

# Lighting Calculations



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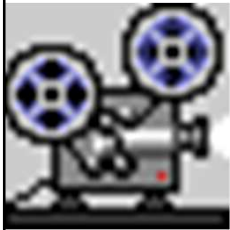
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- Design Considerations
- Typical Calculations
- Lumen Method
- Point-by-point Method
- Other Calculations
- Outdoor Lighting

# Design Considerations



- Video: Lighting Calculations (5:51)



- <http://www.youtube.com/watch?v=sfbXx13JgeU>
- Basic lighting calculations that are required to carry out a lighting design
  - Luminous flux, luminous intensity, illuminance, luminance, colour rendering, colour temperature
  - Glare, working plane, surface reflectances
  - Indoor lighting: calculations are done for both the direct and inter-reflected light; room geometry; maintenance
  - Outdoor lighting: light falls directly on the working plane



# Design Considerations

- Lighting design checklist
  - Safety (e.g. emergency escape lighting)
  - Task requirements
    - Lighting scheme to provide suitable quantity and direction for the task; colour rendering; glare problems
  - Lighting appearance
    - Architecture/Interior design
  - Energy efficiency
    - Lighting equipment, controls, daylighting



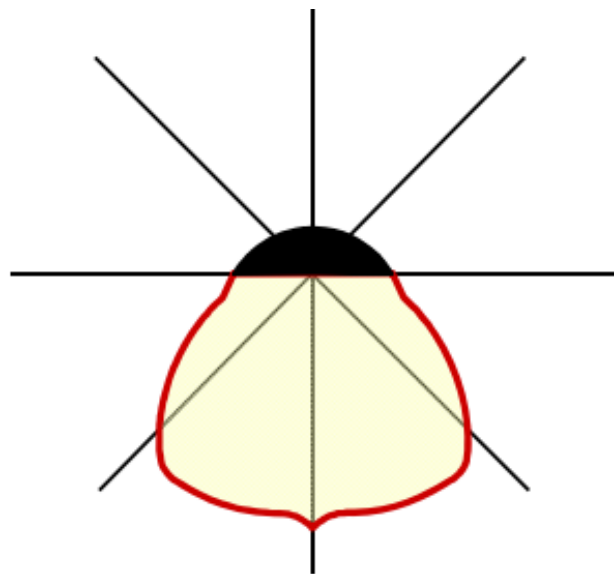
# Design Considerations

- Lighting equipment checklist
  - Lamps
    - Operating characteristics, lamp size/shape, colour
  - Luminaires
    - Size and shape, light distribution, glare control, ballast
    - Operating environment (e.g. corrosive, dusty)
  - Lighting controls
    - Manual switches, time switches, dimming, daylight-linked controls, occupant sensing

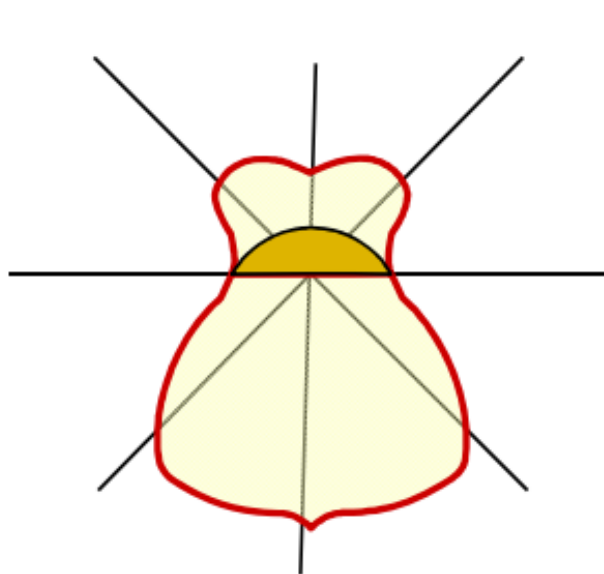
(Examples of the impact on lighting with differing techniques of lighting distribution inside interior spaces:

<http://iarc.uncg.edu/elight/learn/design/la.html>)

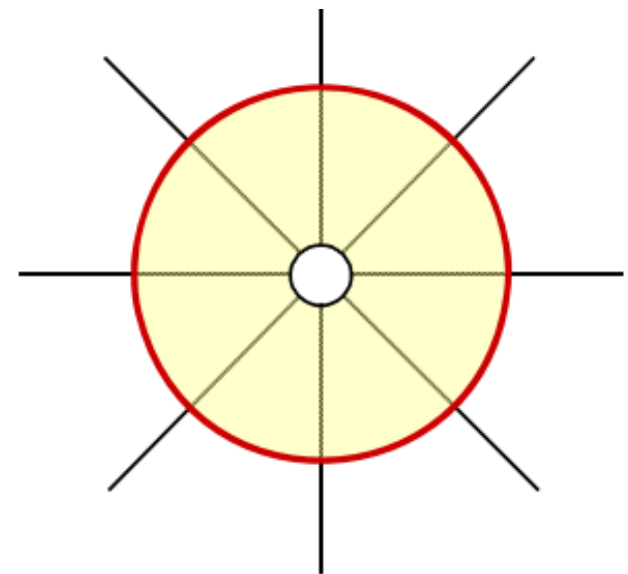
# CIE luminaire types and their light distributions



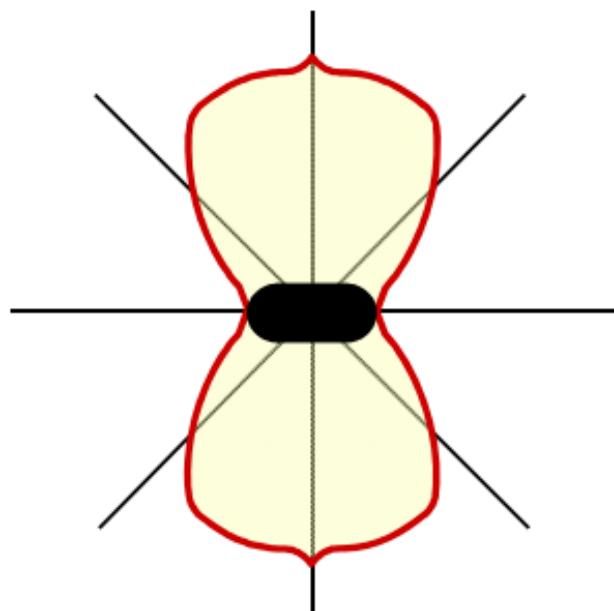
Direct



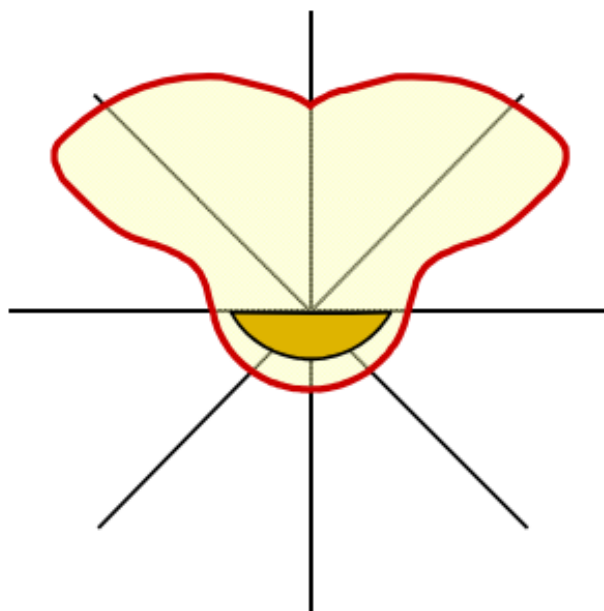
Semi-Direct



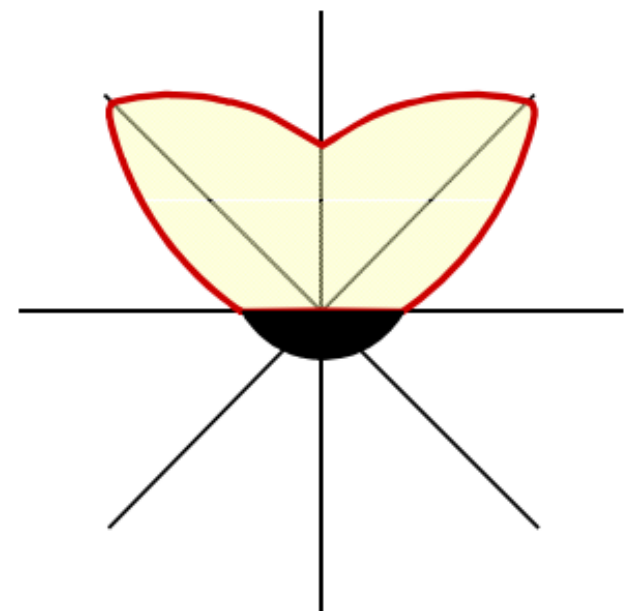
General Diffuse



(IES) Direct-Indirect



Semi-Indirect

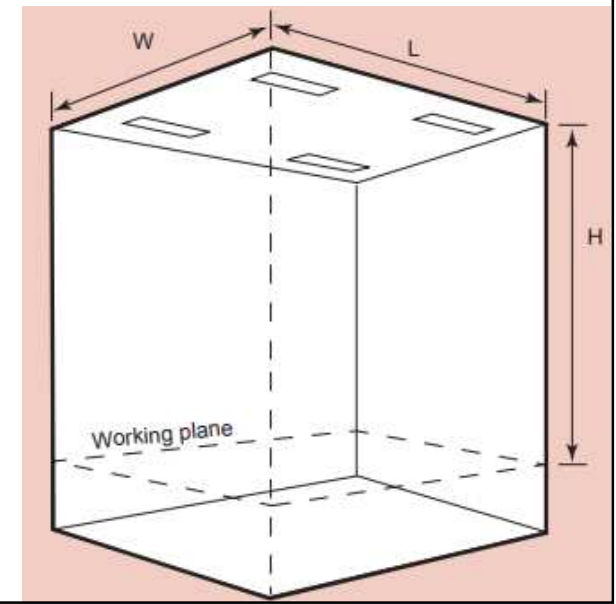


Indirect

# Design Considerations

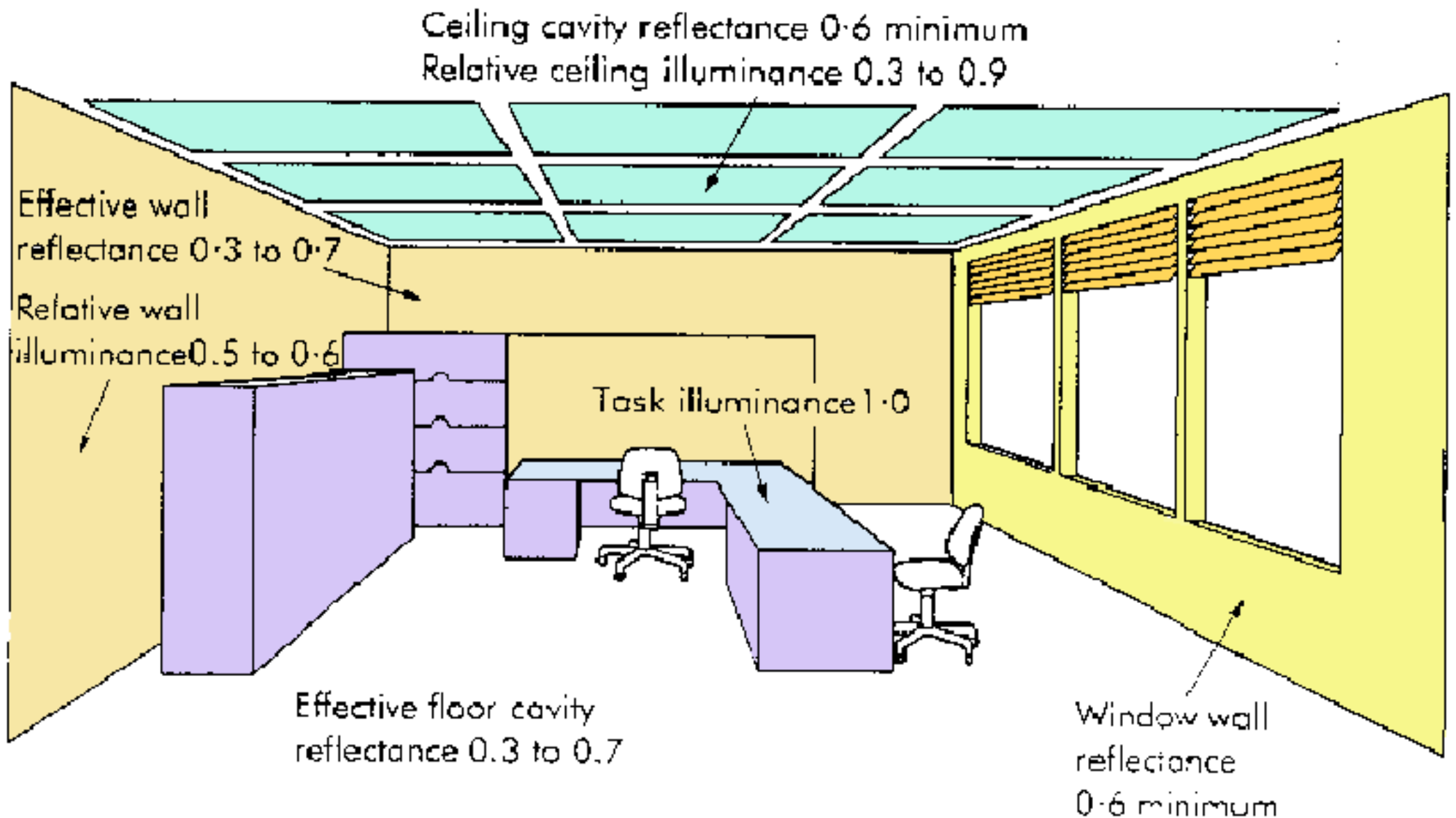


- Collect information for lighting design
  - Room details:
    - Room size (length, width, height)
    - Horizontal working plane height above floor level
    - Room surface reflectance (ceiling, walls, floor)
    - Window size/s and position
    - Room index
      - $K = (L \times W) / (L + W) H$
    - Cleanliness of the room/environment
    - The regularity of the cleaning



# Recommended room reflectances & illuminance ratios

[Source: CIBSE Lighting Code]







# Design Considerations

- Collect information for lighting design (cont'd)
  - Task details:
    - Type of task/application (e.g. office, industrial, retail)
    - Task position (e.g. horizontal/vertical, general/local)
    - Special task lighting requirement (e.g. critical inspection, computer use, disabled persons)
    - Special hazards (e.g. wet or dusty environment, rotating machines) --- luminaire thermal and mechanical protection



# Design Considerations

- Collect information for lighting design (cont'd)
  - Task lighting requirements:
    - Task illuminance (lux)
    - Task illuminance uniformity (e.g. uniform (0.8), non-uniform (as appropriate))
    - Light colour rendering quality and index (Ra)
    - Average installed power density target ( $\text{W/m}^2$ ), to meet building energy code
    - Light pollution, sustainable lighting design

# Design Considerations



- Collect information for lighting design (cont'd)
  - Room lighting requirements:
    - Accent lighting (e.g. display lighting, decorative lighting)
    - Wall lighting (e.g. display lighting, lighting to create room lightness)
    - Ceiling lighting (e.g. lighting to create room lightness)
    - Light colour appearance (e.g. warm, intermediate, cool)
    - Emergency and/or escape lighting requirement

(Examples of the impact on lighting with differing layers of lighting, and material properties of surfaces inside interior spaces:

<http://iarc.uncg.edu/elight/learn/determine/la.html>)



# Typical Calculations

- To calculate the amount of light that will result from a design
  - Critical for commercial & institutional buildings
  - Seldom required for residential design
- Basic considerations
  - Light sources (lamp lumens)
  - Luminaires & light distribution
  - Initial vs. maintained light levels (as lamps age and luminaires get dirty, light level drops)



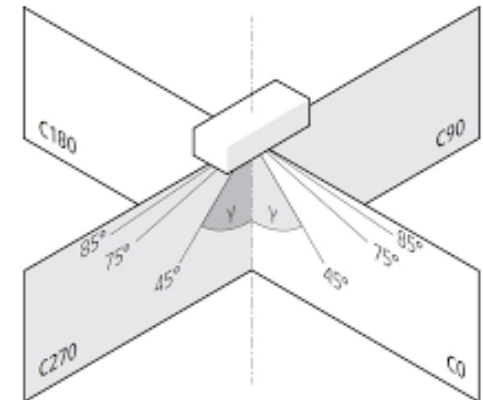
# Typical Calculations

- Design calculations for simple situations
  - The number and layout of luminaires needed for general lighting
  - What additional luminaires are needed to provide local emphasis or accents
  - Energy efficiency of the installation and financial benefits
- Calculation methods:
  - Manual, data sheets/tables, graphical, spreadsheet, computer software

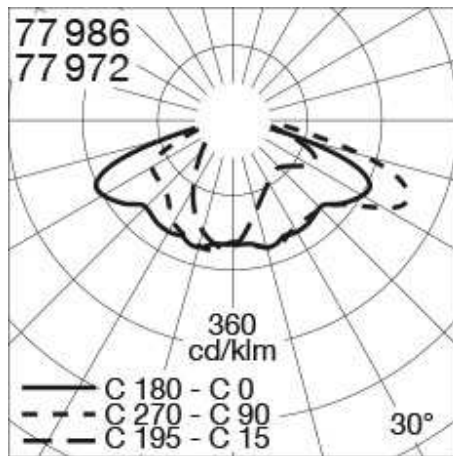


# Typical Calculations

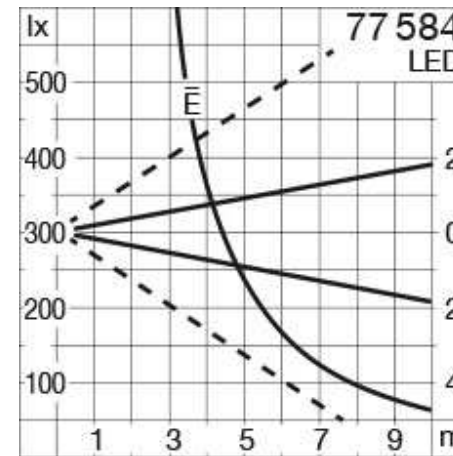
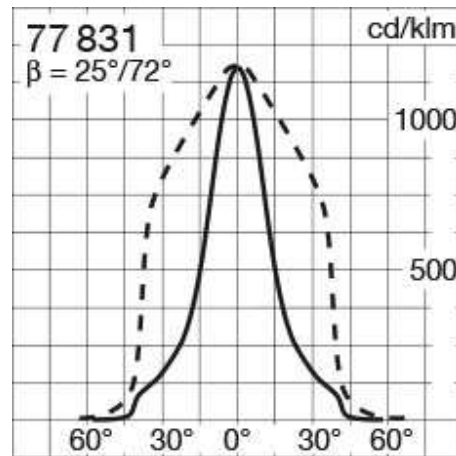
- Determine illuminance level
  - Horizontal (most common)
    - Average illumination on the work plane (lux)
      - Sitting 0.75 to 0.9 m; Standing 0.85 to 1.2m
  - Vertical (e.g. on wall surface)
  - Inclined
- Analyse light distribution
  - Using light distribution curves, illumination and isolux diagrams
    - Illuminance (lux) or luminance ( $\text{cd/m}^2$ )



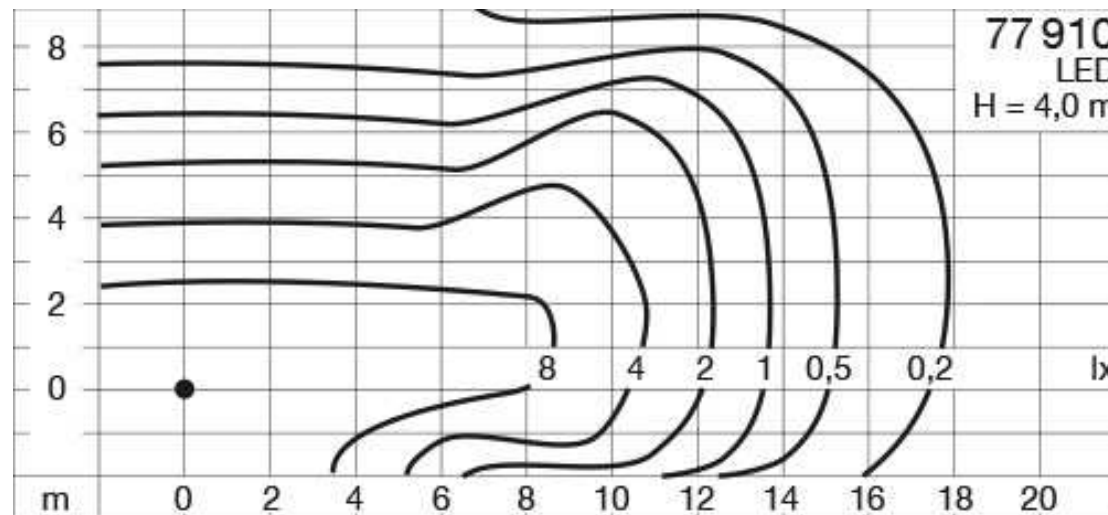
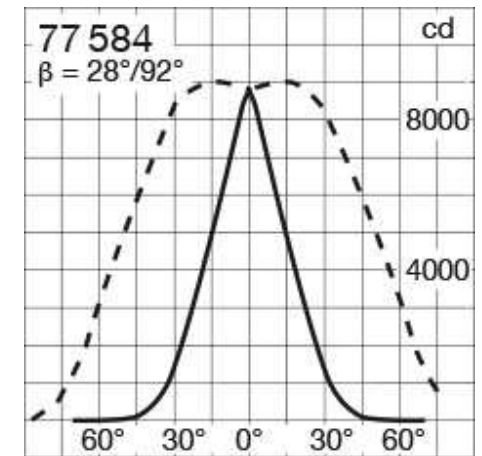
# Light distribution curves, illumination and isolux diagrams\*



Light distribution curves



Illumination diagrams

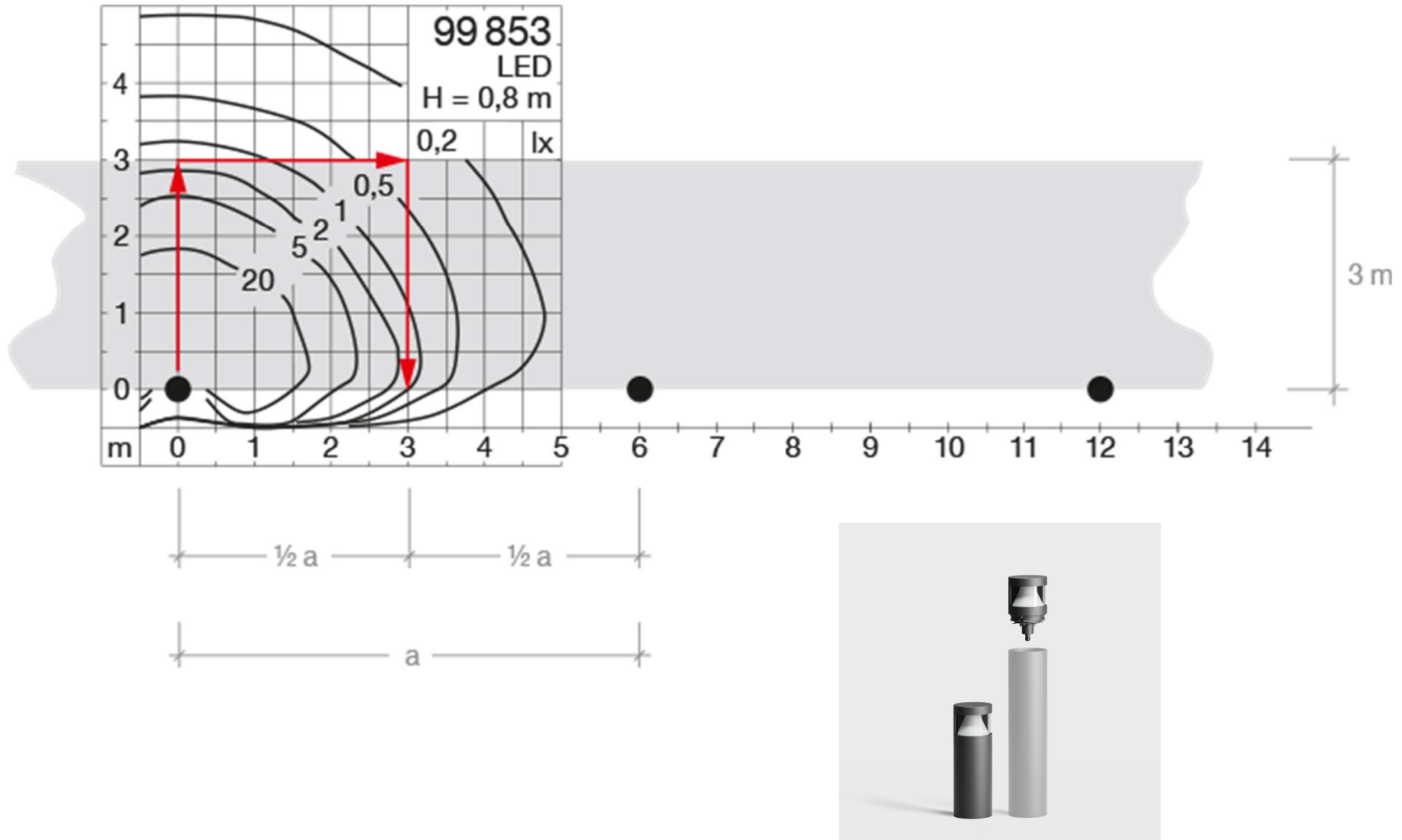


Isolux diagrams

(\* See also: <http://www.bega.de/en/knowledge/about-light-and-illumination/2-information-about-light-and-illumination/2-06-light-distribution-curves-illumination-and-isolux-diagrams/>)



# Example: Determination of the luminaire spacing $a$ for pathway illumination of $E_{\min} = 1 \text{ lx}$ on the basis of the isolux diagram



(\* See also: <http://www.bega.de/en/knowledge/about-light-and-illumination/2-information-about-light-and-illumination/2-06-light-distribution-curves-illumination-and-isolux-diagrams/>)





# Typical Calculations

- Predict general & ambient light levels
  - Rough estimation based on a [Watts/sq.m method](#)
    - Not very accurate, but good for prelim. planning
  - [Lumen method](#) calculations (light flux method)
    - Determines average illuminance in large open areas
    - Good for general lighting
  - [Point-by-point](#) computer calculations
    - Determines light levels at a specific point on an object or surface; complicated, start from fundamental laws
    - Can be used for outdoor lighting

## Rough estimation based on a Watts/sq.m method

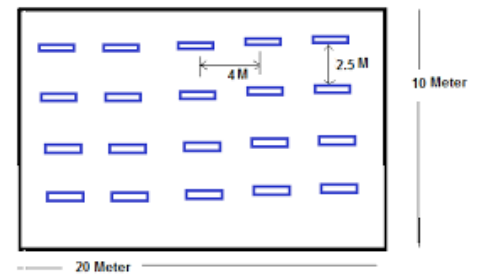
<b>Average light level desired &amp; typical application</b>	<b>Watts/sq.m of fluorescent, CFL or HID lights</b>	<b>Watts/sq.m of incandescent or halogen lamps</b>
25-50 lux Hotel corridors, stair towers	1-2	3-7
50-100 lux Office corridors, parking garages, theatres (house lights)	2-4	7-10
100-200 lux Building lobbies, waiting areas, malls, hotel function spaces	4-8	10-20
200-500 lux Office areas, classrooms, lecture halls, conference rooms, ambient retail lighting, workshops	15-25	Not recommended
500-1000 lux Grocery stores, laboratories, work areas, big box retail stores	12-20	Not recommended

[Source: Adapted from Karlen and Benya, 2004. *Lighting Design Basics*]



# Typical Calculations

- Predict task lighting & focal lighting levels
  - Difficult to predict accurately
  - Methods commonly used
    - Use data/guide of the luminaire's manufacturer
    - Use the inverse-square law to estimate
    - Use a display lighting software program

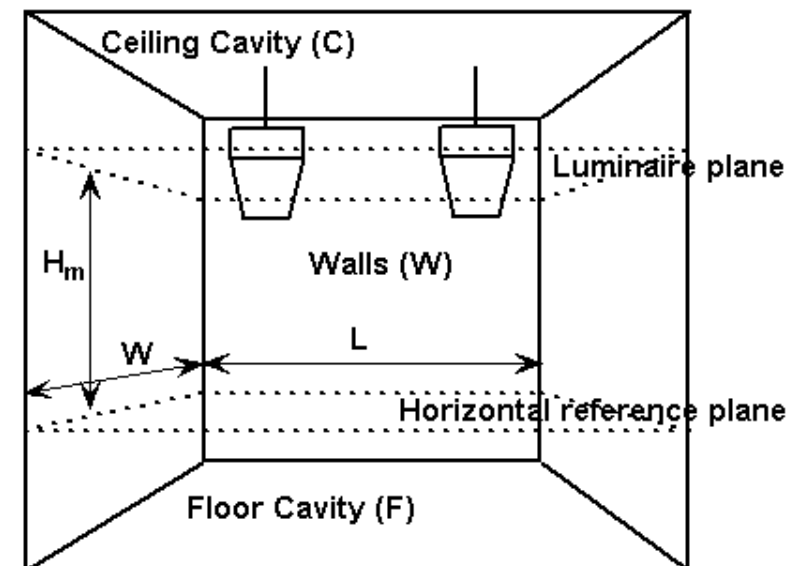


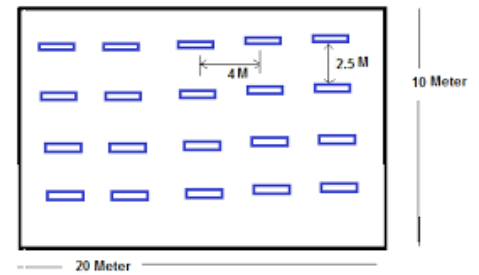
# Lumen Method

- Lumen Method: average illuminance ( $E$ ) is

$$E = \frac{F \times n \times N \times UF \times MF}{A}$$

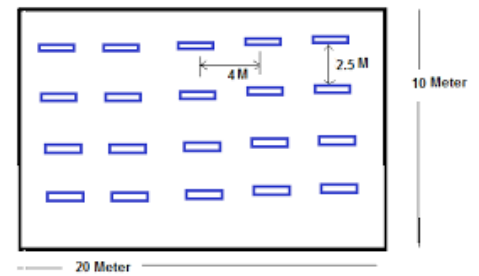
- $F$  = initial bare lamp luminous flux (lumens)
- $n$  = number of lamps per luminaire
- $N$  = number of luminaires
- $UF$  = utilisation factor
- $MF$  = maintenance factor
- $A$  = area of the surface ( $\text{m}^2$ )





# Lumen Method

- **Room index (K):** a measure of the proportions of the room, for rectangular room
  - $K = (L \times W) / (L + W) h_m$ 
    - $L$  = length of the room
    - $W$  = width of the room
    - $h_m$  = height of luminaire above horiz. reference plane
- **Effective reflectances of ceiling, walls & floor**
  - Cavity index (CI) =  $(L \times W) / (L + W) h = K \times h_m / h$ 
    - $h$  = depth of the cavity (ceiling or floor)
  - Determine effective reflectance from tables or formulae (see examples in *CIBSE* or *SLL Lighting Code*)

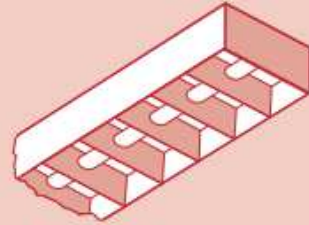


# Lumen Method

- Utilisation factor ( $UF$ )
  - Ratio of total flux received by the surface to the total lamp flux of the installation
    - Indicates the effectiveness of the lighting scheme
  - $UF$  depends upon: the efficiency of luminaire, luminaire distribution, geometry of the space, room reflectance, polar curve
  - Usually,  $UF$  tables are prepared for general lighting with regular arrays of luminaires, for 3 main room surfaces: ceiling cavity, walls, and floor cavity or horizontal reference plane

# Example of luminaire photometric data and utilisation factor

Luminaire type: single 1.5 m, 58 W fluorescent lamp fitting, incorporating a white louvre attachment.



*Illustration of luminaire*



*Luminous Intensity Distributions  
(polar curves) – axial (A) and transverse (T)*

Light output ratio: upward – 0.0; downward – 0.55; total – 0.55.

Spacing/height ratio: nominal – 1.5; maximum (square) – 1.7, maximum (continuous) – 2.0.

Room index	0.75	1.0	1.25	1.5	2.0	2.5	3.0	4.0	5.0
Room reflectances C W F									
70 - 50 - 20	0.36	0.42	0.47	0.51	0.56	0.60	0.63	0.66	0.69
30	0.31	0.36	0.42	0.46	0.52	0.56	0.59	0.63	0.66
10	0.27	0.32	0.37	0.41	0.47	0.52	0.55	0.60	0.63
50 - 50 - 20	0.33	0.38	0.43	0.46	0.51	0.54	0.57	0.60	0.62
30	0.29	0.34	0.38	0.42	0.51	0.51	0.53	0.57	0.59
10	0.25	0.30	0.35	0.38	0.44	0.48	0.50	0.54	0.57
30 - 50 - 20	0.31	0.35	0.39	0.42	0.46	0.49	0.51	0.54	0.55
30	0.27	0.31	0.35	0.38	0.43	0.46	0.48	0.52	0.54
10	0.23	0.28	0.32	0.35	0.40	0.44	0.46	0.50	0.52
0 - 0 - 0	0.20	0.24	0.28	0.30	0.34	0.37	0.39	0.42	0.44

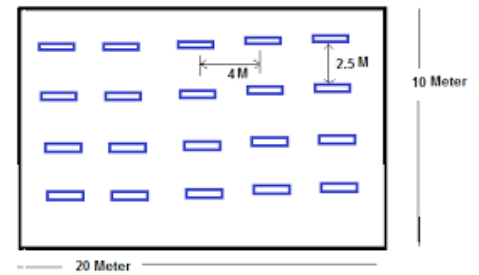
## Using the table

Calculate the room index – see section 4, page 15

Decide on the appropriate reflection factors for ceiling (C), walls (W) and floor (F) – see section 4, page 15

Locate utilisation factor at intersection of appropriate column and row





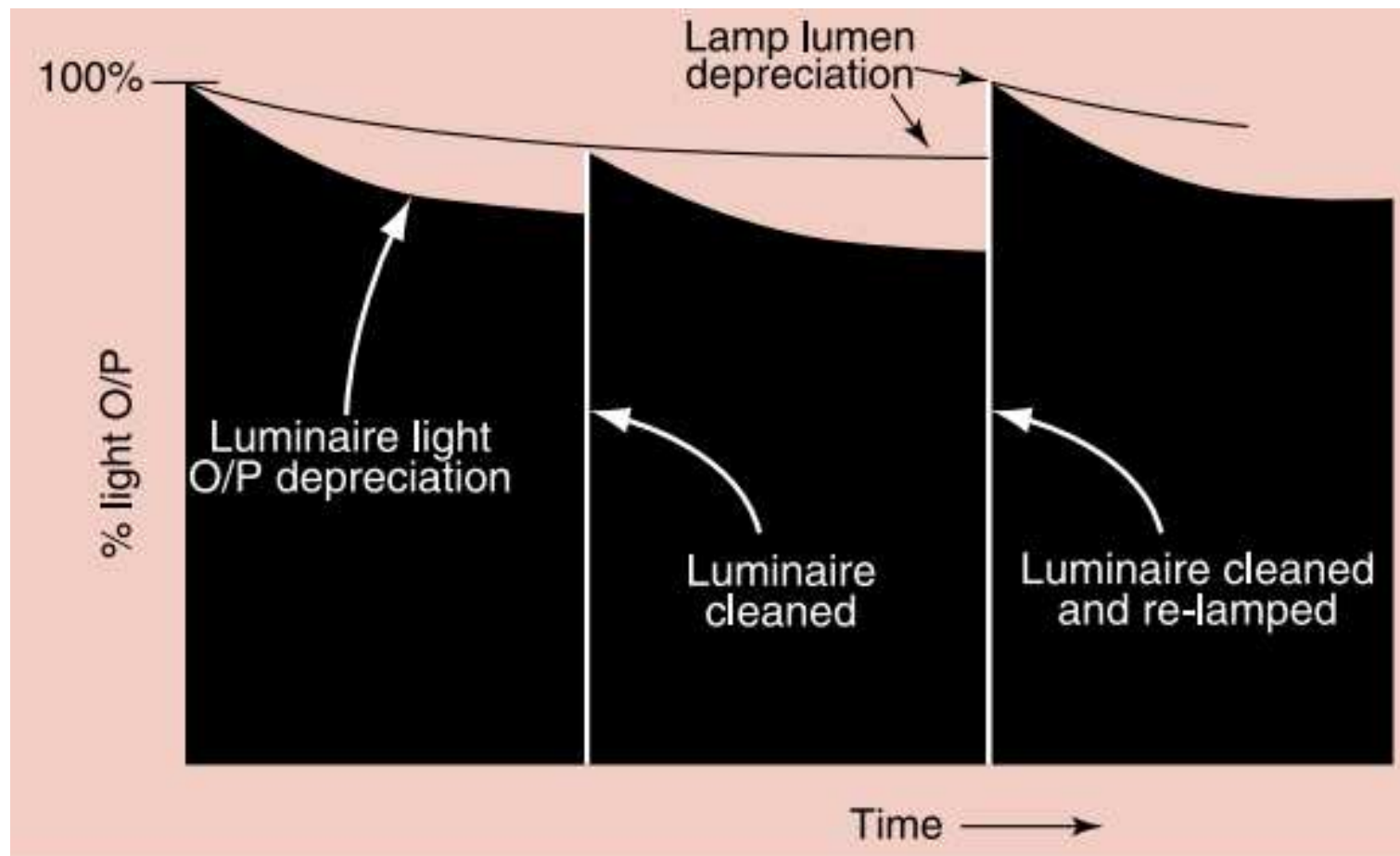
# Lumen Method

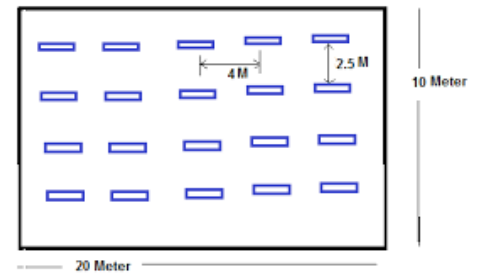
- Maintenance factor ( $MF$ )
  - Ratio of maintained illuminance to initial illuminance (losses for lamp lumen maintenance)
  - $MF = LLMF \times LSF \times LMF \times RSMF$ 
    - Lamp lumen maintenance factor (LLMF)
    - Lamp survival factor (LSF)
    - Luminaire maintenance factor (LMF)
    - Room surface maintenance factor (RSMF)
  - See *CIBSE/SLL Code of Lighting* for description



# Maintenance factor and light depreciation

Environmental condition	Maintenance factor
Clean	0.9
Average	0.8
Dirty	0.7





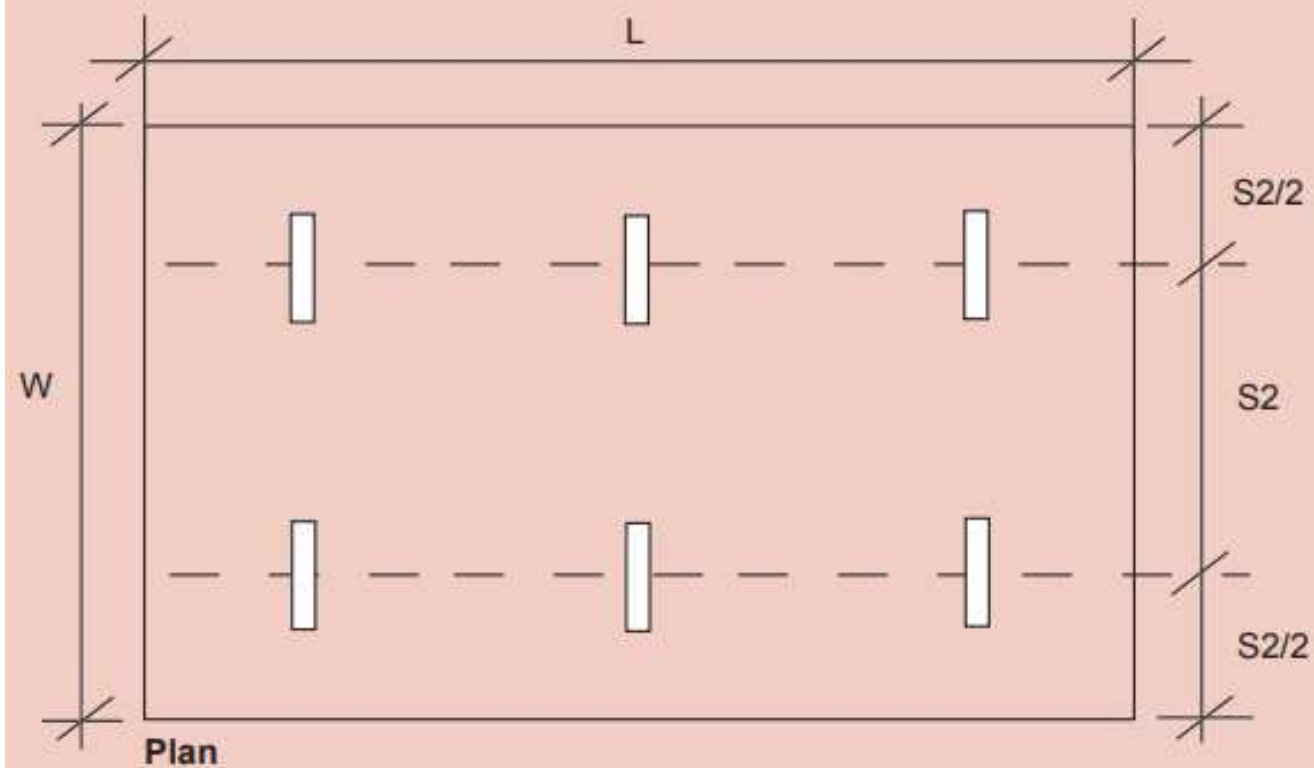
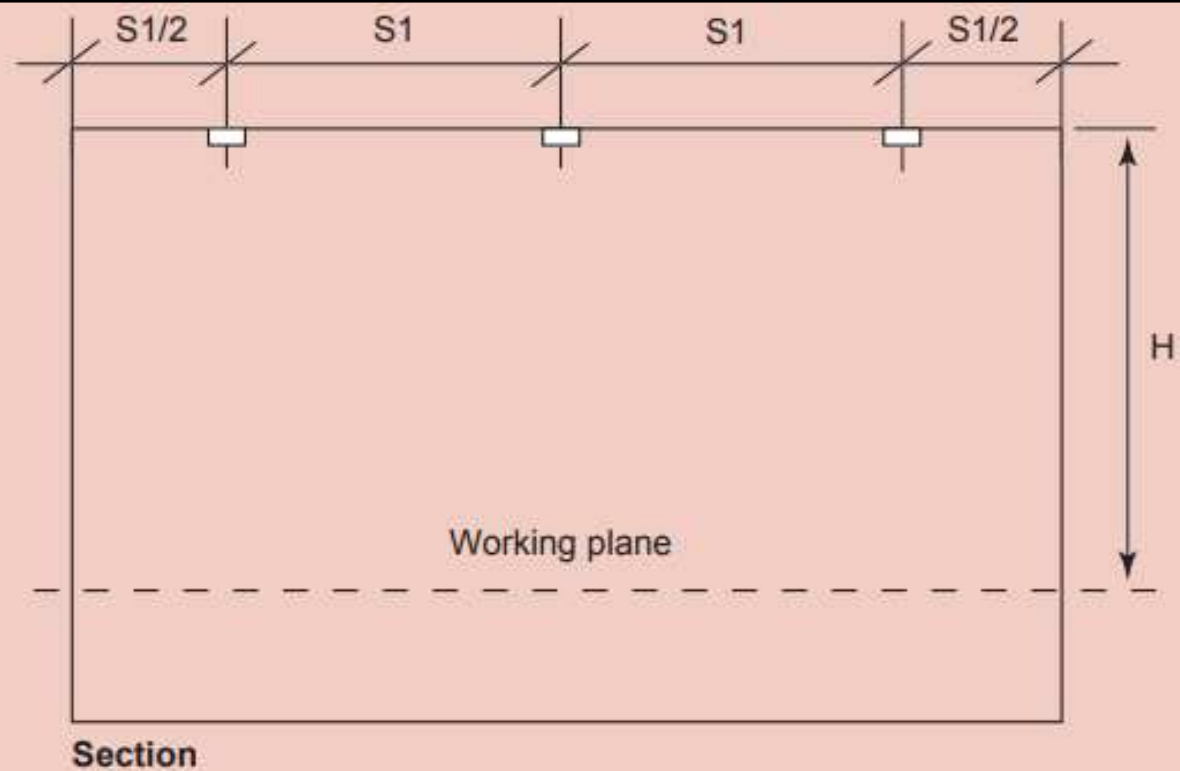
# Lumen Method

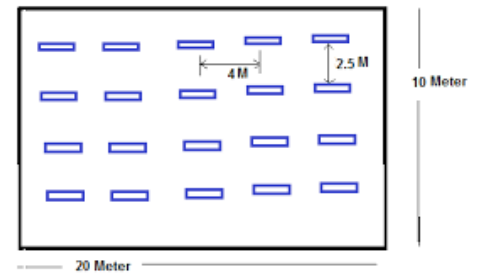
- The number of luminaires required for a required illuminance level  $E$  (lux) is:

$$N = \frac{E \times A}{F \times n \times UF \times MF}$$

- Planning the luminaire layout
  - Work out a regular layout of luminaires with an acceptable uniformity
  - Rounding the number found to a whole number that will divide into a regular grid
  - Check on the spacing to height ratio

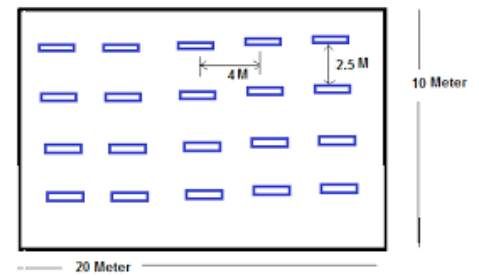
# Luminaire layout and spacing





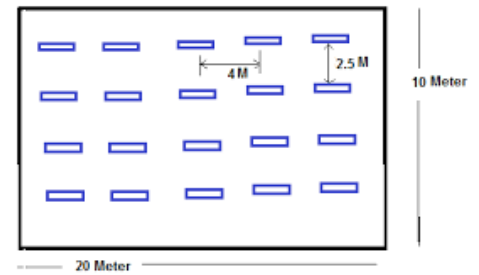
# Lumen Method

- Spacing to height ratio (SHR)
  - Ratio of distance between adjacent luminaires (centre to centre) to their height above the working plane
 
$$SHR = \frac{1}{H_m} \sqrt{\frac{A}{N}}$$
    - where  $H_m$  = mounting height;  $A$  = total floor area;  $N$  = number of luminaires
- Maximum spacing to height ratio ( $SHR_{max}$ )
  - Luminaire spacing shall not exceed the max. (provided by manufacturer) to ensure uniformity



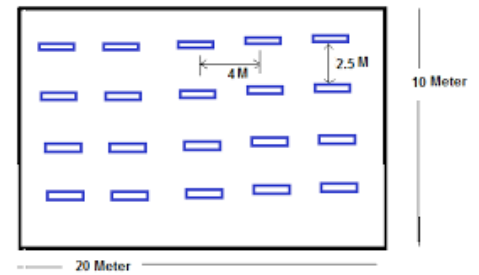
# Lumen Method

- Lumen method: calculation procedure --- a summary
  - Calculate room index  $K$ , floor/ceiling cavity index
  - Calculate effective reflectances of ceiling cavity, walls & floor cavity
  - Determine utilisation factor ( $UF$ ) from manufacturer's data, using the room index and effective reflectances
  - Determine maintenance factor ( $MF$ )
  - Obtain nos. of luminaires required
  - Determine a suitable layout
  - Check that the geometric mean spacing-to-height ratio
  - Check the layout does not exceed  $SHR_{max}$
  - Calculate illuminance achieved by the final layout



# Lumen Method

- Basic assumptions underlying the lumen method
  - Rectangular room
  - Ratio of length to width = 1.6 : 1, with a max. of 4 : 1
  - Completely empty room
  - Uniform reflectance and completely diffuse reflection properties of the perimeter surfaces
  - Uniform distribution of luminous flux over all areas
  - Regular luminaire configuration throughout the room
  - In the case of fluorescent lamps, luminaire axis = room axis



# Lumen Method

- Examples of lumen method calculations:
  - Lighting Design Calculation in a Building – Step by Step
    - <http://www.electricaltechnology.org/2017/03/lighting-design-calculation-in-building.html>
  - Lumen method calculations
    - [http://www.arca53.dsl.pipex.com/index\\_files/lummethd.htm](http://www.arca53.dsl.pipex.com/index_files/lummethd.htm)
  - The installer's guide to lighting design, Good Practice Guide 300 (page 22-26)
    - <http://www.cibse.org/getmedia/0276ac78-dc41-4694-9378-8f984ef924f2/GPG300-The-Installers-Guide-to-Lighting-Design.pdf.aspx>

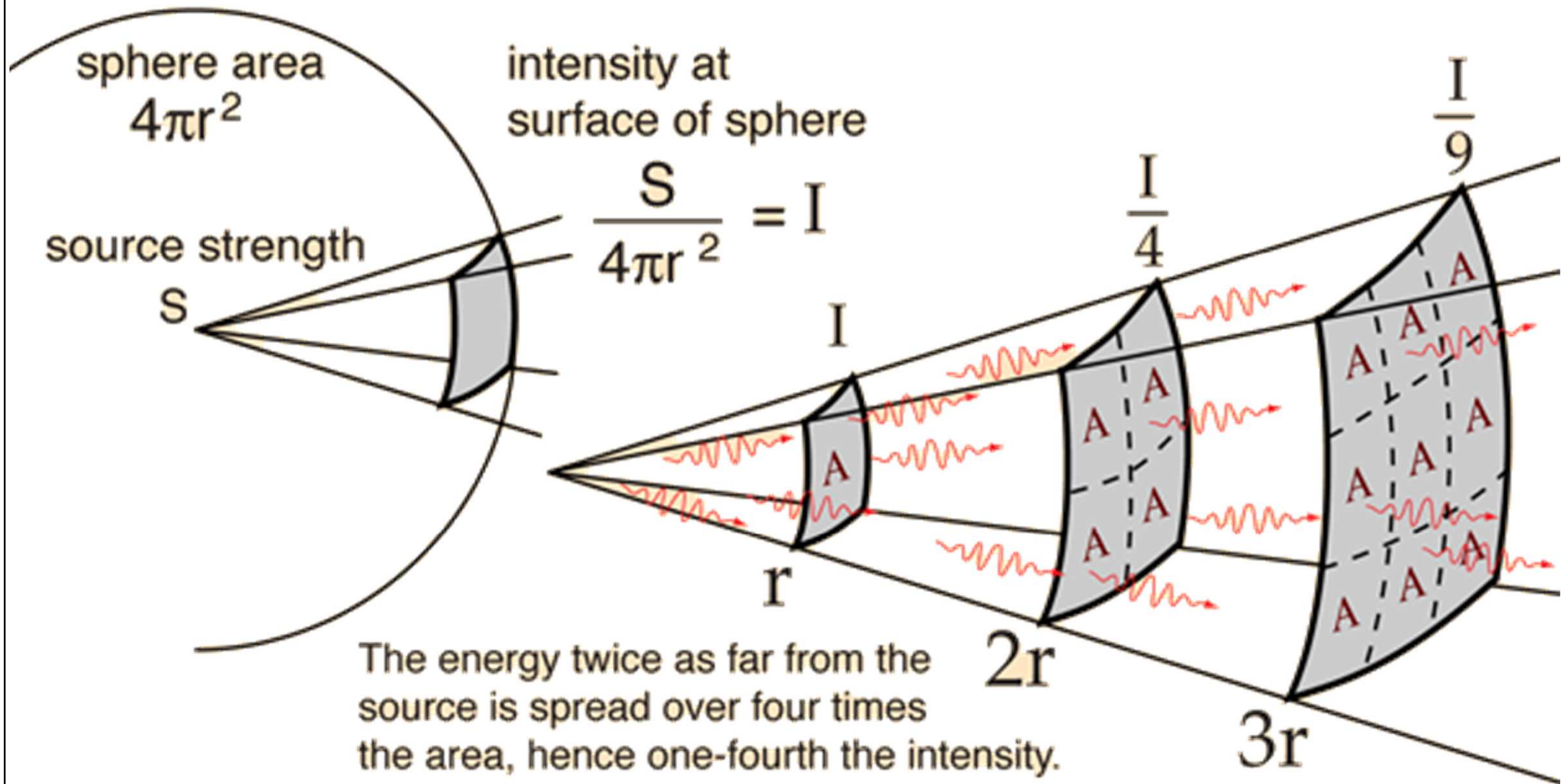
# Point-by-point Method



- Predict direct illuminance at each point on a plane, using measured data of luminous intensity distribution of a source or a luminaire
  - Based on the inverse square law and cosine law
- Three factors must be considered:
  - Luminous intensity
  - Distance
  - Orientation of the surface

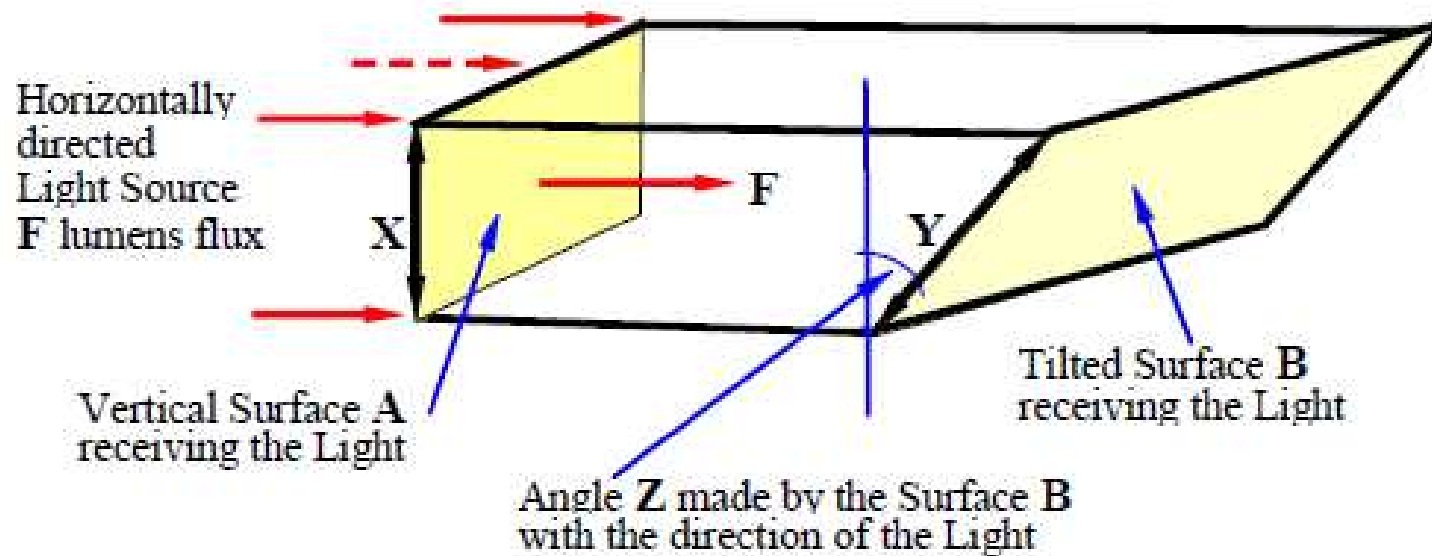


## Inverse Square Law for lighting calculations



# Cosine Law for lighting calculations

## COSINE LAW (Illuminance on Tilted Surface)



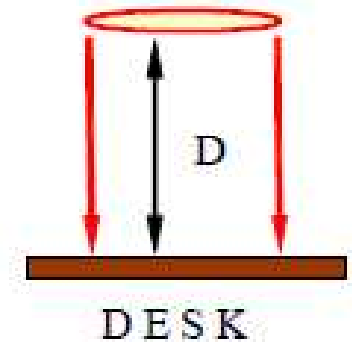
The Areas A and B are proportional to the lengths of their sides X and Y

$$A / B = \cos (Z) \quad B = A / \cos (Z) \quad \text{Illuminance } E_A = F / A$$

$$\text{Illuminance } E_B = F / B = F / (A / \cos (Z)) = F / A * \cos (Z) = E_A * \cos (Z)$$

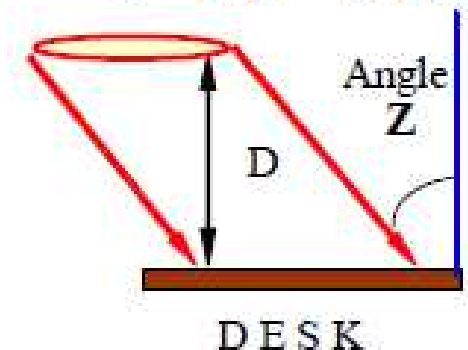
$E = I / D^2$  when the incident angle is 0 degrees.  
The general equation becomes  $E = I / D^2 * \cos (Z)$

Light Source Intensity =  
I Candelas  $E = I / D^2$



Light Source Intensity =  
I Candelas

$$E = I / D^2 * \cos (Z)$$



## Cosine Values of Angles

0	6	12	18	24	30	36	42	48	54	60	66	72	78	84	90
1.000	0.995	0.978	0.951	0.914	0.866	0.809	0.743	0.669	0.588	0.500	0.407	0.309	0.208	0.105	0.000

# Point-by-point Method



- Video:
  - Lighting Point by Point (5:08)
    - <http://www.youtube.com/watch?v=C8ZKNOvDmCQ>
- Limits for using point by point method:
  - Maximum physical dimension of the surface under design is not larger than  $\frac{1}{5}$ th the mounting height above the evaluation point
  - Does not apply to a surface of infinite length

# Point-by-point Method



- **Computer software** can be used to perform numerical point-by-point calculations of direct or reflected light incident on any real surface or imaginary plane
  - The results can be used to predict or quantify the distribution of artificial or natural light in any environment (lighting simulation)
    - Brightness of room surfaces and patterns of light on the ceiling, walls, and floor
    - Also lighting quality & visual performance

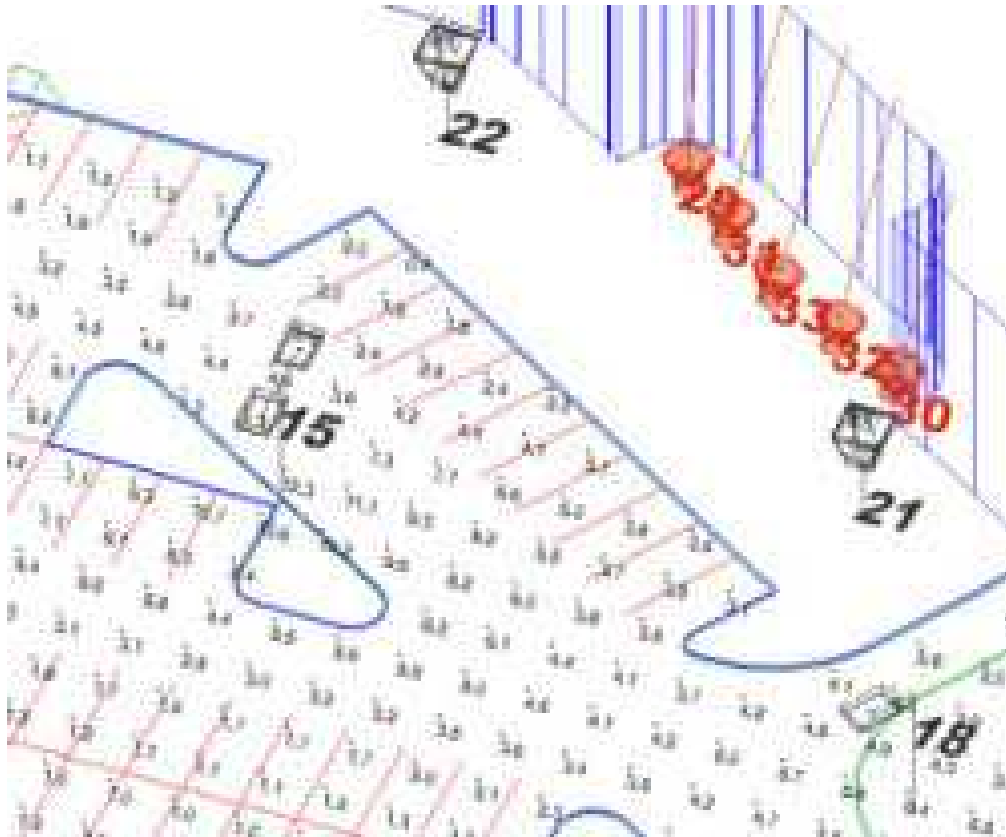
# Point-by-point Method



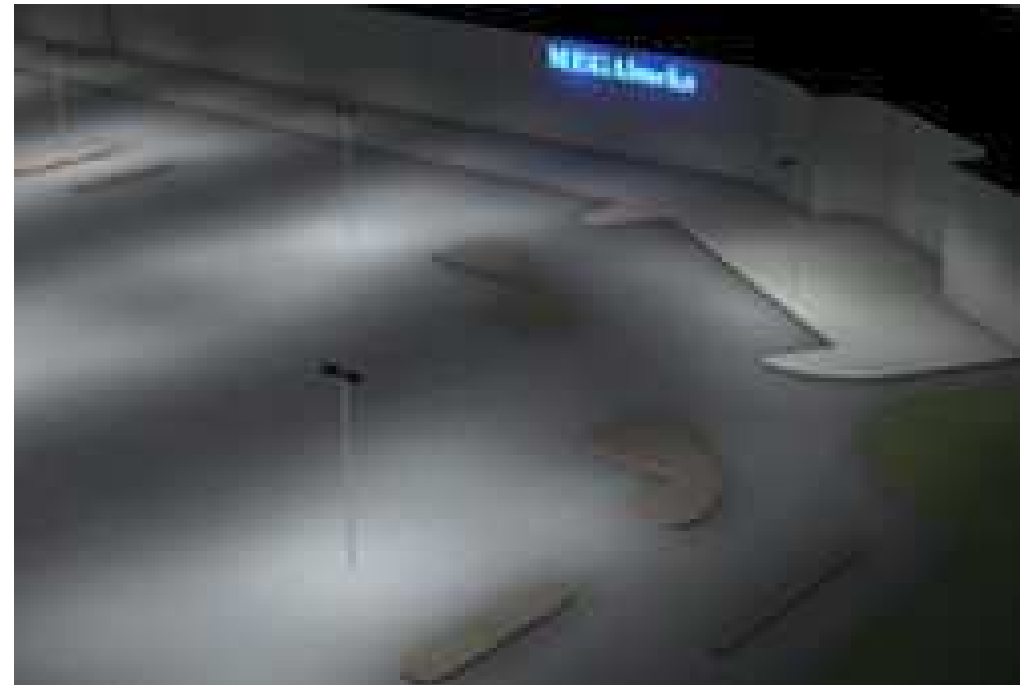
- Two calculation techniques when simulating a lighting application
  - Direct Calculation Method
    - A simplified technique when reflected light need not be considered in the results; often used in exterior lighting applications e.g. road and sports lighting
    - It cannot be rendered
  - Full Radiosity Method
    - Accurate computation of interreflected light; for interior lighting applications or when rendering is desired

# Two calculation techniques for simulating a lighting application

## Direct calculation

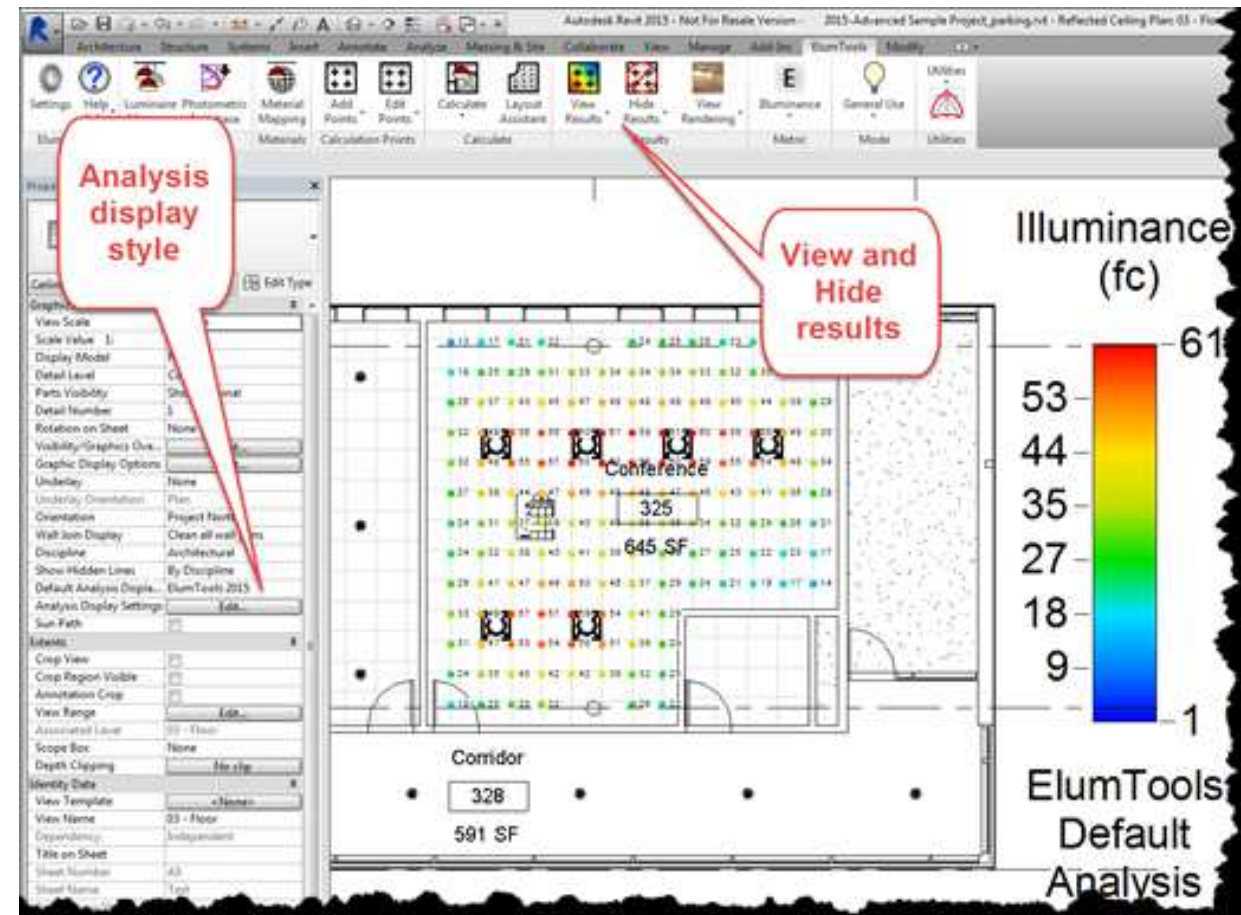
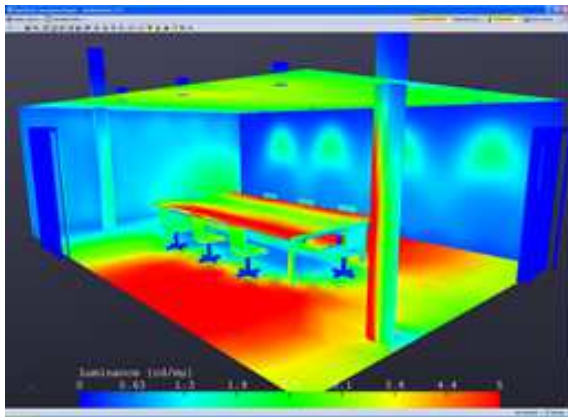
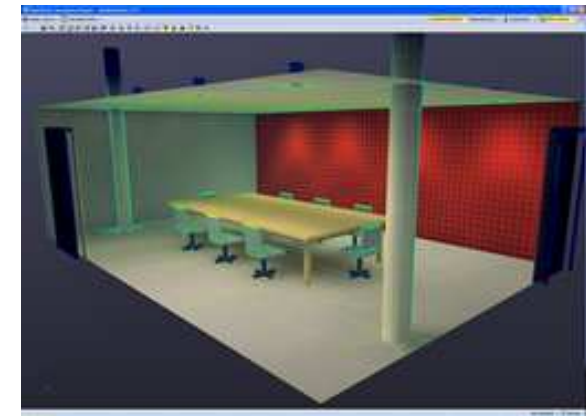
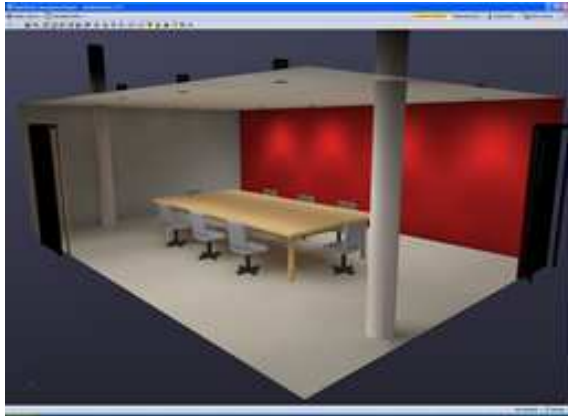


## Full Radiosity calculation

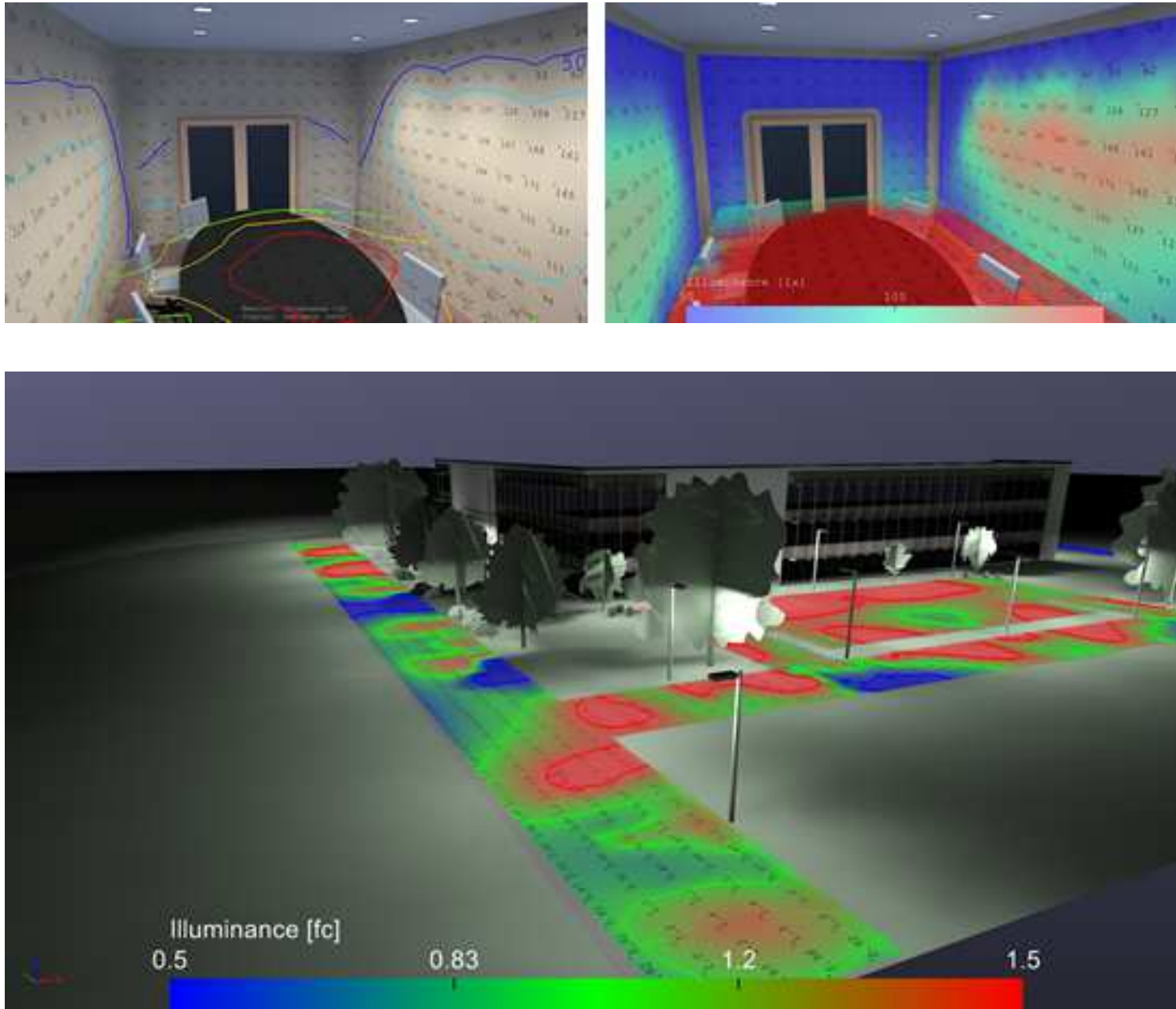




# Lighting calculations and simulation in Revit BIM using ElumTools



# Using isolines and spatial maps to evaluate the gradient of light across a workplane or surface





# Other Calculations



- Lighting to provide local emphasis
  - Emphasis or accent lighting is used to draw attention to an area or an object, e.g. a reception desk in an entrance area or a display in a shop
  - The amount of light needed to emphasise or draw attention to an object depends on the level of general lighting
  - Ratio of display light to general lighting:
    - ‘Subtle’ effect --- 5 : 1
    - ‘Moderate’ emphasis --- 15 : 1
    - ‘Strong’ emphasis --- 30 : 1

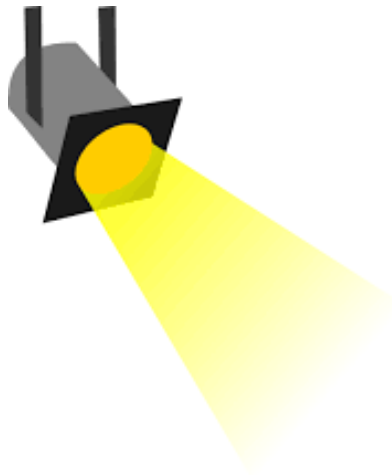
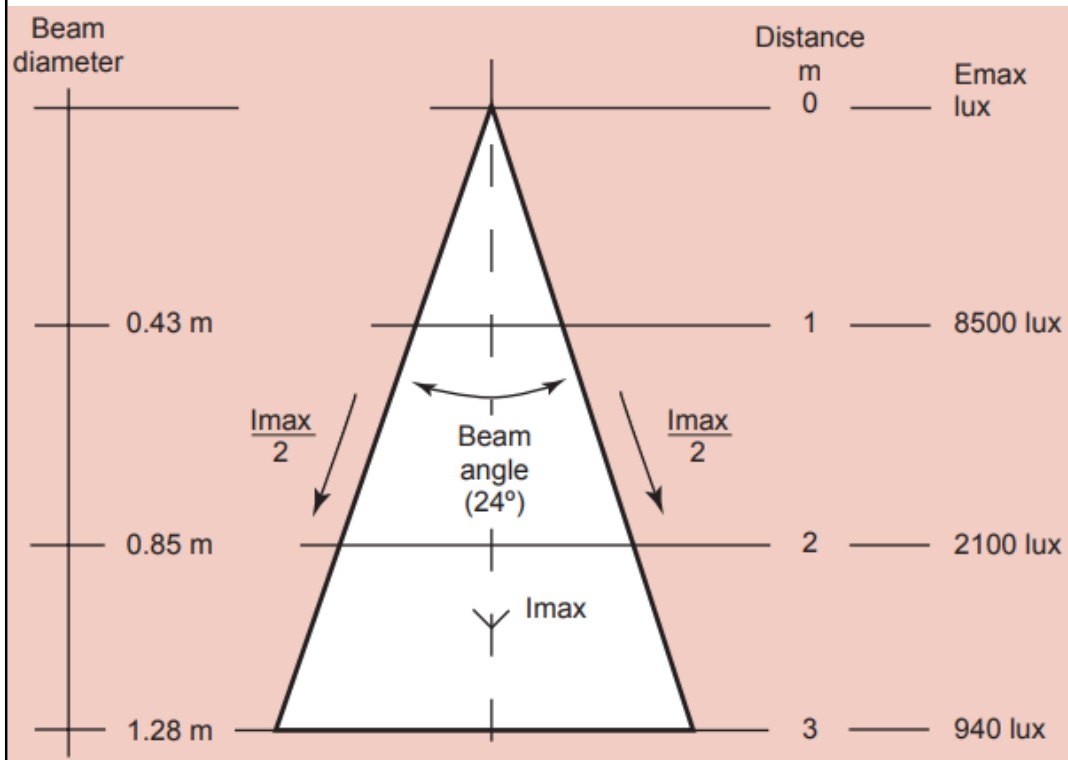
# Other Calculations



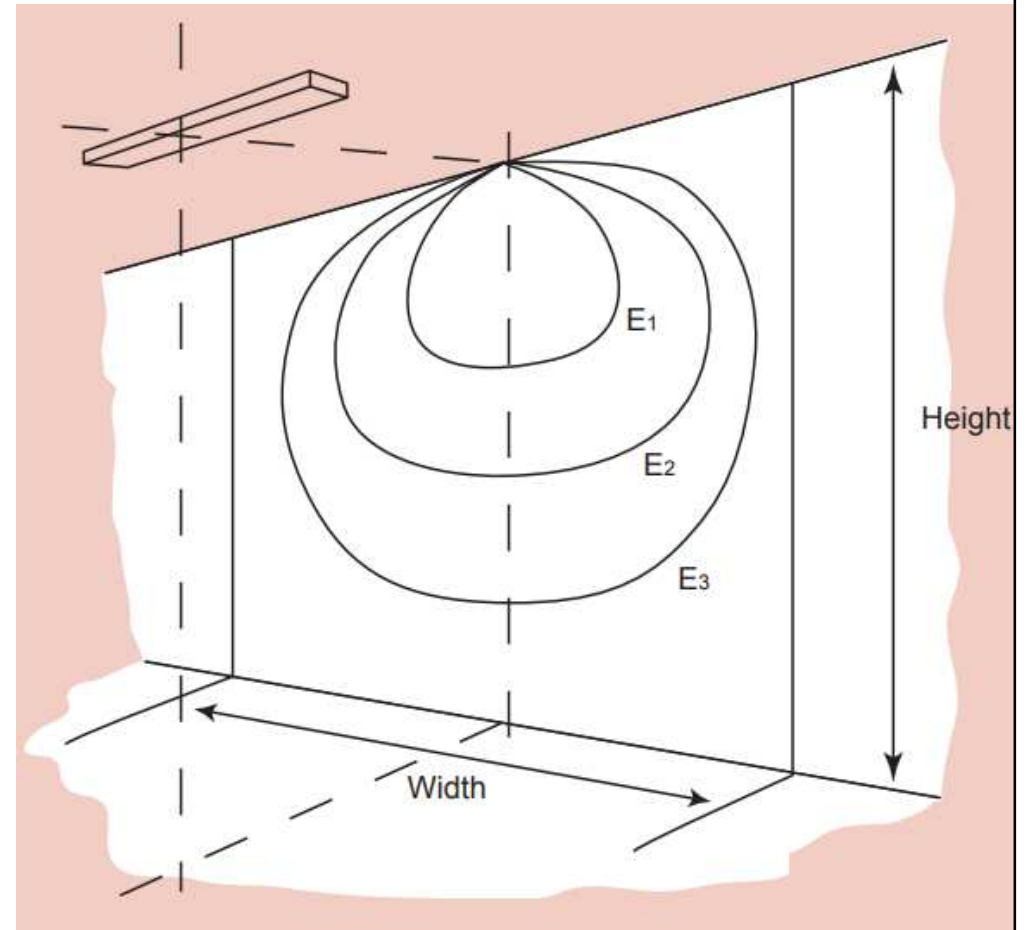
- Example: Use spotlight for local emphasis
  - Manufacturers usually provide information in a diagrammatic form showing the effect of a particular spotlight at various distances
    - Width of the beam and either the illuminance at the beam centre or the average illuminance across the beam
    - Calculate the illuminance from a spotlight or any other small source using the ‘point source formula’
  - Wall washing: This uses luminaires that usually have an asymmetric beam shape. The manufacturers usually provide details of the luminaire layout and illuminance performance

# Typical performance data for spotlight and wall-washing luminaire

## Spotlight



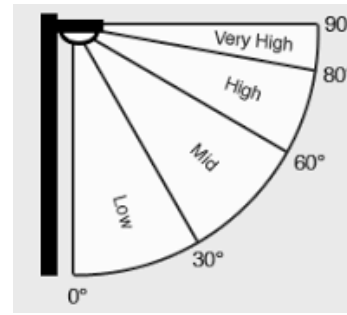
## Wall-washing luminaire



# Other Calculations



- Outdoor area lighting design, such as floodlighting, sports and road lighting
  - Area lighting Design Calculations - Part One
    - <http://www.electrical-knowhow.com/2013/01/area-lighting-design-calculations-part.html>



- Daylighting and daylight factor
  - <http://personal.cityu.edu.hk/~bsapplec/methods.htm>

# Other Calculations



- Other lighting system related calculations:



- Checking for energy efficiency
  - Local building/lighting energy efficiency code
  - Average installed power density ( $\text{W}/\text{m}^2$ )
- Energy-saving payback calculations
  - Demonstrate to a client that the additional cost of installing efficient equipment is worthwhile is by calculating payback period – the length of time before the savings match the extra initial cost
    - $\text{Payback} = (\text{the extra initial cost}) / (\text{annual cost savings})$
  - After this period, the user has saved more than he has spent and continues to save money



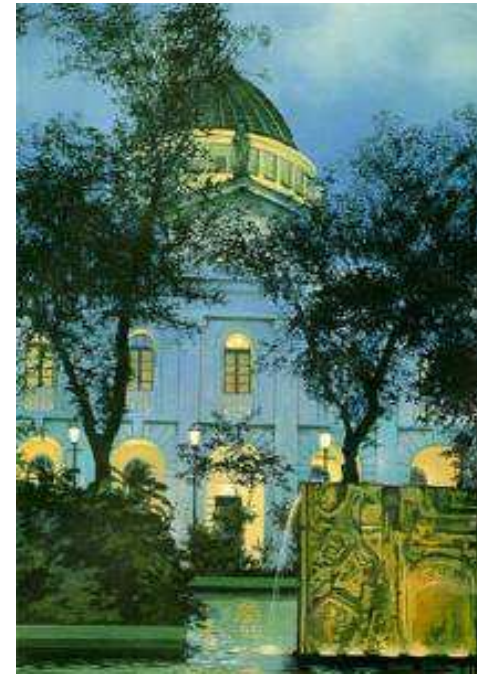
# Outdoor Lighting



- Outdoor (or exterior) lighting
  - Floodlighting: flooding a surface with light
    - Achieve illumination on vertical or horizontal surfaces
  - Design issues
    - Appearance during daytime
    - Glare from the installation
    - Decorative lighting
    - Lighting for specific outdoor activities e.g. sports
  - Applications:
    - Building façade, sports, road lighting



# Legislative Council Building (now Court of Final Appeal) at daytime and night-time



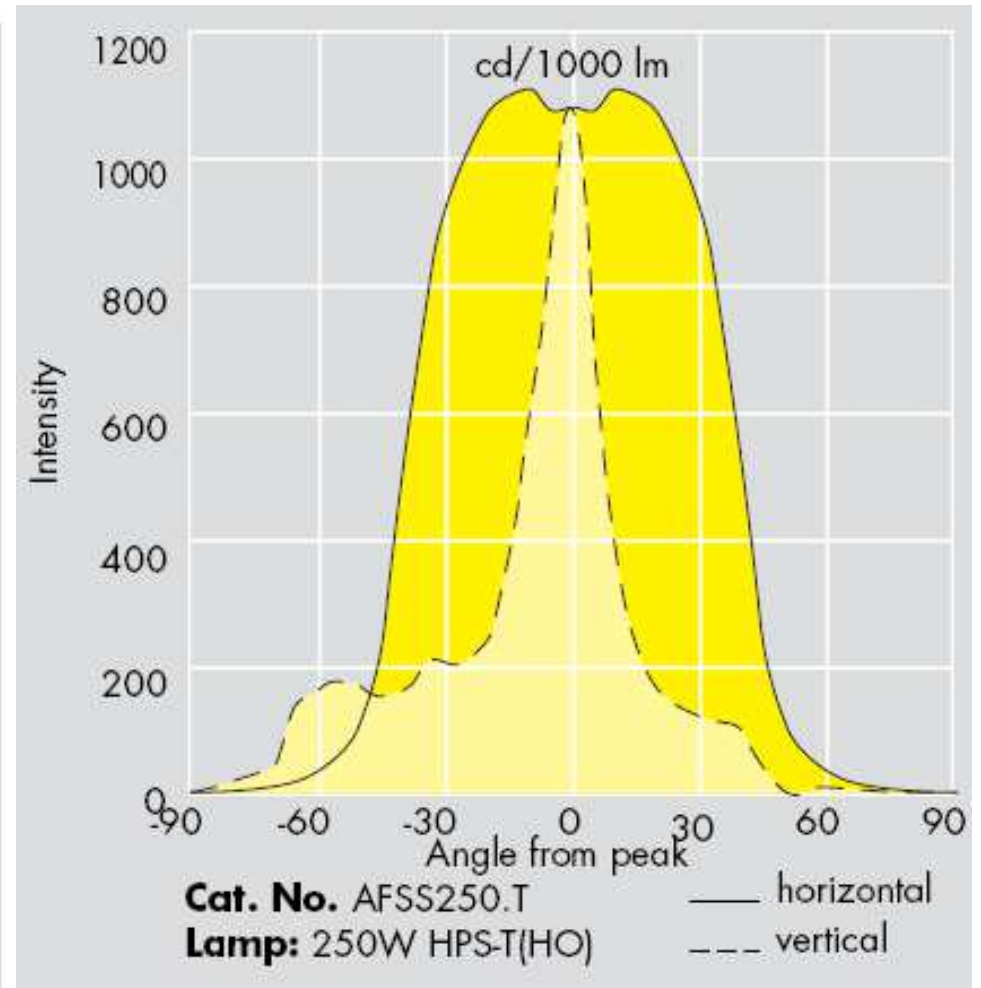
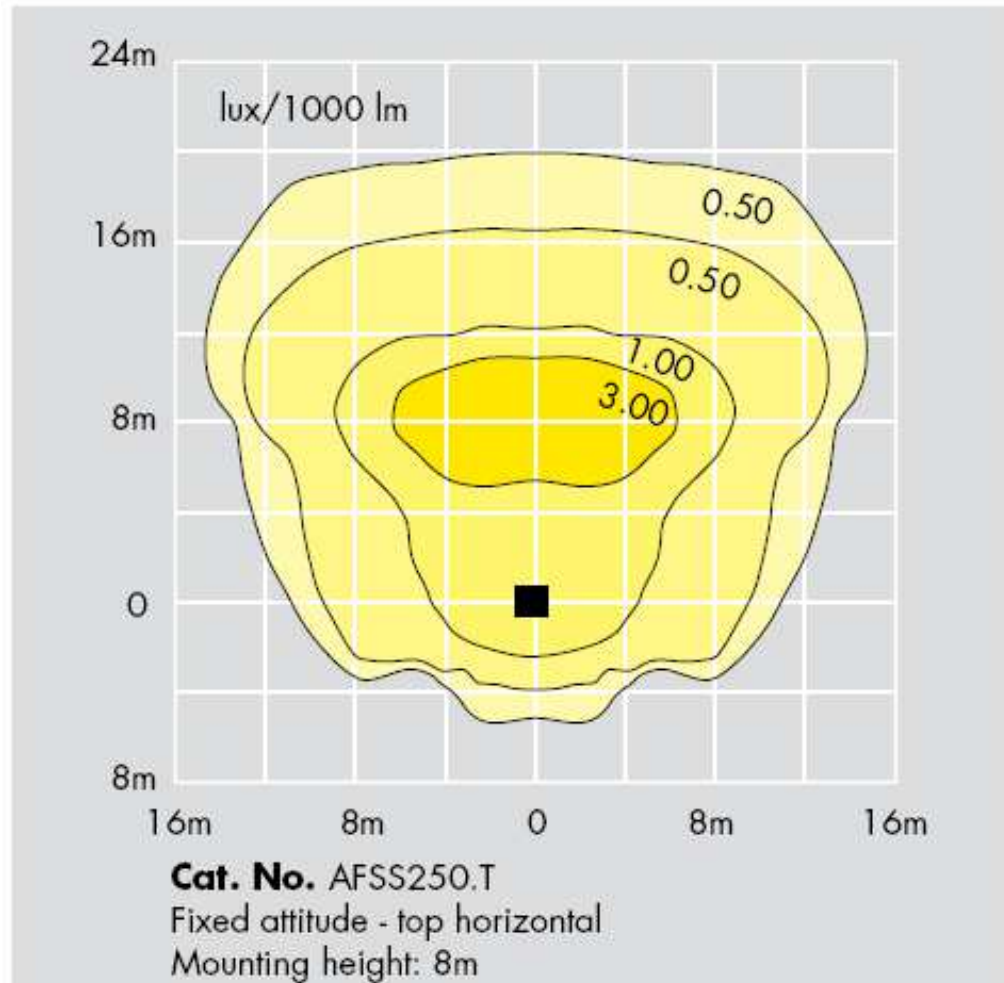
# Outdoor Lighting



- Outdoor lighting (cont'd)
  - Floodlighting a building
    - Requires a sense of drama and colour
    - Select locations for putting floodlights & aiming points
      - Peak intensity & beam angle
    - Usually all the beams from each floodlight shall overlap
      - Uniformity ratio (max : average) about 5:1
  - Floodlighting a horizontal open area
    - Use isolux diagram (horizontal illumination plots)
      - Or isocandela and zonal flux diagram
    - Calculate using inverse square law and cosine law

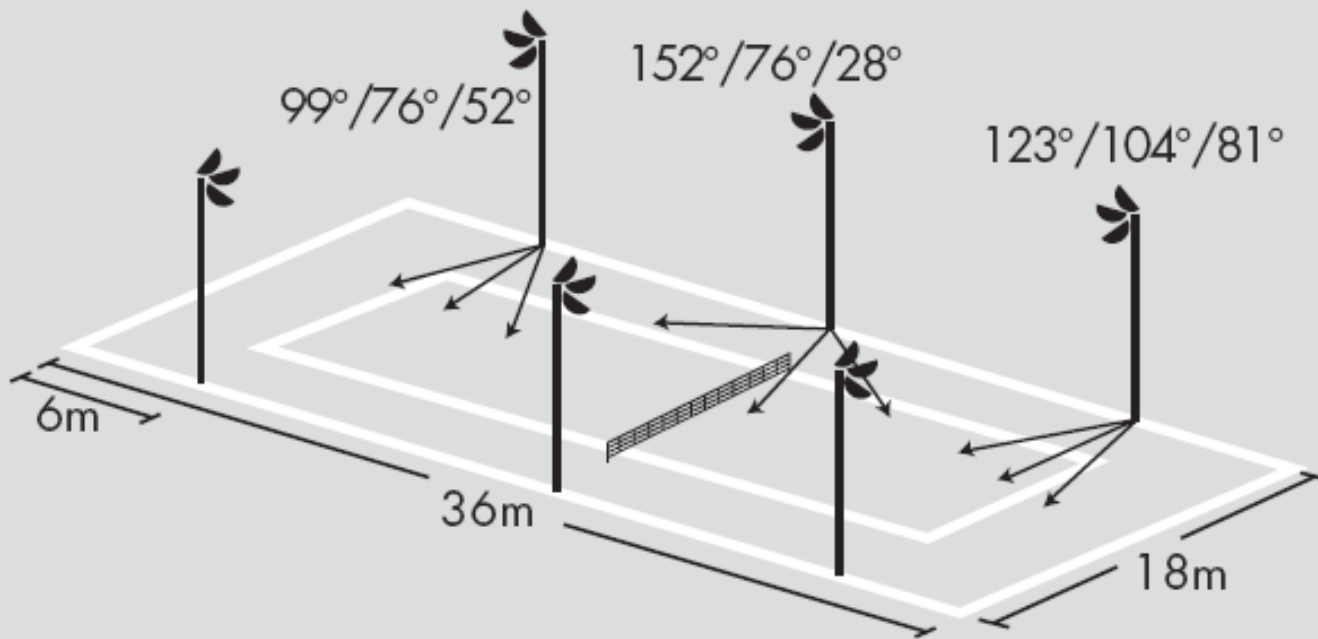


# Floodlight Data



Floodlight design data  
[Source: Thorn Lighting, UK]

# Troika



Aiming angles given

**Class 2 Competition**  
**Mounting height:** 8m  
**Maintenance factor:** 0.8

**Cat. No:** QTKA2540MSE40  
+ CON2HQT400.4

**Lamp:** 18 x HIT 400W

**Lumens:** 38000

**Lux:** 300 avg

**Lamp position:** 1

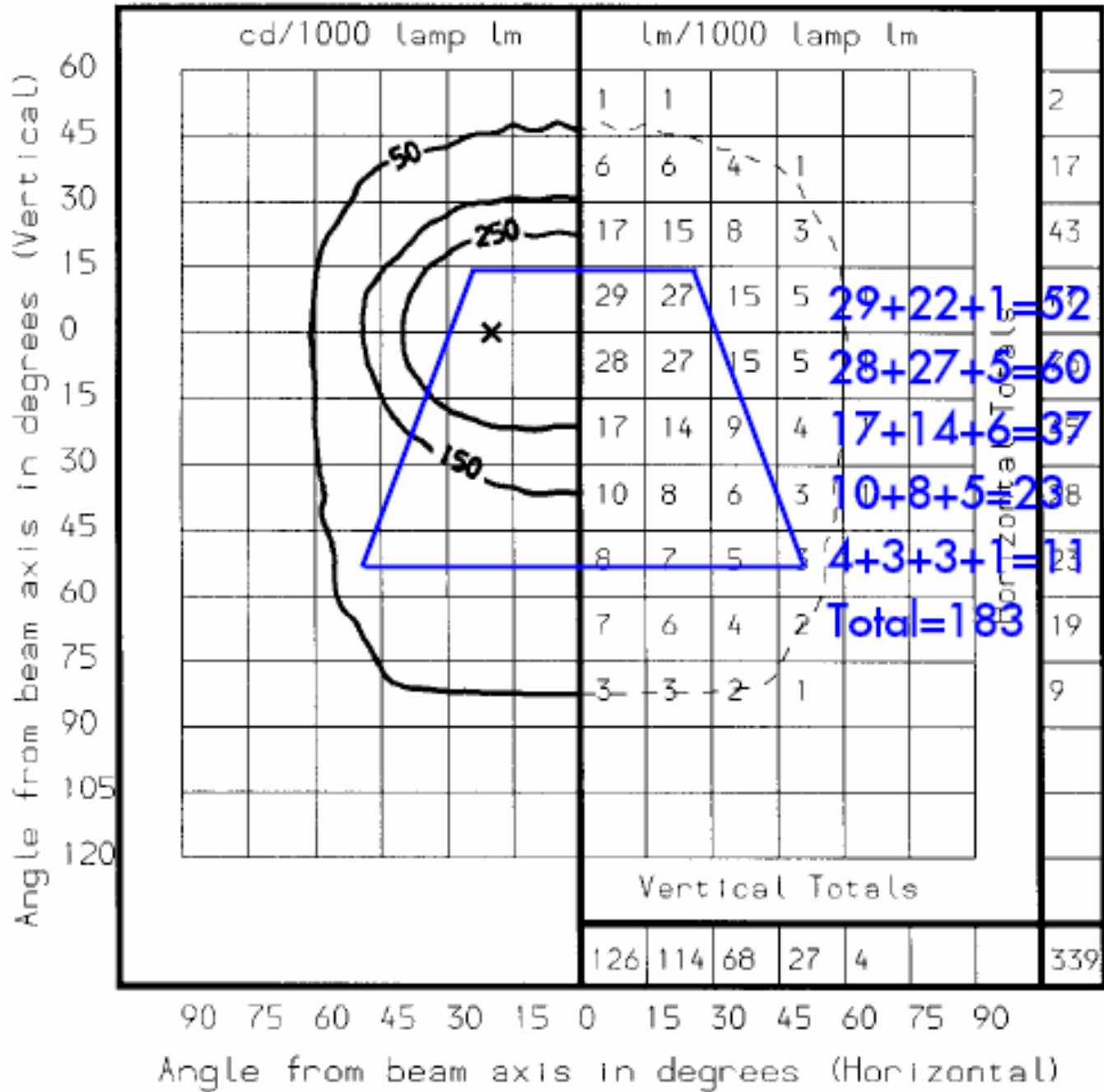
**Uniformity:** 0.8

**Glare rating:** 41

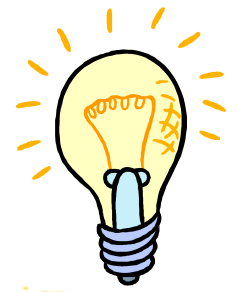
Sample floodlight design for a tennis court

[Source: Thorn Lighting, UK]

### Isocandela and zonal flux diagram



[Source: Thorn Lighting, UK]



# Further Reading

- e-light: LEARN: the different stages of the lighting design process <http://iarc.uncg.edu/elight/learn/learn.html>
  - Establish design criteria  
<http://iarc.uncg.edu/elight/learn/establish/est.html>
  - Record architectural constraints  
<http://iarc.uncg.edu/elight/learn/record/record.html>
  - Determine visual functions and tasks  
<http://iarc.uncg.edu/elight/learn/determine/deter.html>
  - Design light distribution  
<http://iarc.uncg.edu/elight/learn/design/design.html>
  - Qualitative and quantitative results  
<http://iarc.uncg.edu/elight/learn/qualitative/qual.html>



# Further Reading

- Lighting Design Calculation in a Building – Step by Step
  - <http://www.electricaltechnology.org/2017/03/lighting-design-calculation-in-building.html>
- The installer's guide to lighting design, Good Practice Guide 300
  - <http://www.cibse.org/getmedia/0276ac78-dc41-4694-9378-8f984ef924f2/GPG300-The-Installers-Guide-to-Lighting-Design.pdf.aspx>



# References

- SLL, 2009. *The SLL Lighting Handbook*, Society of Light and Lighting (SLL), Chartered Institution of Building Services Engineers, London.
  - Chapter 6: Lighting design
- Raynham, P., 2012. *The SLL Code for Lighting*, Society of Light and Lighting (SLL), London.
  - Chapter 12: Photometric datasheets
  - Chapter 13: Indoor lighting calculations
  - Chapter 14: Outdoor lighting calculations