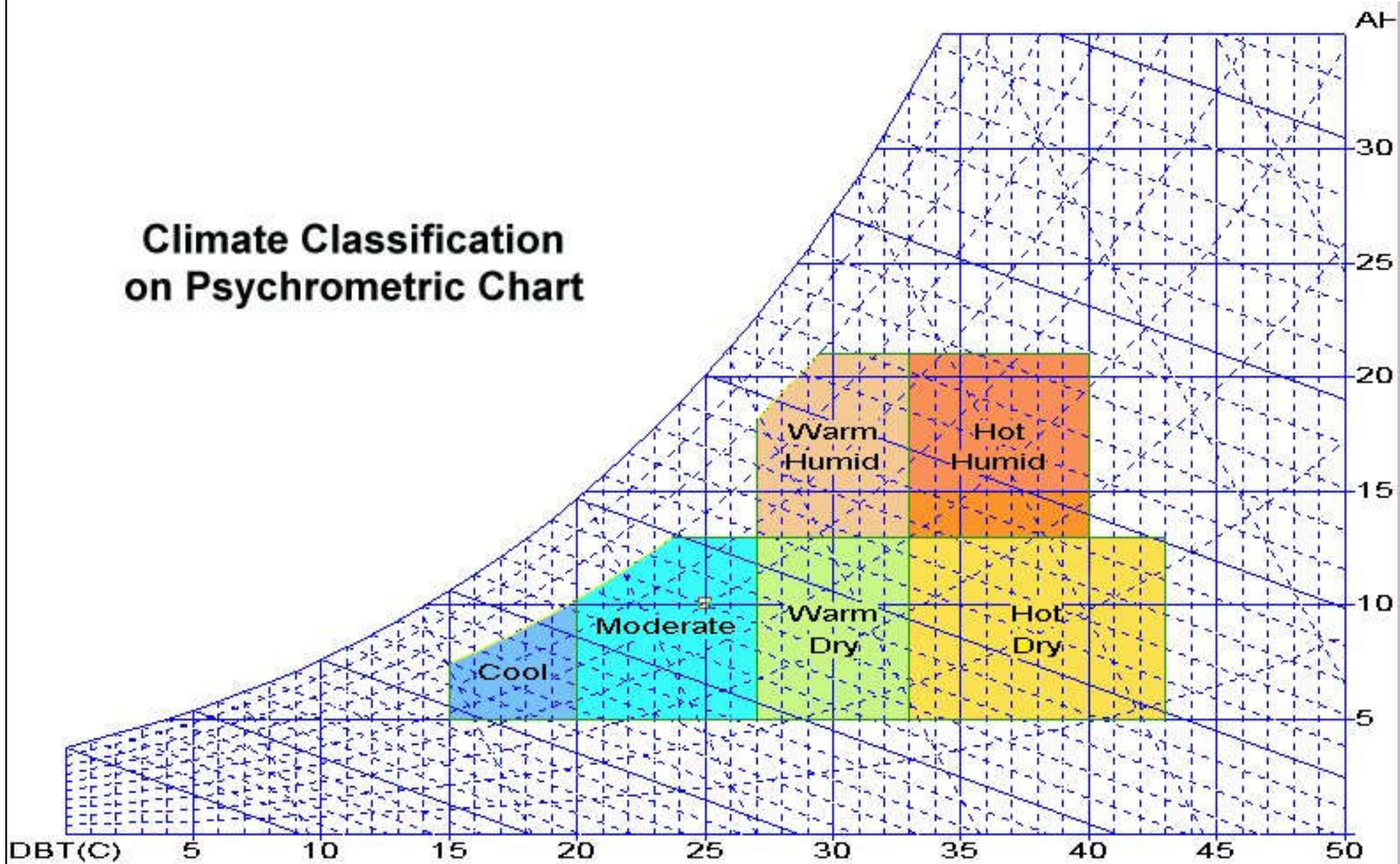
# Psychrometric Software



- Other examples of psychrometric software:
  - ArchiSci Software – PSYCHWIN
    - <http://ibse.hk/archisci.zip>
  - Daikin's Psychrometrics tool
    - [https://www.daikin.eu/en\\_us/customers/software-downloads/daikin-psychometrics-diagram-viewer.html](https://www.daikin.eu/en_us/customers/software-downloads/daikin-psychometrics-diagram-viewer.html)
  - HDPsyChart (Hands Down Software)  
<http://www.handsdownsoftware.com/Downloads.htm>
  - Psychrometric Chart (PSY) software
    - <http://www.vector.co.jp/soft/win95/business/se288946.html>

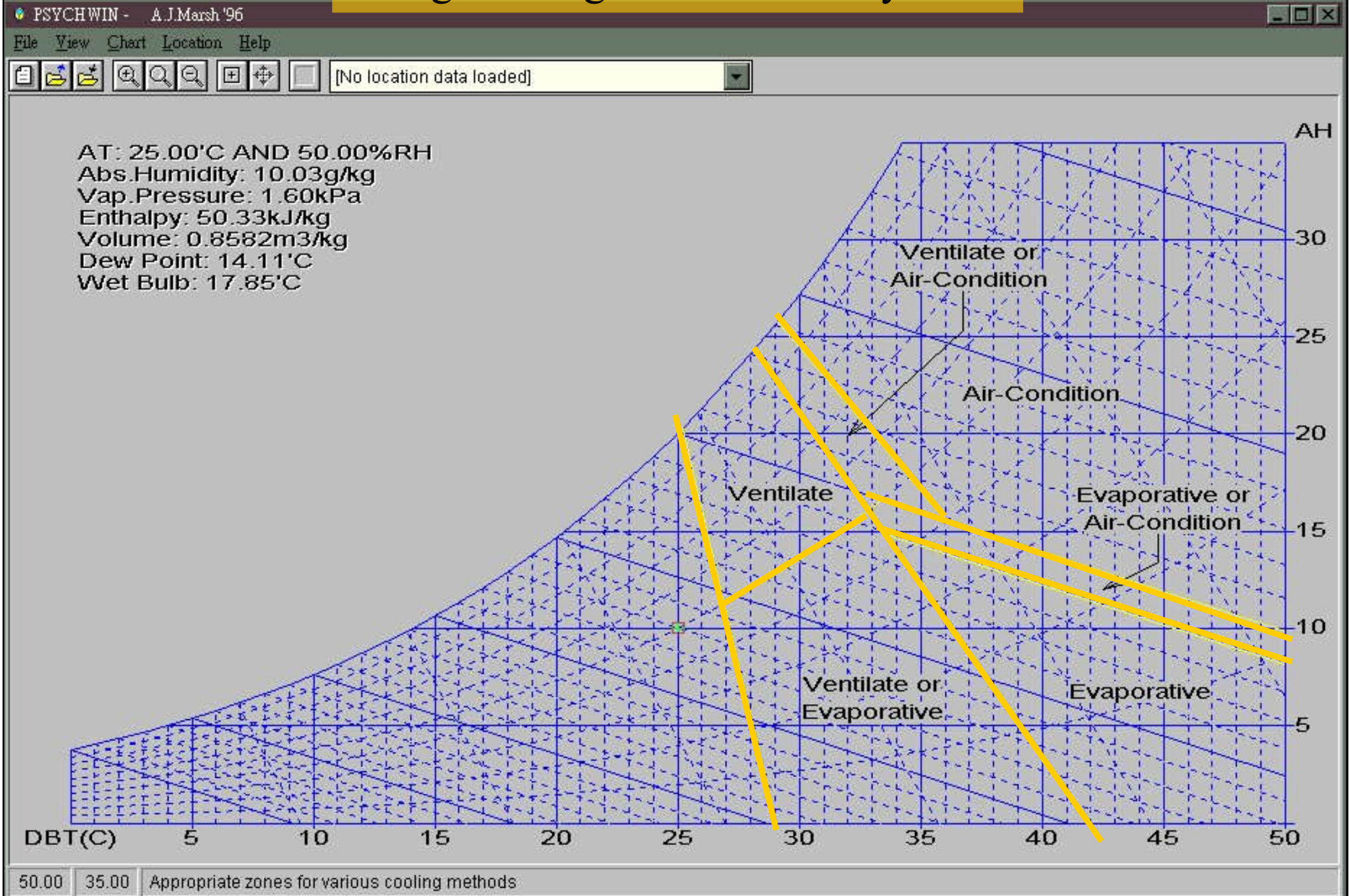


# Climate Classification on Psychrometric Chart



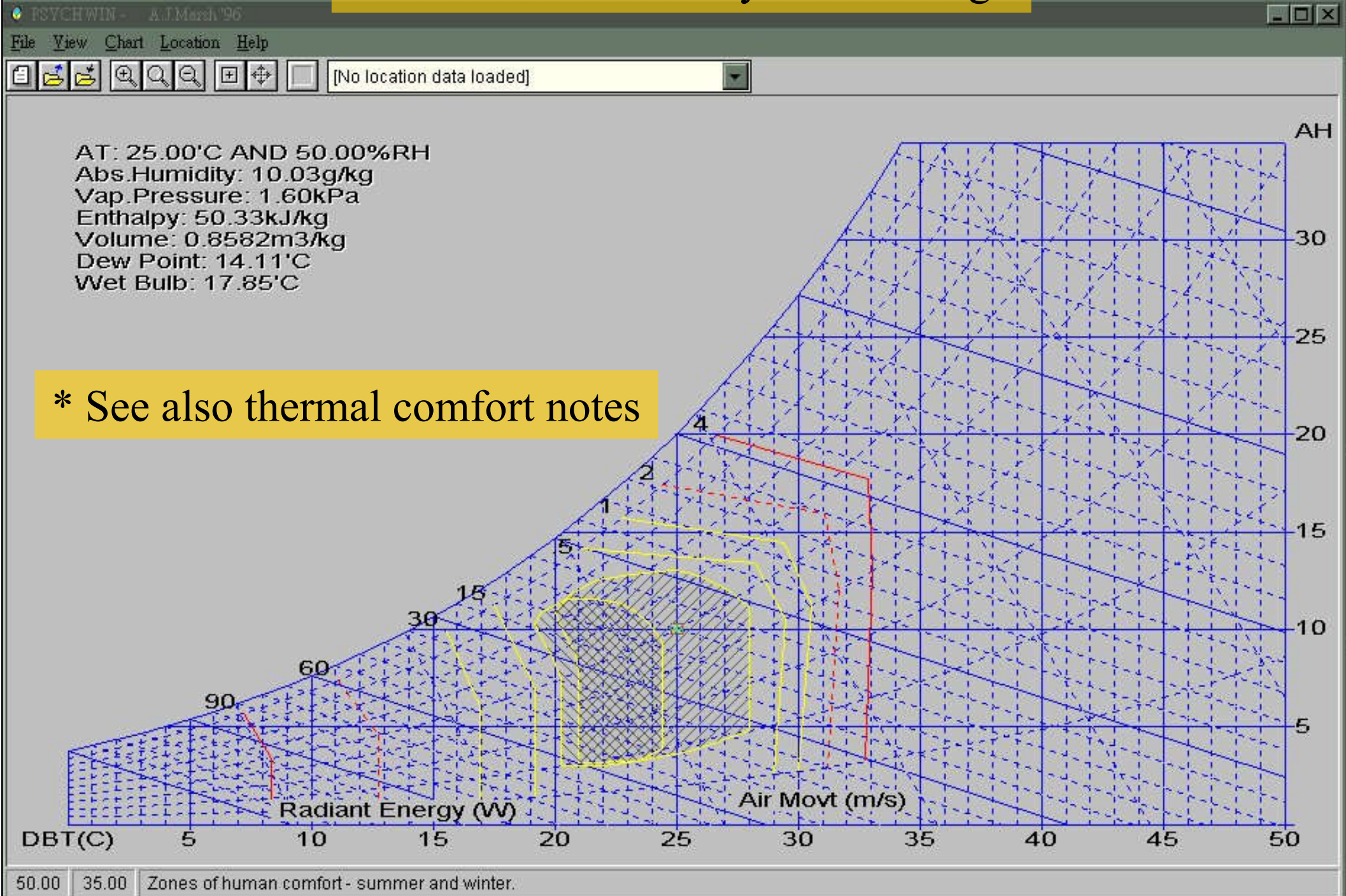
(Source: ArchiSci Software - PSYCHWIN)

# Design strategies for HVAC systems

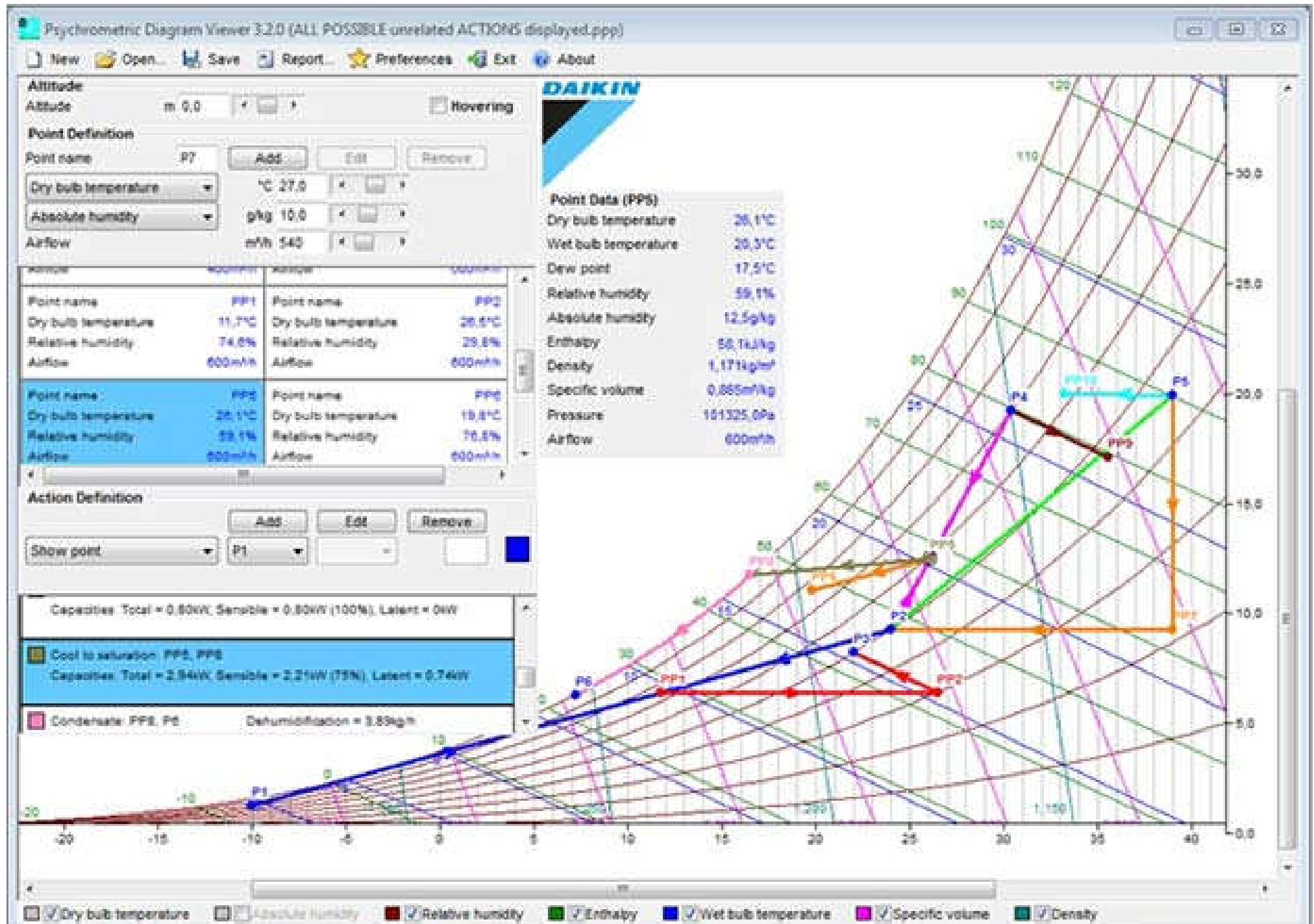


(Source: ArchiSci Software - PSYCHWIN)

# Thermal comfort analysis and design



# Daikin psychrometric diagram viewer software



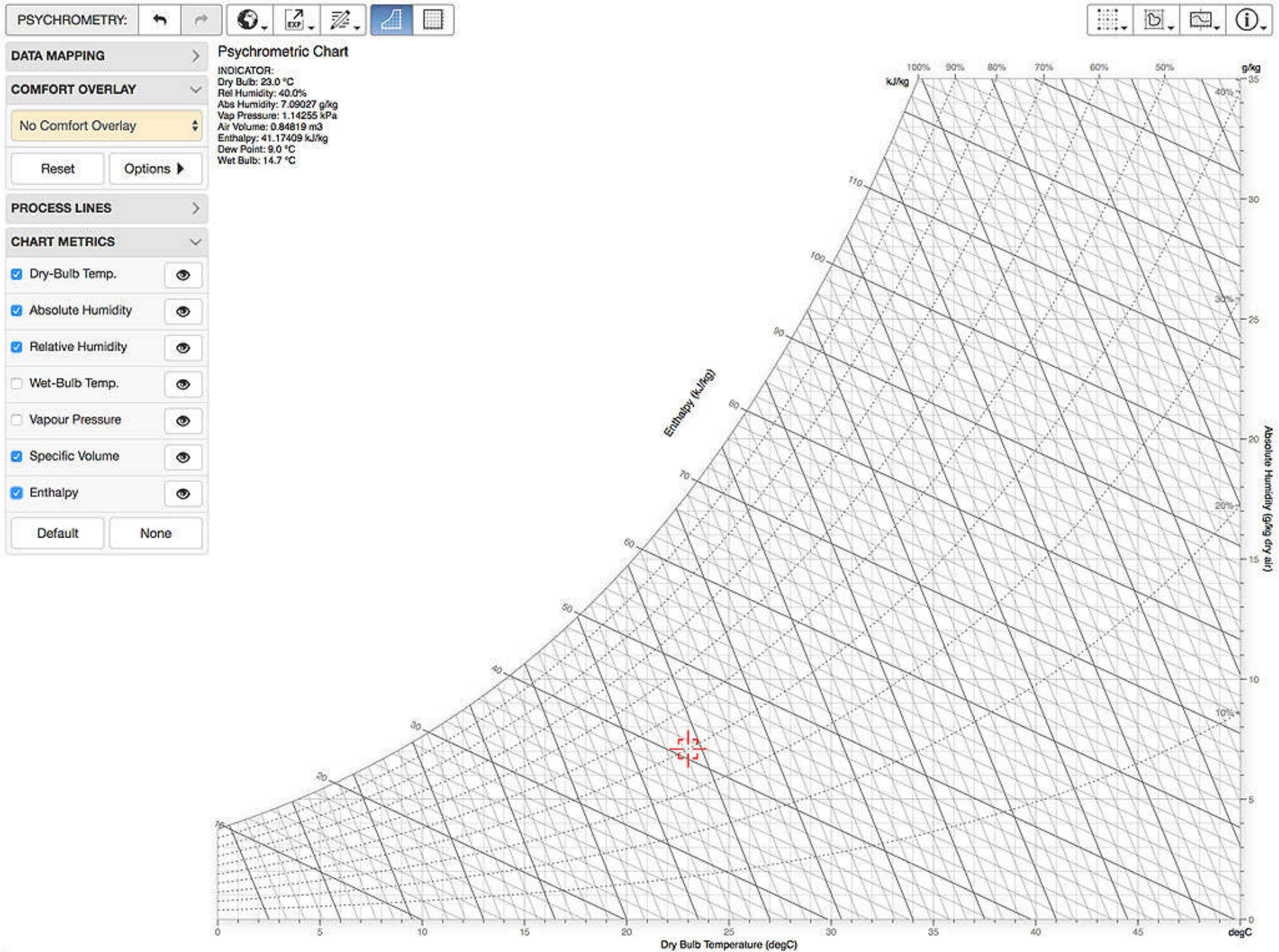
(Source: <https://www.coolingpost.com/products/daikin-upgrades-psychrometric-software/>)

# Psychrometric Software



- Online psychrometric chart (examples)
  - Psychrometric Chart (from Dr. Andrew Marsh)
    - <http://andrewmarsh.com/software/psychro-chart-web/>
    - <https://drajmarsh.bitbucket.io/psychro-chart2d.html>
  - PsyOnline (by FlyCarpet) (English & Chinese)
    - <http://www.flycarpet.net/en/PsyOnline>
  - Online psychrometric chart and calculator
    - <https://www.herramientasingeneria.com/onlinecalc/psychrometrics/psychrometrics.html>

# Psychrometric Chart (from Dr. Andrew Marsh)



# PsyOnline (by FlyCarpet)

www.flycarpet.net/en/PsyOnline

Home About Projects Contact

Free Online Psychrometric Chart World's first online, and only! A convenient, precise and powerful psychrometric chart & calculator tool for HVAC engineers.

Basic Process Cycle 1 Cycle 2 Setting Display 简体中文

Click on chart for air properties

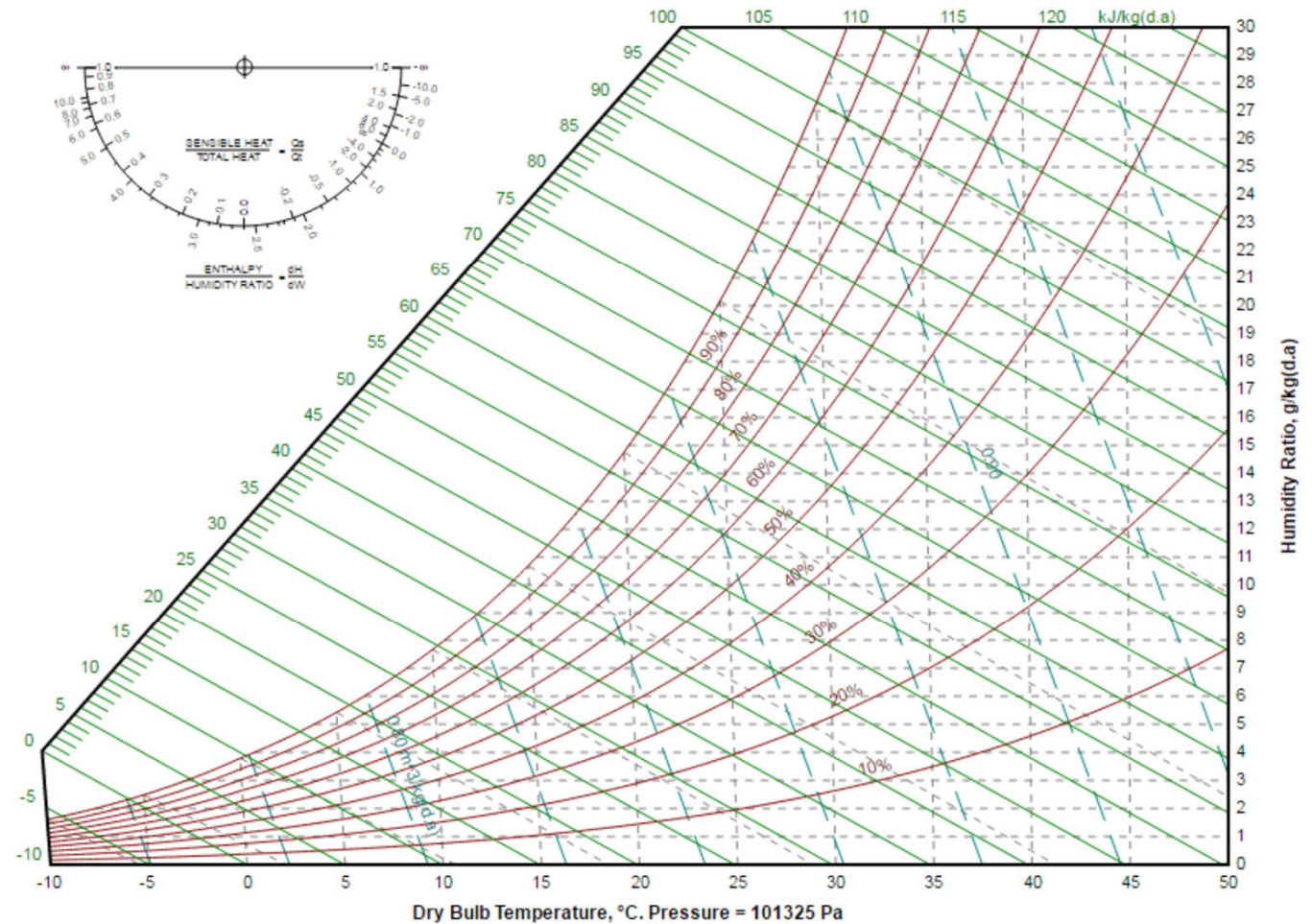
Or input data for air properties

T.Dry, °C 25

Rel.Humid, % 50

Quantity	Value	Units
P.Ambient		Pa
T.Dry Bulb		°C
Humid.Ratio		g/kg(d.a)
Rel.Humid		%
T.Wet.Bulb		°C
T.Dew		°C
T.Saturation		°C
Enthalpy		kJ/kg(d.a)
P.Vapour		Pa
P.Sat.Vapour		Pa
Spec.Heat		kJ/(kg.K)

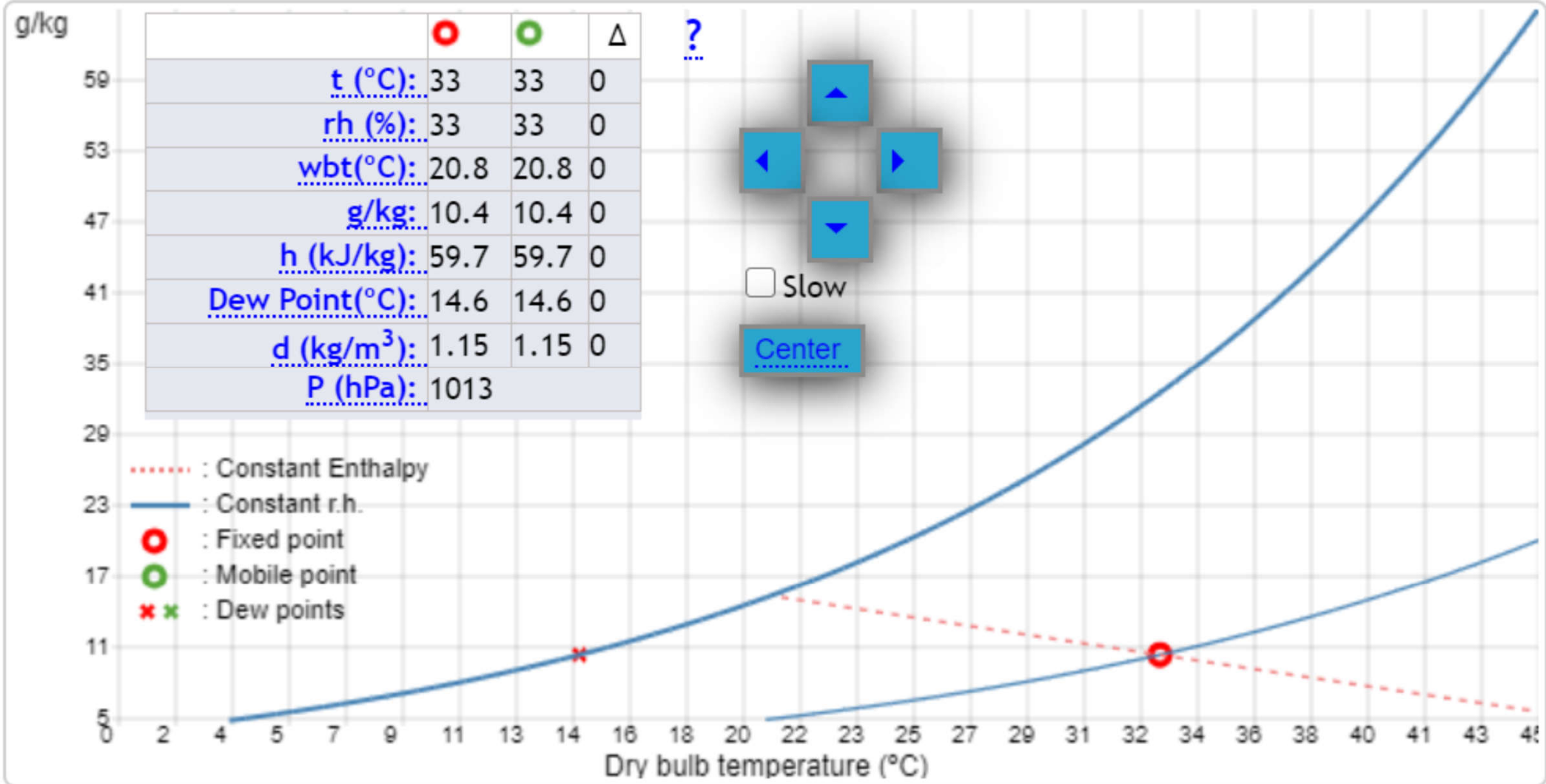
Stop and Play. We have a free small game for you: Survive Broken. Click to start play.



(Source: <http://www.flycarpet.net/en/PsyOnline>)

# Online psychrometric chart and calculator

## Interactive Psychrometric Diagram.



(Source: <https://www.herramientasingeneria.com/onlinecalc/psychrometrics/psychrometrics.html>)

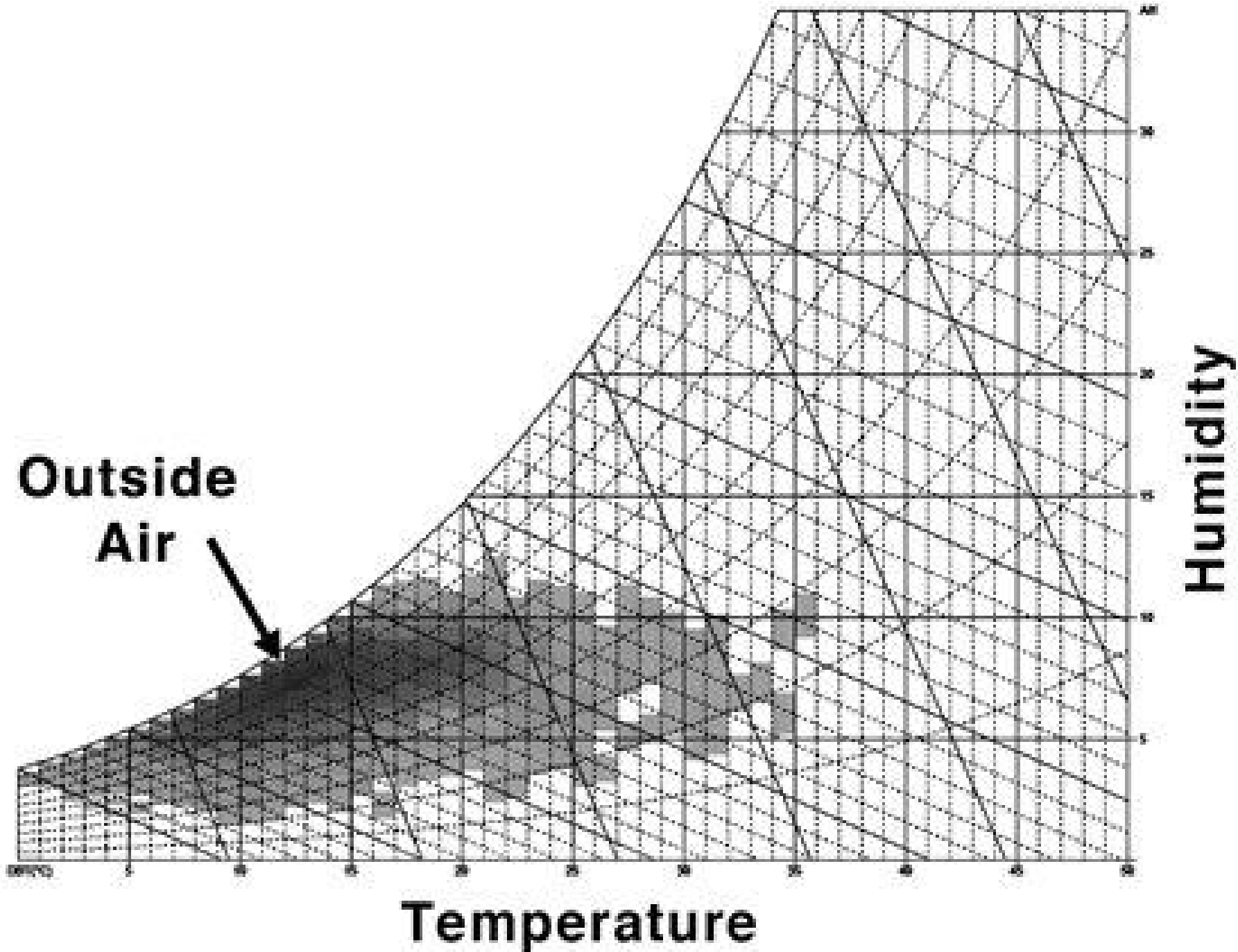


# Psychrometric Analysis

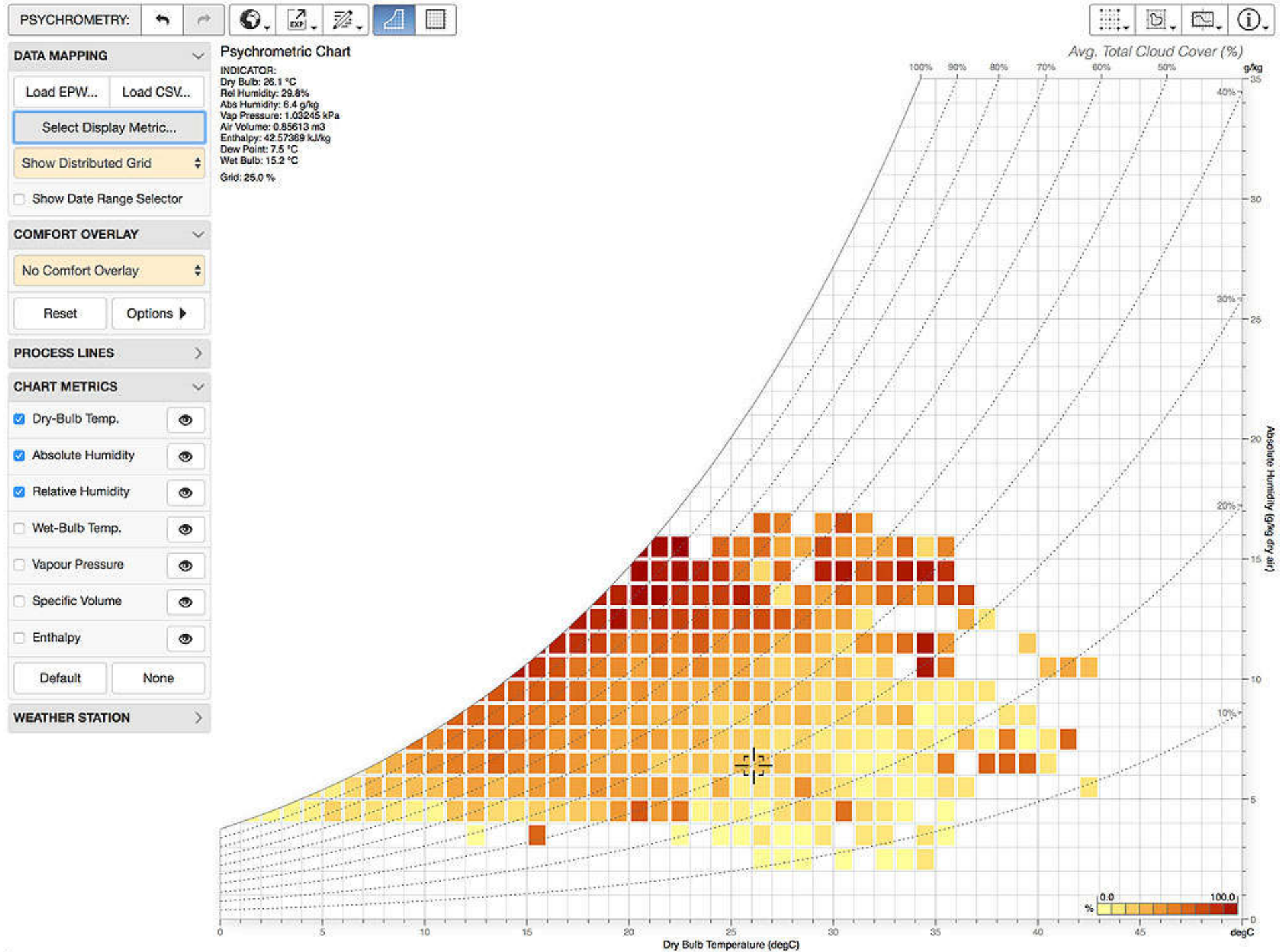


- Using psychrometric chart to analyse moist air
  - Climate analysis
    - Frequency distribution of annual weather data on psychrometric charts
  - Thermal comfort analysis
    - Bioclimatic analysis (such as Givoni bioclimatic chart)
    - Thermal comfort zones & index
      - ASHRAE Standard 55 (<https://comfort.cbe.berkeley.edu/>)
  - Cooling & ventilation strategies
    - Natural ventilation & passive cooling design

# Analysis of outside air (climatic) conditions using a psychrometric chart

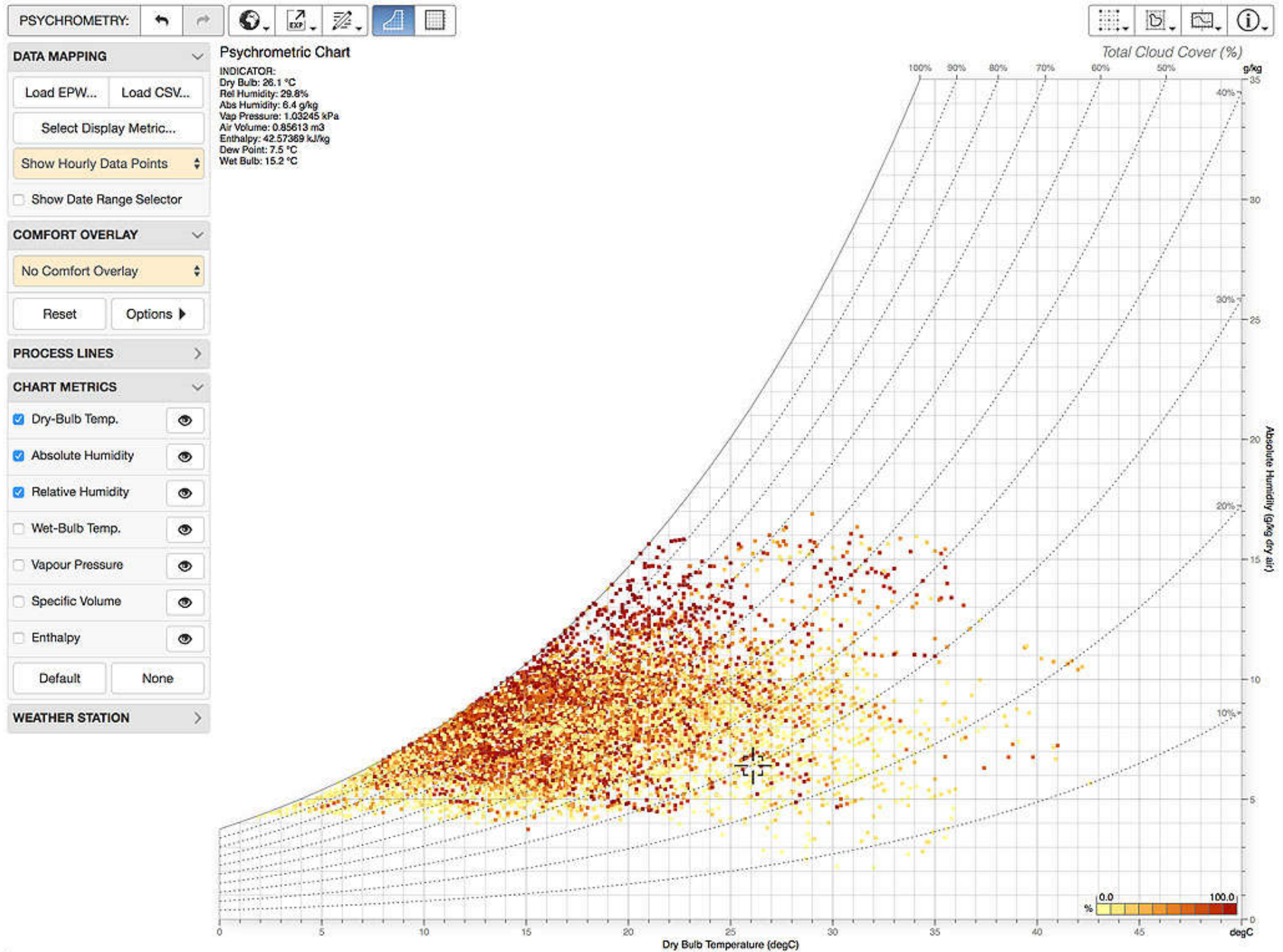


# Hourly climatic data as a distributed grid



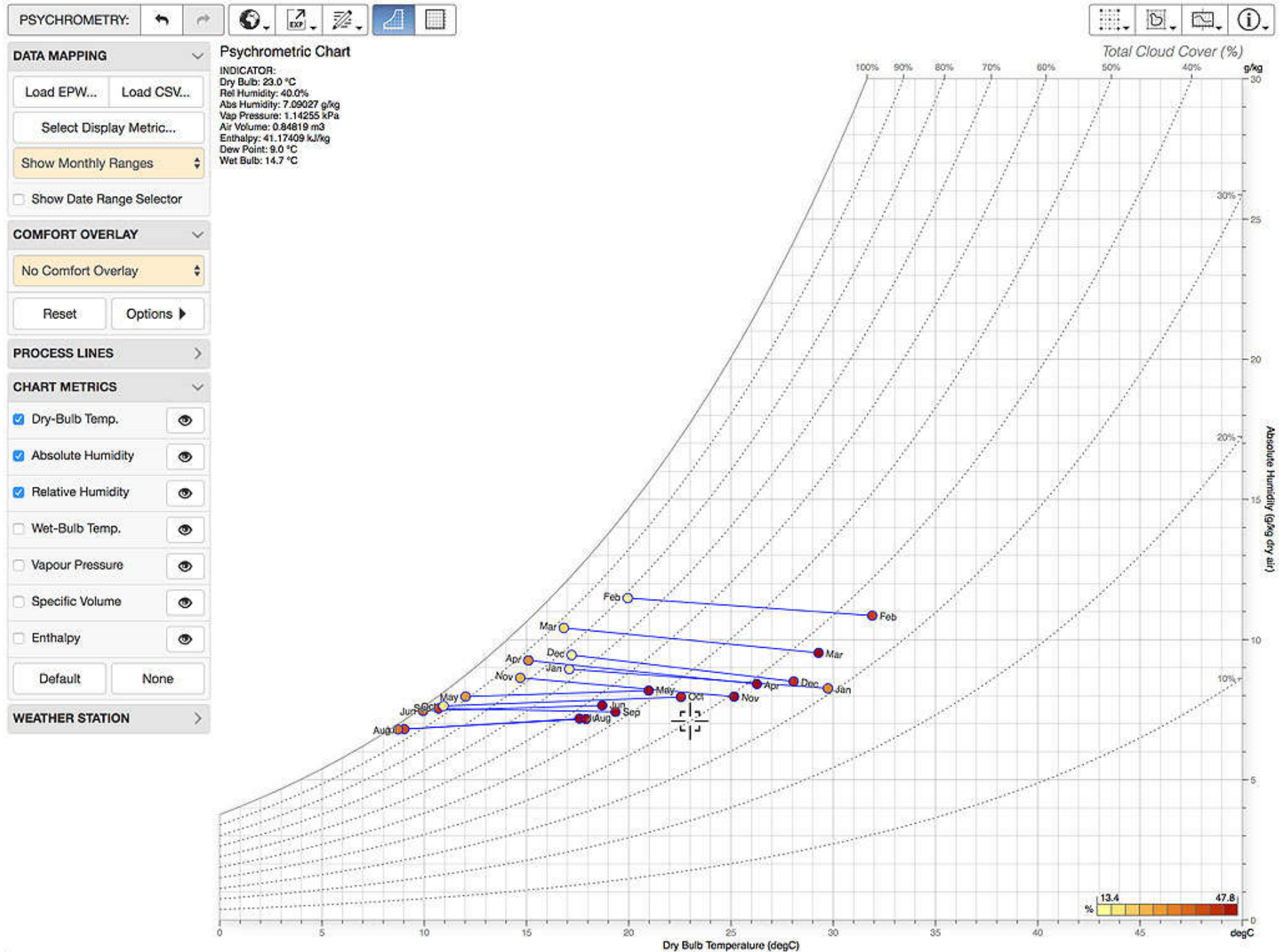
(Source: <http://andrewmarsh.com/software/psychro-chart-web/>)

# Climatic data as individual hourly data points



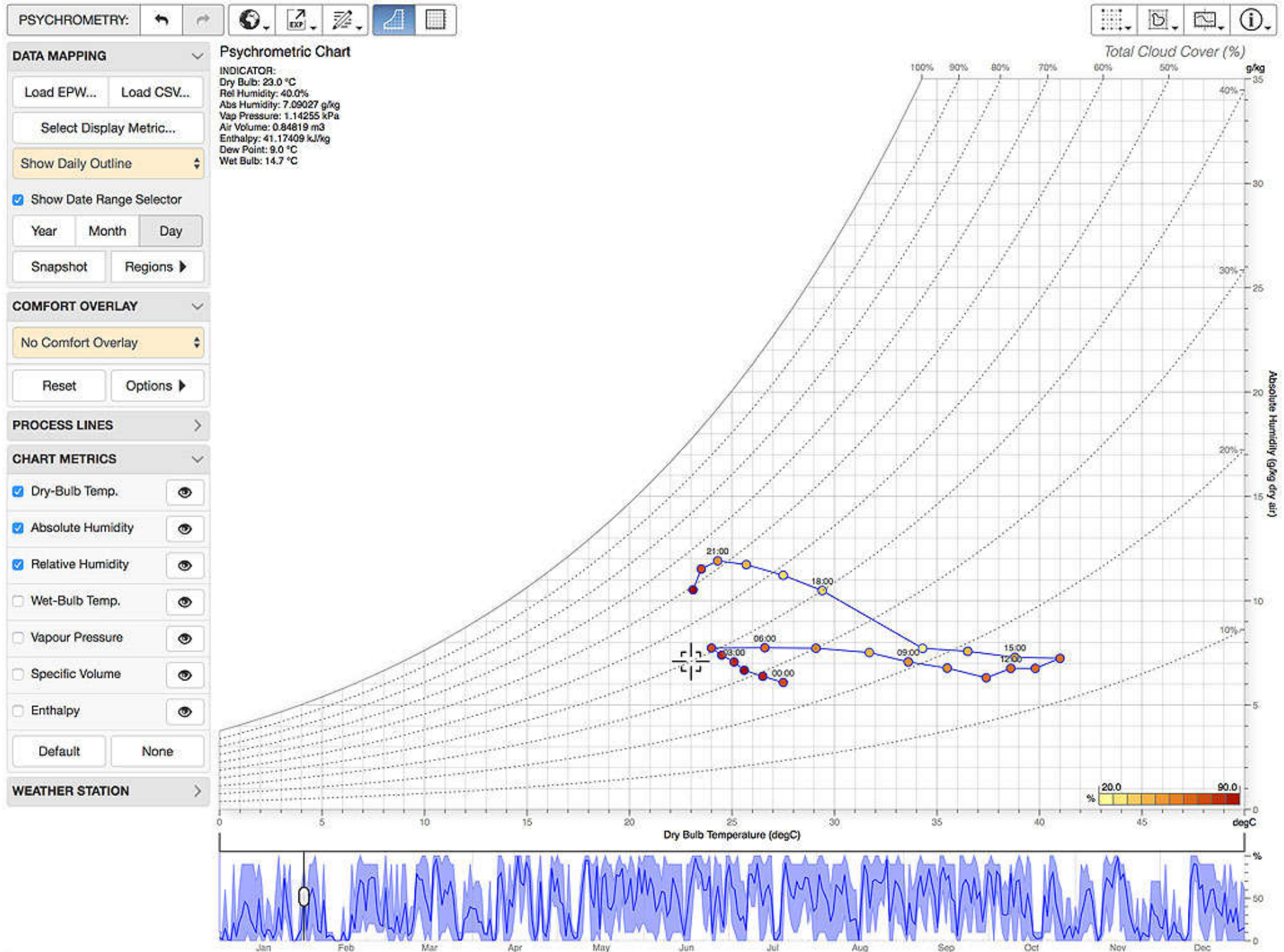
(Source: <http://andrewmarsh.com/software/psychro-chart-web/>)

# Climatic data as monthly mean average min/max lines

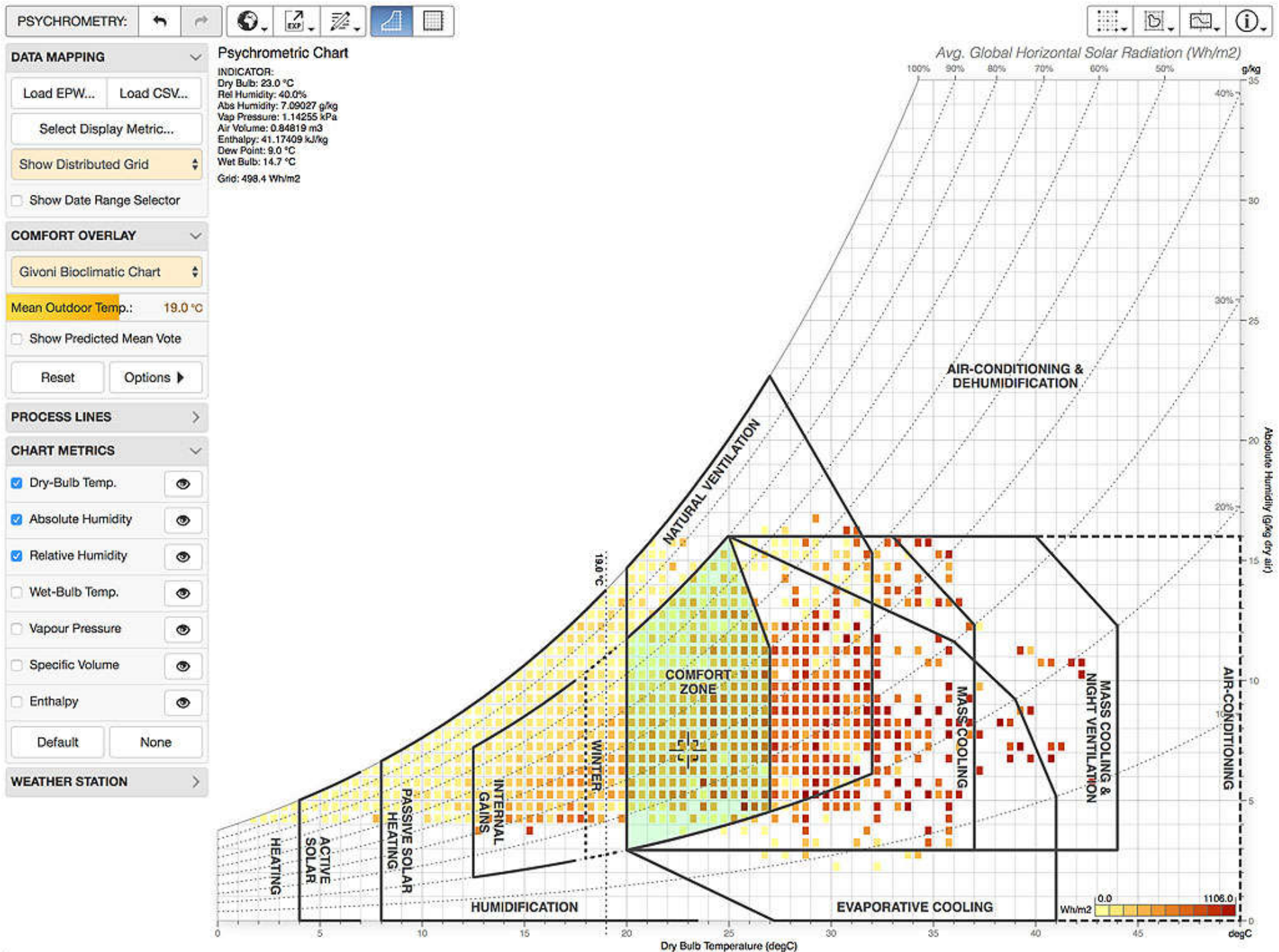


(Source: <http://andrewmarsh.com/software/psychro-chart-web/>)

# Climatic data as track conditions over the course of a day

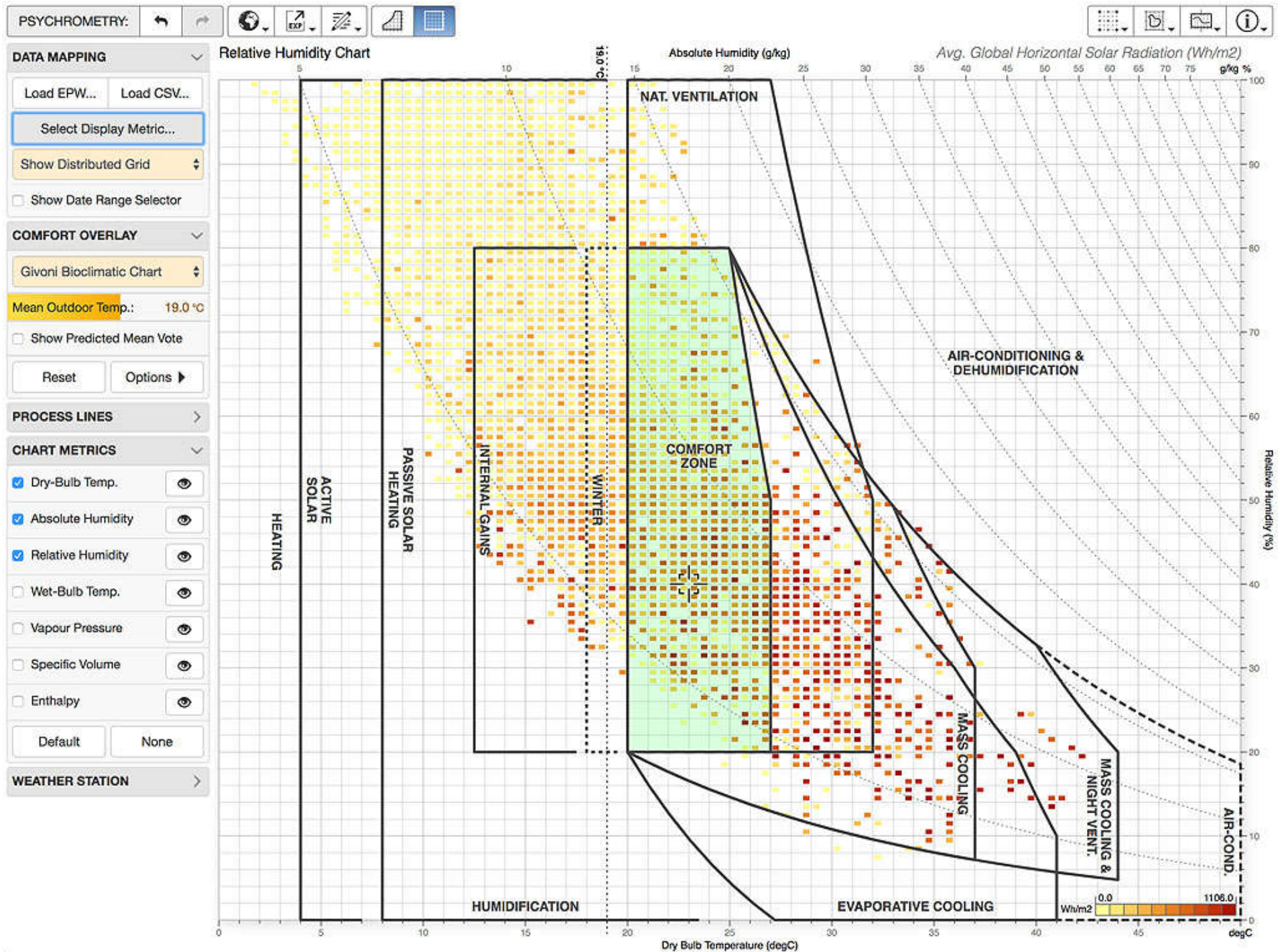


# Bioclimatic analysis using a psychrometric chart



(Source: <http://andrewmarsh.com/software/psychro-chart-web/>)

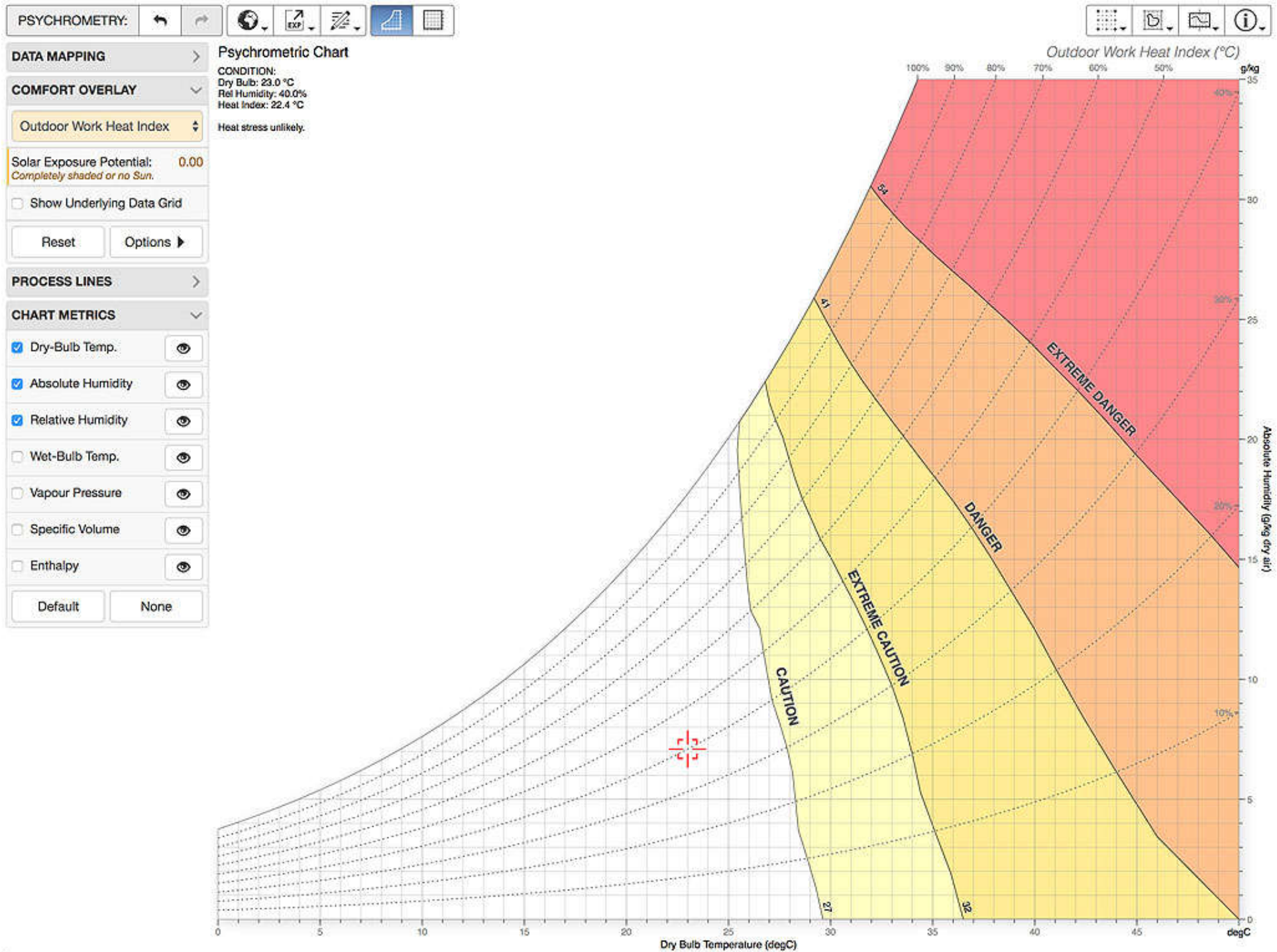
# Bioclimatic analysis using a relative humidity chart



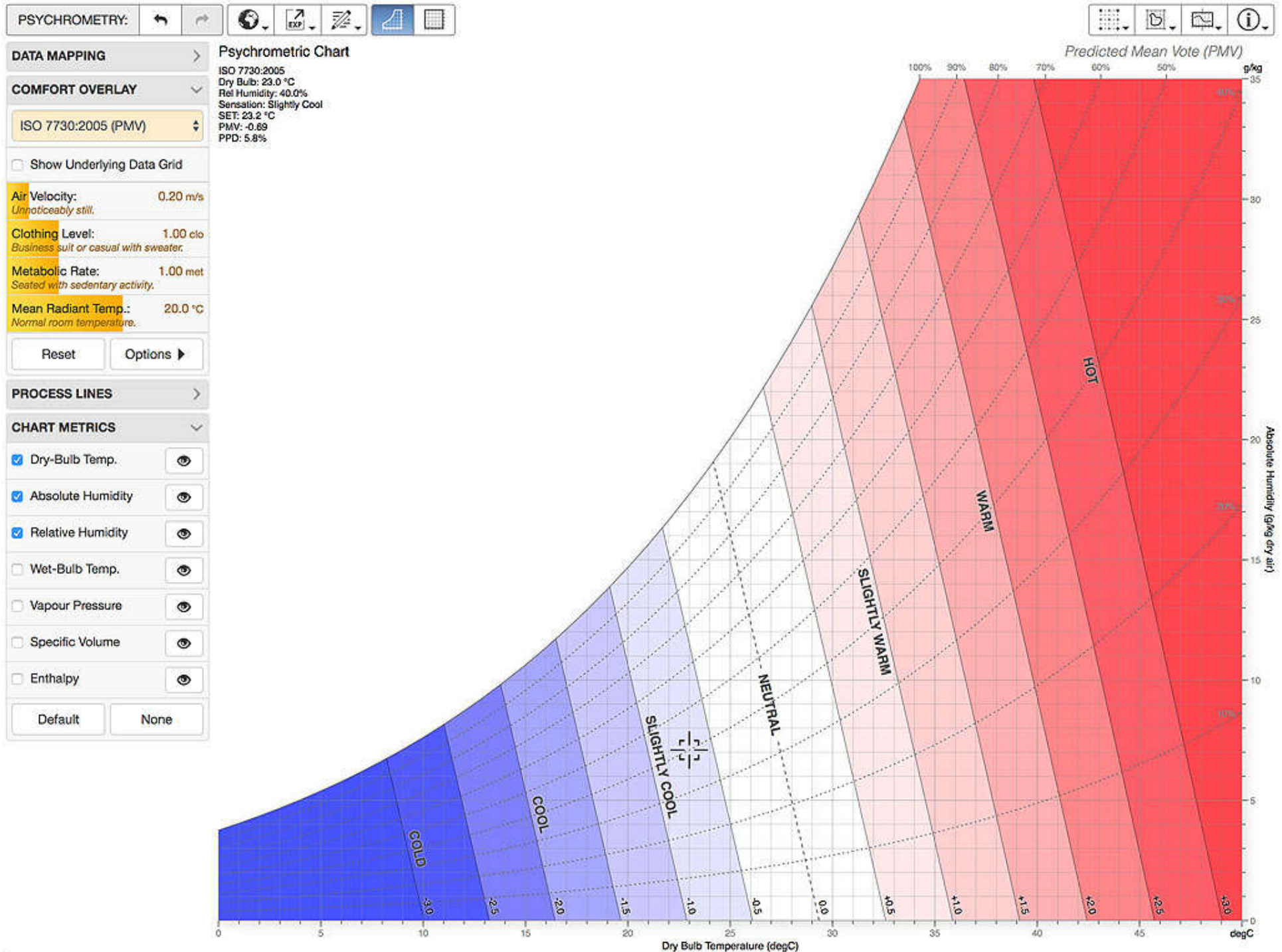
(Source: <http://andrewmarsh.com/software/psychro-chart-web/>)



# Heat index contours mapped over the psychrometric chart

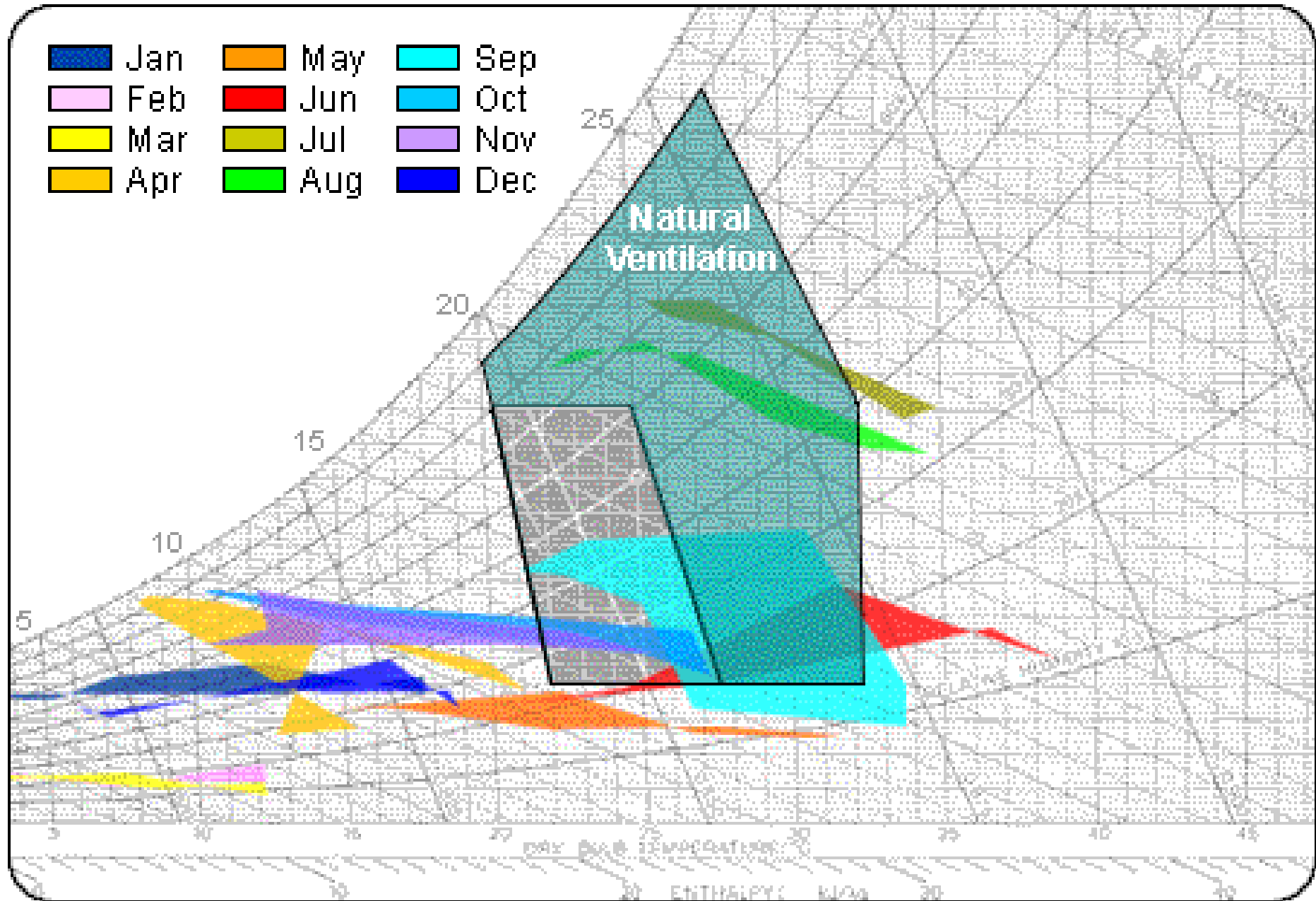


# Thermal comfort predicted mean vote (PMV) contours



(Source: <http://andrewmarsh.com/software/psychro-chart-web/>)

# Analysis of external climate on cooling & ventilation strategies



# Example of how plotted data on a psychrometric chart can be studied, and related to passive design (using Climate Consultant\*)

## PSYCHROMETRIC CHART ASHRAE Standard 55

LOCATION: Climate Zone 3, CA, USA  
 Latitude/Longitude: 37.7° North, 122.2° West, Time Zone from Greenwich -8  
 Data Source: WYEC2-C-00003 724930 WMO Station Number. Elevation 6 ft

### LEGEND

COMFORT INDOORS  
 100% COMFORTABLE  
 0% NOT COMFORTABLE

### DESIGN STRATEGIES: JANUARY through DECEMBER

- 9.5% 1 Comfort(829 hrs)
- 2.0% 2 Sun Shading of Windows(256 hrs)
- 0.7% 3 High Thermal Mass(61 hrs)
- 4 High Thermal Mass Night Flushed(0 hrs)
- 5 Direct Evaporative Cooling(0 hrs)
- 6 Two-Stage Evaporative Cooling(0 hrs)
- 7 Natural Ventilation Cooling(0 hrs)
- 8 Fan-Forced Ventilation Cooling(0 hrs)
- 50.2% 9 Internal Heat Gain(4400 hrs)
- 10 Passive Solar Direct Gain Low Mass(0 hrs)
- 19.2% 11 Passive Solar Direct Gain High Mass(1680 hrs)
- 0.1% 12 Wind Protection of Outdoor Spaces(11 hrs)
- 13 Humidification Only(0 hrs)
- 0.6% 14 Dehumidification Only(56 hrs)
- 0.3% 15 Cooling, add Dehumidification if needed(22 hrs)
- 30.4% 16 Heating, add Humidification if needed(2662 hrs)

100.0% Comfortable Hours using Selected Strategies  
 (8760 out of 8760 hrs)

Comfort Zones show:  
 Summer clothing on right,  
 Winter clothing on left.

PLOT: COMFORT\_INDOORS

Hourly  Daily Min/Max

All Hours  Selected Hours

1 a.m. through midnight

All Months  Selected Months

JAN through DEC

One Month JAN Next Month

One Day 1 Next Day

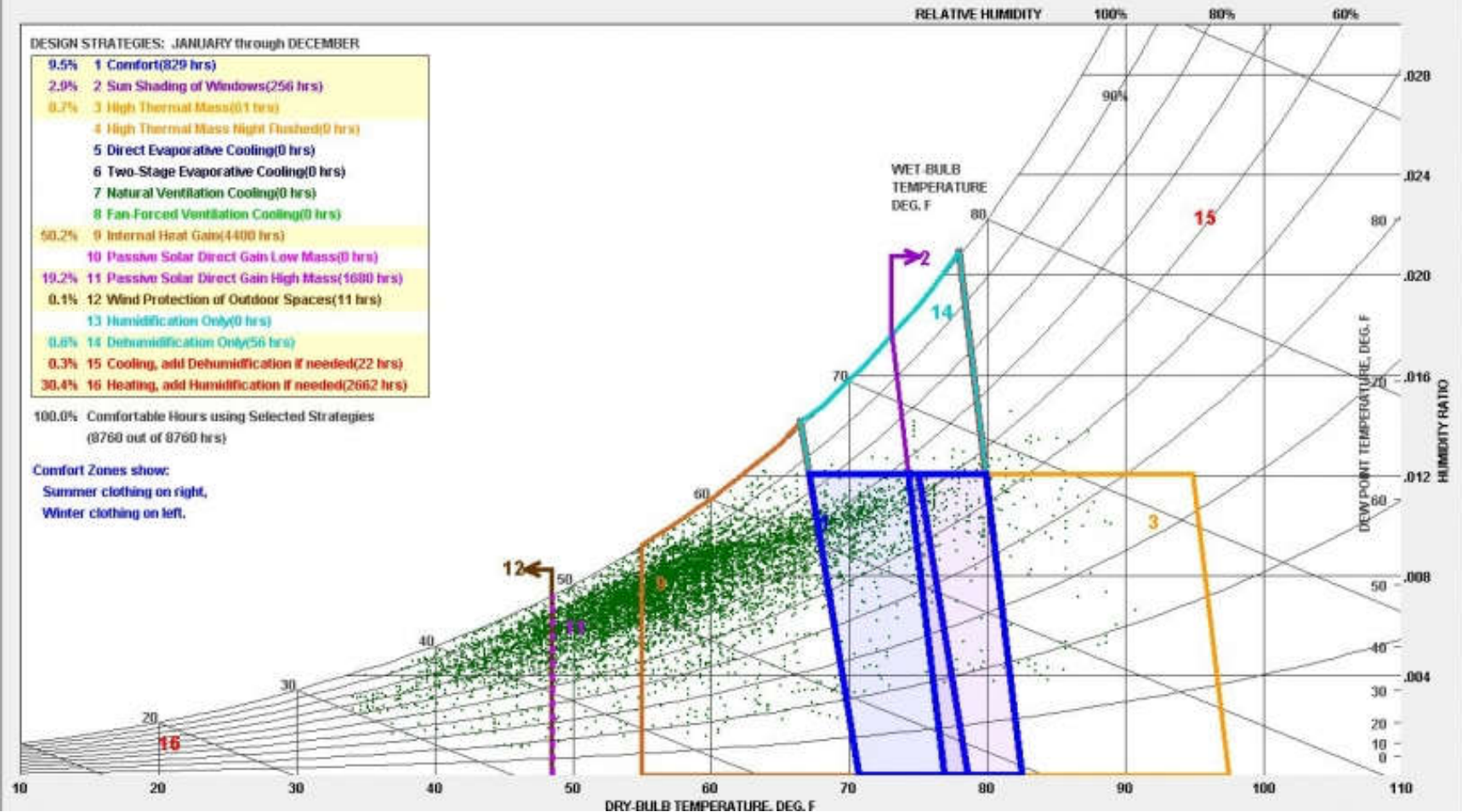
One Hour 1 a.m. Next Hour

TEMPERATURE RANGE:

10 to 110 °F  Fit to Data

Display Design Strategies

Show Best set of Design Strategies



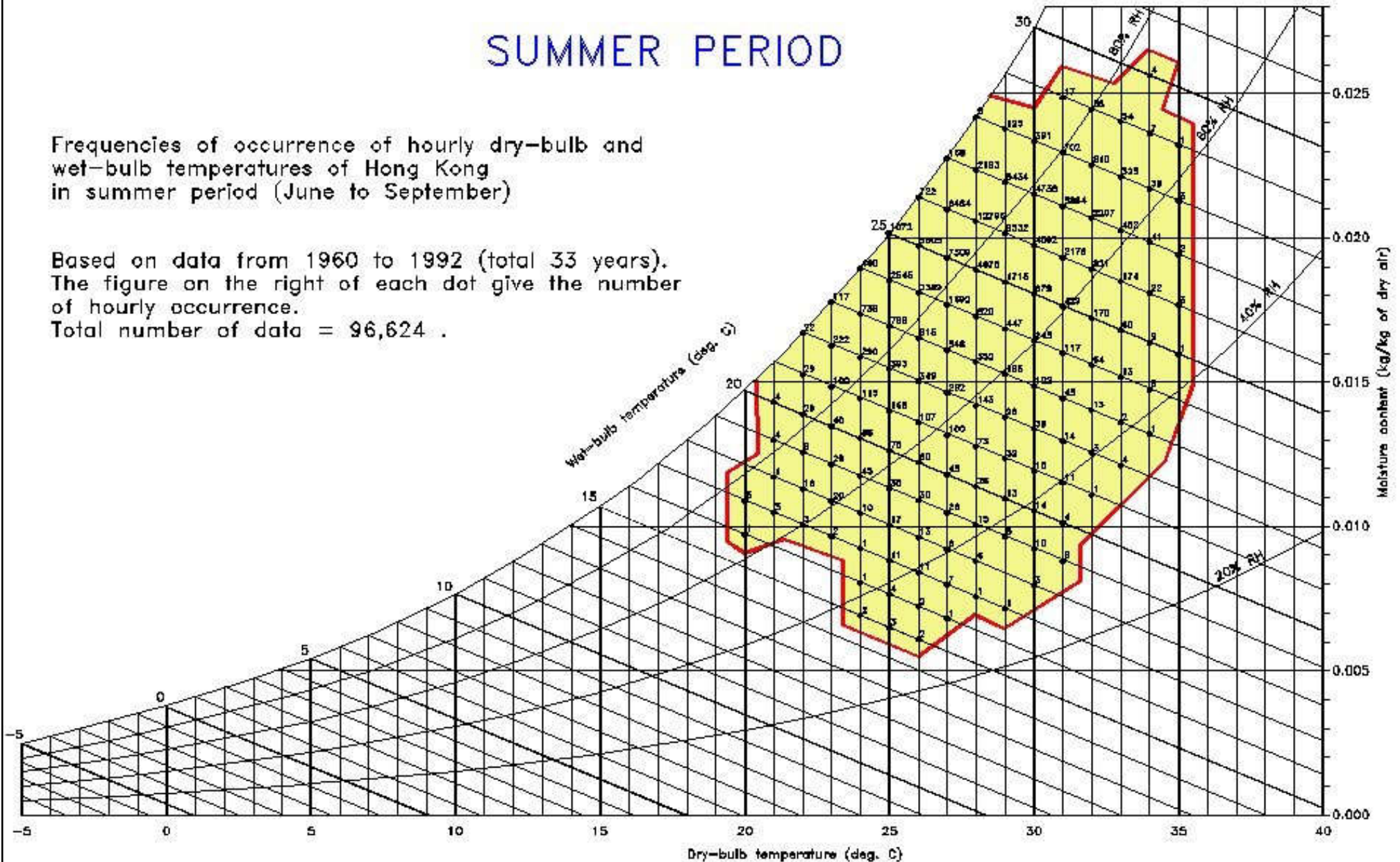
(\*Climate Consultant <http://www.energy-design-tools.aud.ucla.edu/>)

# Analysis of weather conditions in Hong Kong

## SUMMER PERIOD

Frequencies of occurrence of hourly dry-bulb and wet-bulb temperatures of Hong Kong in summer period (June to September)

Based on data from 1960 to 1992 (total 33 years).  
The figure on the right of each dot give the number of hourly occurrence.  
Total number of data = 96,624 .

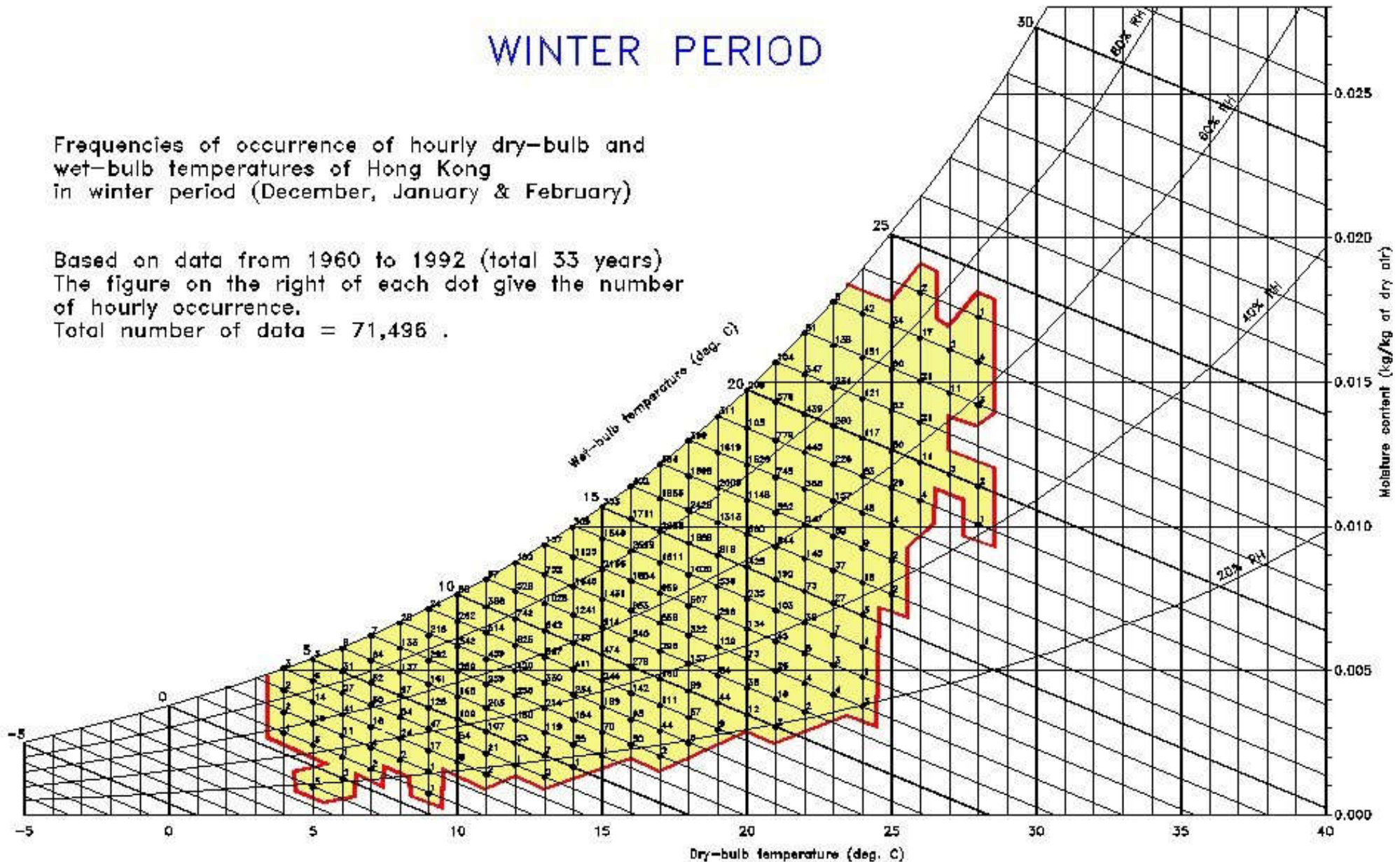


# Analysis of weather conditions in Hong Kong

## WINTER PERIOD

Frequencies of occurrence of hourly dry-bulb and wet-bulb temperatures of Hong Kong in winter period (December, January & February)

Based on data from 1960 to 1992 (total 33 years)  
The figure on the right of each dot give the number of hourly occurrence.  
Total number of data = 71,496 .

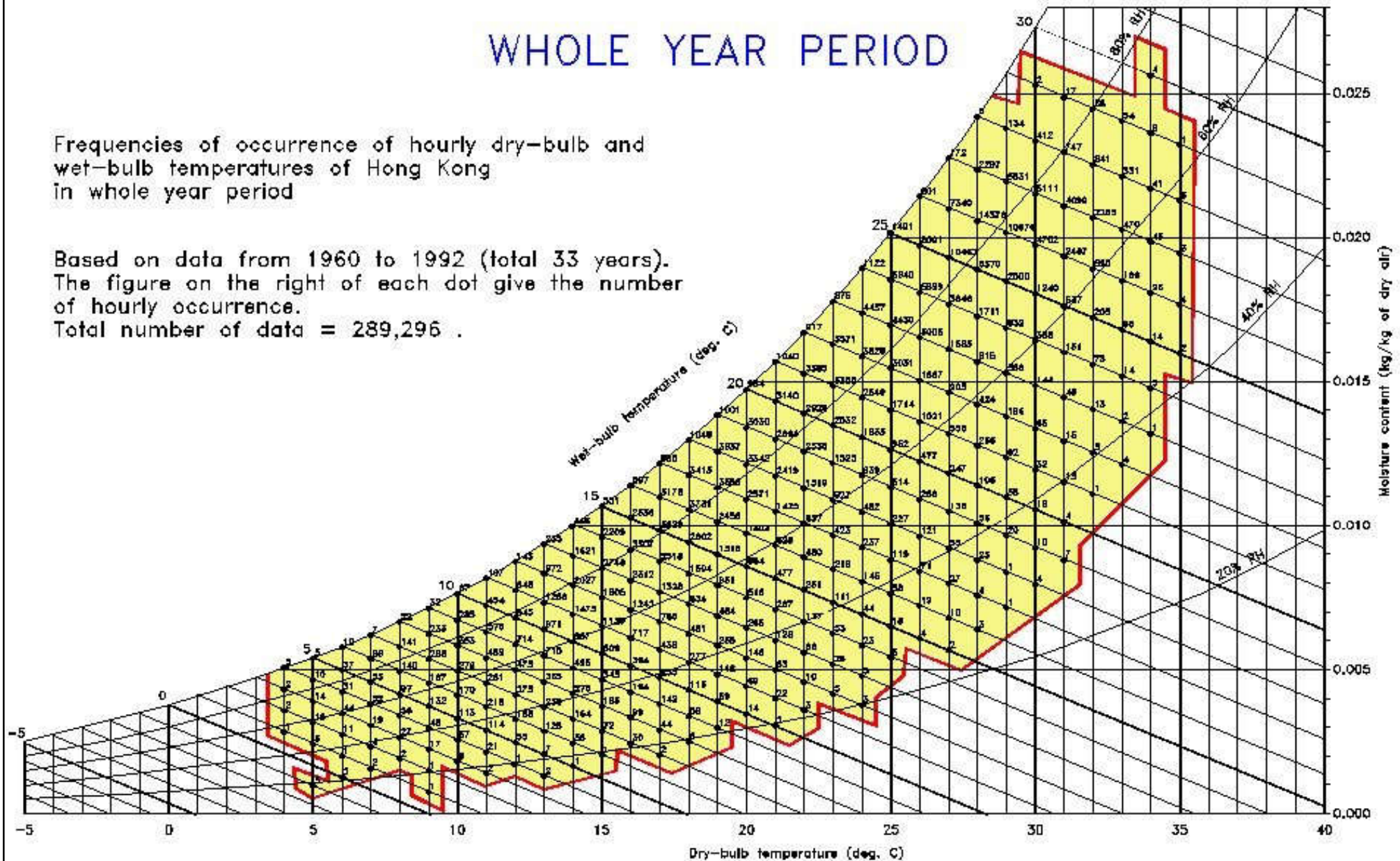


# Analysis of weather conditions in Hong Kong

## WHOLE YEAR PERIOD

Frequencies of occurrence of hourly dry-bulb and wet-bulb temperatures of Hong Kong in whole year period

Based on data from 1960 to 1992 (total 33 years).  
The figure on the right of each dot give the number of hourly occurrence.  
Total number of data = 289,296 .



# Analysis of weather conditions in Hong Kong



ASHRAE PSYCHROMETRIC CHART NO.1

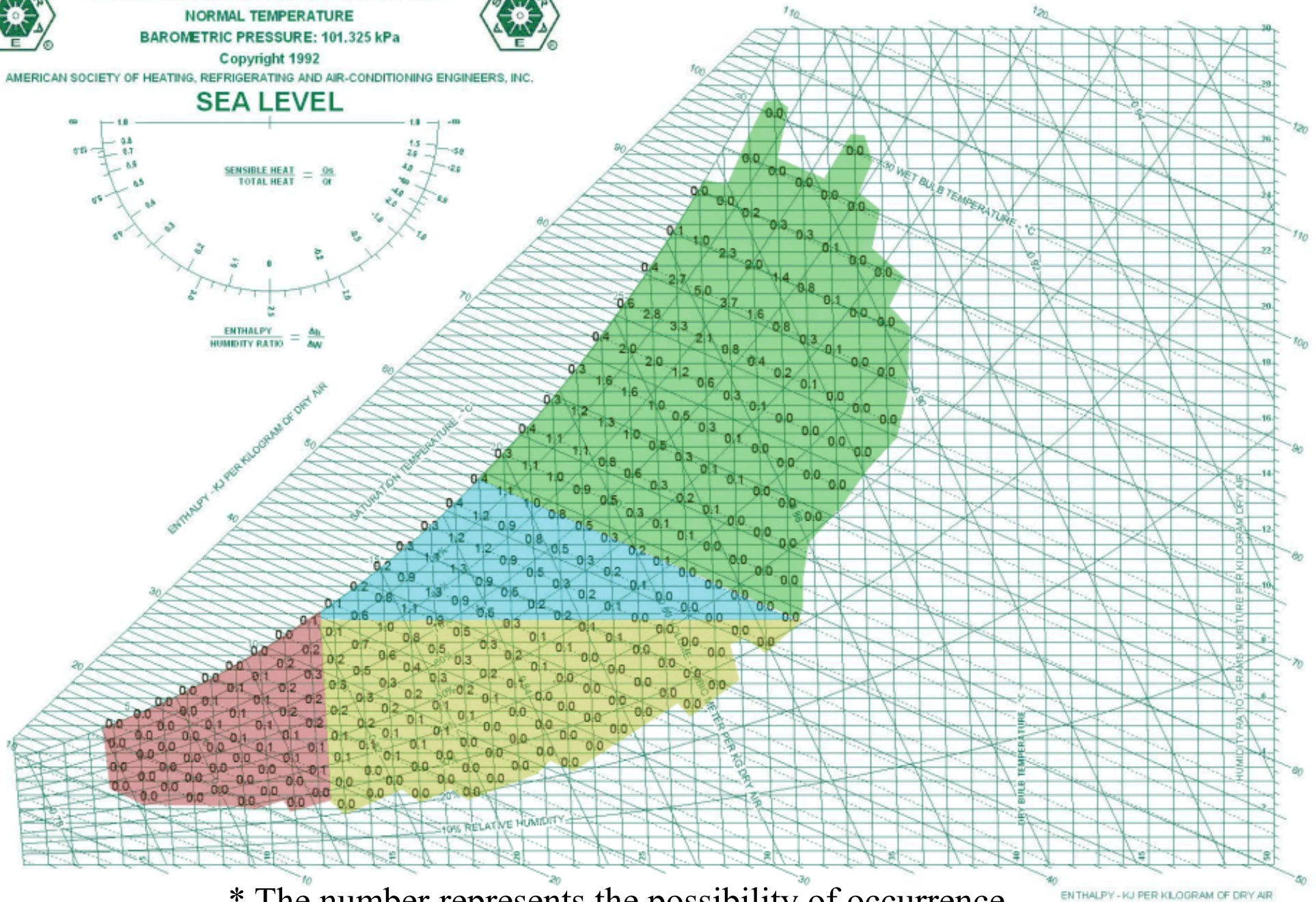
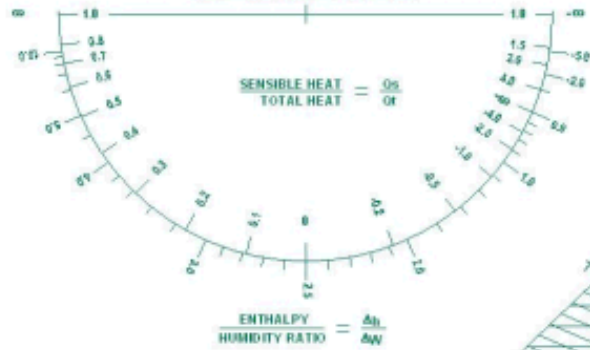
NORMAL TEMPERATURE

BAROMETRIC PRESSURE: 101.325 kPa

Copyright 1992

AMERICAN SOCIETY OF HEATING, REFRIGERATING AND AIR-CONDITIONING ENGINEERS, INC.

SEA LEVEL



\* The number represents the possibility of occurrence.



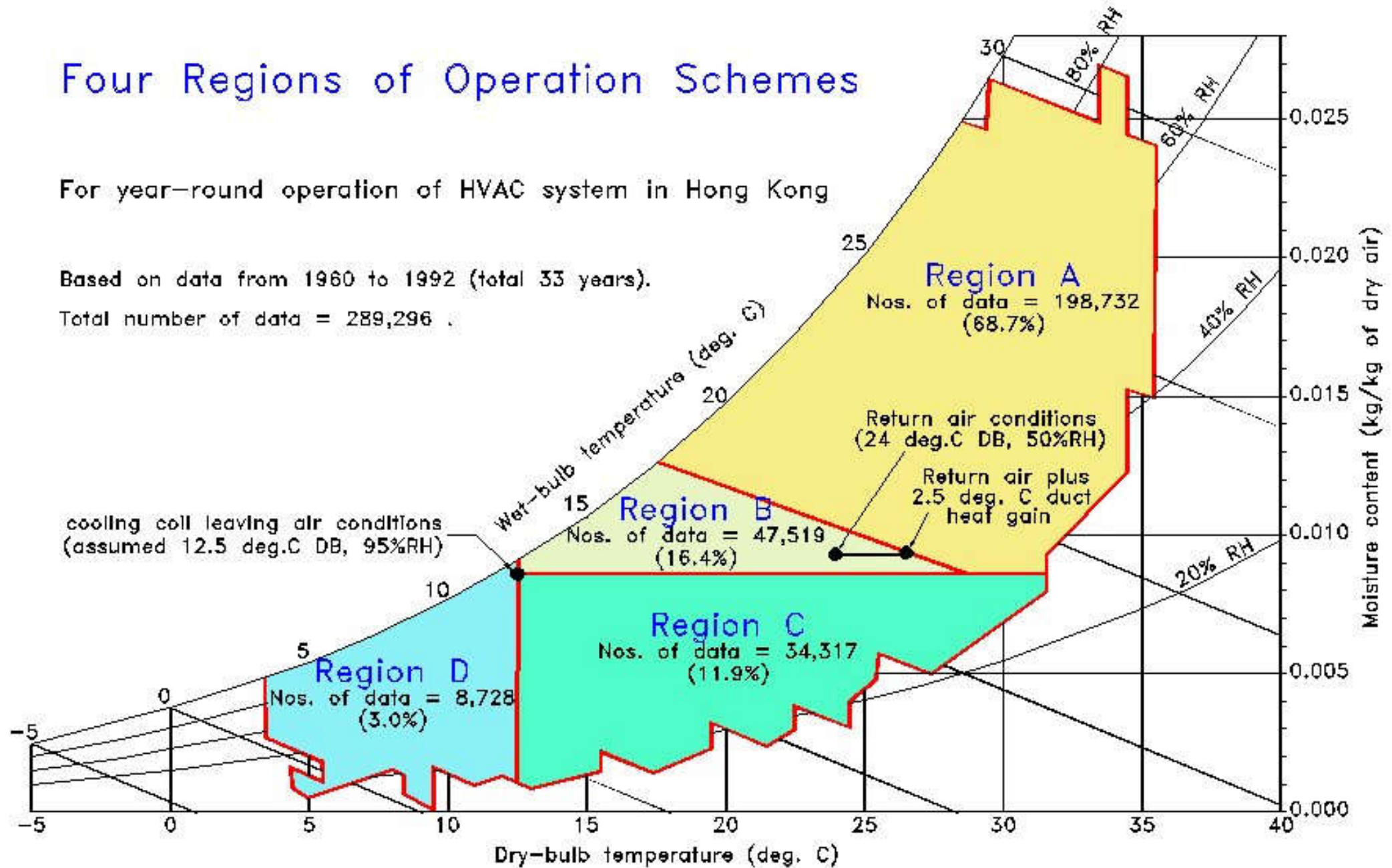
# Analysis of HVAC operation strategy

## Four Regions of Operation Schemes

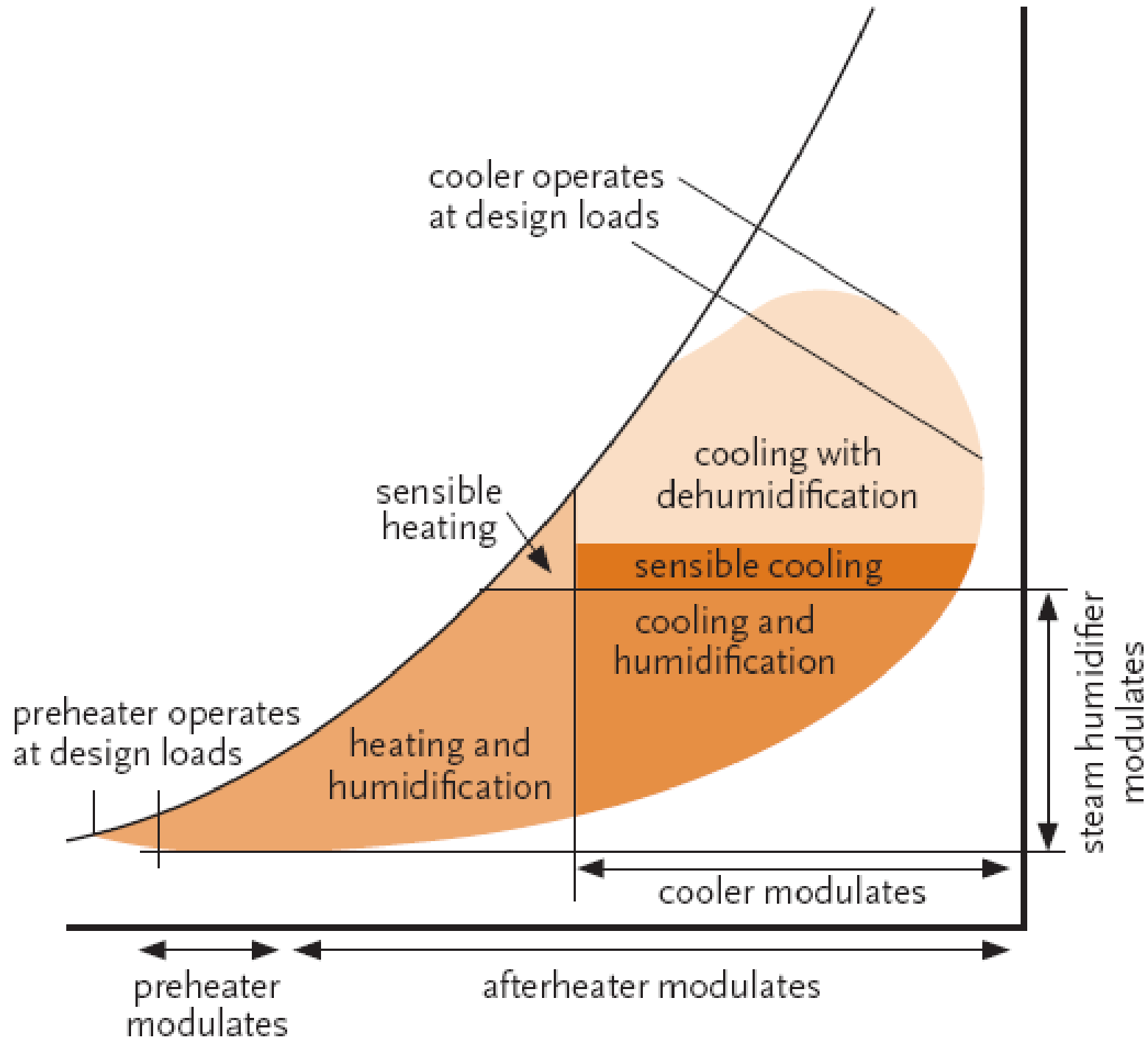
For year-round operation of HVAC system in Hong Kong

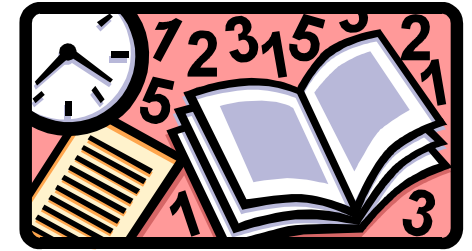
Based on data from 1960 to 1992 (total 33 years).

Total number of data = 289,296 .



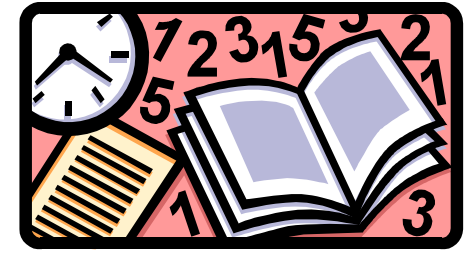
# All-year-round operating regime based on outdoor conditions





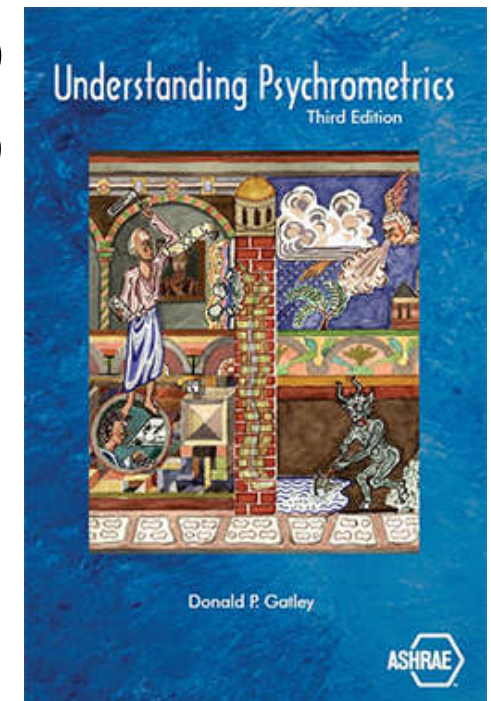
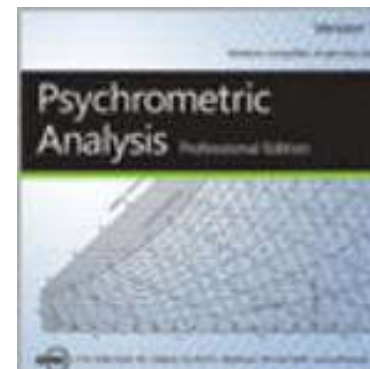
# Further Reading

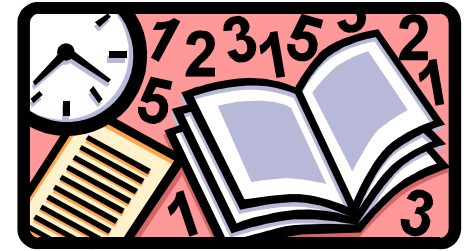
- Why Learn Psychrometrics? (by Donald P. Gatley)
  - <https://www.ashrae.org/news/ashraejournal/why-learn-psychrometrics>
- CIBSE Journal CPD modules: <http://www.cibsejournal.com/cpd/>
  - Module 3: The properties of air  
<https://www.cibsejournal.com/cpd/modules/2009-04/>
  - Module 7: Applying the psychrometric relationships  
<https://www.cibsejournal.com/cpd/modules/2009-08/>
  - Module 9: The basic psychrometric processes  
<https://www.cibsejournal.com/cpd/modules/2009-10/>
  - Module 11: The psychrometrics of HVAC sub-systems  
<https://www.cibsejournal.com/cpd/modules/2009-12/>
  - Module 14: The psychrometrics of air conditioning systems  
<https://www.cibsejournal.com/cpd/modules/2010-03/>
  - Module 23: Travelling into time with psychrometry  
<https://www.cibsejournal.com/cpd/modules/2010-12/>



# References

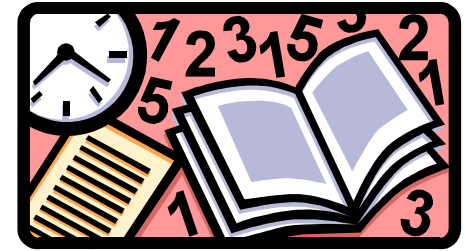
- ASHRAE Psychrometrics Tools
  - [www.ashrae.org/resources--publications/bookstore/psychrometrics](http://www.ashrae.org/resources--publications/bookstore/psychrometrics)
  - Psychrometric Chart Mobile App (on iPad)
    - Video: ASHRAE HVAC Psychrometric Chart App (8:11)  
<https://youtu.be/VFFqkBHDqPk>
  - Psychrometric Analysis CD, Version 7 (2012)
  - Understanding Psychrometrics, 3rd ed. (2013)





# References

- Understanding Psychrometrics, 3rd ed. (2013)
  - Supplemental Files <http://www.ashrae.org/UP3>
    - 25 ASHRAE psychrometric charts and three 0°C to 400°C 0-1.0 humidity ratio charts for 5.53, 101.325, and 2000 kPa
    - LibHuAirProp Add-In Demo
    - HW.exe (to generate a table of 1983 Hyland-Wexler psychrometric properties)



# References

- NPTEL E-learning course -- Refrigeration and Air Conditioning <http://nptel.ac.in/courses/112105129/>
  - Lesson 28 Psychrometric Processes
  - Lesson 30 Psychrometry Of Air Conditioning Systems
- Gatley, D. P., 2013. *Understanding Psychrometrics*, 3rd ed., American Society of Heating, Refrigerating, and Air-Conditioning Engineers, Atlanta, GA.  
<https://azaranstore.com/download/articles/157%20Psychrometrics%20ASHRAE.pdf>
- Gatley D. P., 2004. Psychrometric chart celebrate 100th anniversary, *ASHRAE Journal*, 46 (11) 16-20.  
<http://www.handsdownsoftware.com/Psychrometrics-100th-Bday.pdf>
- Sherif, S. A., 2002. Overview of psychrometrics, *ASHRAE Journal*, 44 (7) 33-39. [http://www.handsdownsoftware.com/Overview\\_of\\_Psychrometrics.pdf](http://www.handsdownsoftware.com/Overview_of_Psychrometrics.pdf)